

Post-suppositions and uninterpretable questions*

Linmin Zhang^{1,2}[0000-0002-7864-125X]

¹ NYU Shanghai, ² NYU-ECNU Institute of Brain & Cognitive Science
zhanglinmin@gmail.com linmin.zhang@nyu.edu
<https://sites.google.com/site/zhanglinmin/>

1 **Abstract.** For a sentence like *exactly three boys are between 5 feet 10*
2 *inches and 6 feet tall*, why cannot we abstract the height information
3 out and raise a corresponding degree question like *#How tall are ex-*
4 *actly three boys?* Inspired by the ideas that (i) there is a connection
5 between *wh*-questions (e.g., *who did Mary kiss*) and definite descrip-
6 tions (e.g., *the people that Mary kissed*) and (ii) definite descriptions and
7 modified numerals (e.g., *exactly three boys*) bring post-suppositions (i.e.,
8 delayed evaluations that lead to relative definiteness, [Brasoveanu 2013](#),
9 [Bumford 2017](#)), I propose that when different elements that bring post-
10 suppositions are present, a potential conflict arises in computing relative
11 definiteness, leading to uninterpretability.

12 **Keywords:** Dynamic semantics · Post-suppositions · *Wh*-questions ·
13 Degree questions · Modified numerals · Cumulative reading · Definiteness
14 · Weak island effects · Intervention effects

15 1 Introduction

16 This paper aims to explain the unacceptability of sentences like (2b): a **con-**
17 **stituent question** containing a **modified numeral**.

- 18 (1) a. Brienne is between 5'10" and 6' tall.
19 b. How tall is Brienne?
20 (2) a. Exactly three boys are between 5'10" and 6' tall.
21 b. #How tall are exactly three boys?

22 For a sentence like (1a), we can naturally abstract the height information
23 (the underlined part) out and raise a corresponding degree question on Brienne's
24 height (see (1b)). Intriguingly, in contrast to (1), for a sentence like (2a), which
25 contains a modified numeral (here *exactly three boys*), abstracting the height
26 information out to form a corresponding degree question does not work, yielding
27 an intuitively unacceptable sentence (see (2b)).

* This project was financially supported by the Program for Eastern Young Scholars at Shanghai Institutions of Higher Learning (to L.Z.). The current paper supersedes an earlier manuscript included in the Pre-Conference *Proceedings of LENLS16* ([Zhang 2019](#)). I thank Anna Szabolcsi and the anonymous reviewers and audience of both LENLS16 and TLLM2022 for comments and feedback. Errors are mine.

28 The uninterpretability of constituent questions like (2b) does not seem like an
 29 entirely new observation. Similar unacceptable question phenomena have been
 30 reported in the literature on **intervention effects** or **weak island effects** (see,
 31 e.g., Szabolcsi and Zwarts 1993, Szabolcsi 2006, Rullmann 1995, Honcoop 1996,
 32 Beck 1996, 2006, Fox and Hackl 2007, Abrusán 2014).

33 As illustrated by the contrast between (3a) and (3b) (i.e., *wh*-in-situ vs. *wh*-
 34 movement), **intervention effects** arise when an intervener (here the negation
 35 expression *koi nahiiN*) precedes a *wh*-word (here *kyaa*) in a *wh*-question. This
 36 kind of intervention effects are often attested in *wh*-in-situ languages (e.g., Hindi,
 37 Korean). Cross-linguistically, typical interveners include, but are not limited to,
 38 focus particles and downward entailing (DE) quantifiers (e.g., *no*, *few*, *at most*).

- 39 (3) **Intervention effects:** examples from Beck (2006)
- 40 a. ?? koi **nahiiN** kyaa paRhaa
 anyone not what read-Perf.M
 Intended: ‘What did no one read?’ (Hindi: (12a) in Beck 2006)
- 41 b. kyaa koi **nahiiN** paRhaa
 what anyone not read-Perf.M
 ‘What did no one read?’ (Hindi: (12b) in Beck 2006)

44 **Islands** refer to domains which prevent the displacement of items contained
 45 within them, and **weak islands** are those that are only closed for some kinds
 46 of items, but not all kinds of items (see Szabolcsi 2006, Abrusán 2014). As
 47 illustrated by (4), negation words or DE quantifiers create **weak islands effects**
 48 in the formation of a degree question (see (4a) and (4c)), *how-many* question
 49 (see (4b)), or manner question (see (4d)). In contrast, negation words or DE
 50 quantifiers do not create islands for the displacement of items like *which book*
 51 (see (5)). Elements that create weak island effects are also not limited to negation
 52 operators or DE quantifiers.

- 53 (4) **Weak island effects:** examples from Abrusán (2014)
- 54 a. #How tall isn’t John? (§3.4, (32a))
- 55 b. ??How many children does **none of these women** have? (§5.3, (19))
- 56 c. #How far did **few girls** jump? (§5.3, (24c))
- 57 d. #How did **at most 3 girls** behave? (§5.3, (24e))
- 58 (5) a. Which book haven’t you read? (Abrusán 2014: §1.1, (3))
- 59 b. Which book did { **no one** / **few girls** / **at most 3 girls** } read?

60 Within the existing literature, there are already a variety of proposals on
 61 intervention effects or weak island effects, sometimes with different empirical
 62 coverages. The pattern ‘modified numeral + degree question’ (see (2b)) seems
 63 relevant, but it has not been much studied as a core piece of data. In this paper,
 64 I propose to start with the special property of modified numerals that they bring
 65 post-suppositions (Brasoveanu 2013) and explore how far this new perspective
 66 can advance our understanding of sentences like (2b) as well as empirical data
 67 related to intervention effects or weak island effects.

68 In a nutshell, I adopt and develop existing ideas in the literature on *wh*-
 69 questions: there is a connection between the interpretation of *wh*-questions (e.g.,
 70 *who did Mary kiss*) and definite descriptions (e.g., *the people that Mary kissed*).
 71 Then given that definite descriptions and modified numerals are both elements
 72 that bring **post-suppositions** (see Brasoveanu 2013, Bumford 2017), i.e., de-
 73 layed evaluations that result in a deterministic update with relative definiteness,
 74 the presence of both these kinds of items in the same sentence potentially yields
 75 a conflict with regard to relative definiteness, leading to uninterpretability. I will
 76 also address how this potential uninterpretability can be circumvented.

77 In the following, Section 2 first presents how modified numerals and defi-
 78 nite descriptions contribute post-suppositions (Brasoveanu 2013, Bumford 2017).
 79 Section 3 argues for a parallel analysis for interpretable *wh*-questions and mod-
 80 ified numerals / definite descriptions. Based on this, Section 4 accounts for the
 81 uninterpretability of the core data under discussion (see (2b)). Section 5 com-
 82 pares the current proposal with existing approaches developed within the litera-
 83 ture on intervention effects and weak island effects and shows advantages of the
 84 current proposal. Section 6 concludes.

85 2 Post-suppositions

86 2.1 Brasoveanu (2013): Modified numerals as post-suppositions

87 Modified numerals bring **post-suppositions**: their numerical information is at-
 88 tached to a **non-local, sentence-level maximization** (Brasoveanu 2013).

89 The maximization effect of modified numerals has been widely reported in the
 90 literature (see, e.g., Szabolcsi 1997, Krifka 1999, de Swart 1999, Umbach 2006,
 91 Zhang 2018). As illustrated by the contrast in (6), compared to bare numerals
 92 like *two dogs*, modified numerals like *at least two dogs* exhibit maximality, as
 93 evidenced by the infelicitous continuation *perhaps she fed more*. In other words,
 94 while the semantic contribution of *two* in (6a) is **existential**, *at least two* in
 95 (6b) conveys the quantity information of the **totality** of dogs fed by Mary.

- 96 (6) a. Mary fed two dogs. They are cute. Perhaps she fed more.
 97 b. Mary fed at least two dogs. They are cute. #Perhaps she fed more.

98 The non-localness of this maximization is best reflected in the **cumulative**
 99 **reading** of sentences like (7). (7) has a distributive reading (7a) and a cumulative
 100 reading (7b), and we focus on the cumulative reading (7b) here. (For notation
 101 simplicity, cumulative closure is assumed for lexical relations when needed.)

- 102 (7) Exactly 3 boys saw exactly 5 movies.
 103 a. **Distributive reading:**
 104
$$\sigma x[\text{BOY}(x) \wedge \delta x[\underbrace{\sigma y[\text{MOVIE}(y) \wedge \text{SEE}(x, y)]}_{\text{the mereologically maximal } y}] \wedge |y| = 5]] \wedge |x| = 3$$

$$\underbrace{\hspace{10em}}_{\text{the mereologically maximal } x}$$
 105 (σ : maximality operator; δ : distributivity operator.)

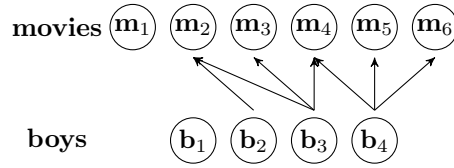


Fig. 1. The **cumulative** reading of *exactly 3 boys saw exactly 5 movies* is **true** under this scenario.

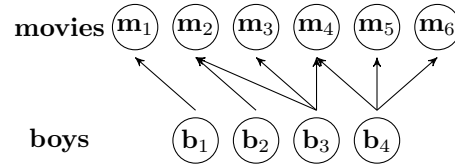


Fig. 2. The **cumulative** reading of *exactly 3 boys saw exactly 5 movies* is **false** under this scenario.

106 (There are in total three boys, and for each atomic boy, there are in
107 total 5 movies such that he saw them.)

108 b. **Cumulative reading:**

$$109 \quad \underbrace{\sigma x \sigma y [\text{BOY}(x) \wedge \text{MOVIE}(y) \wedge \text{SEE}(x, y)]}_{\text{the mereologically maximal } x \text{ and } y} \wedge |y| = 5 \wedge |x| = 3$$

110 (The cardinality of all the boys who saw any movies is 3, and the
111 cardinality of all movies seen by any boys is 5.)

112 **True** under the context of Fig. 1, **false** under the context of Fig. 2.

113 According to the intuition of native speakers, sentence (7) is true under the
114 scenario described by Fig. 1, but false under the scenario described by Fig. 2.

115 It is worth noting that if we adopt the analysis shown in (8), then sentence (7)
116 should be judged true under the scenario of Fig. 2: there are two such boy-sum
117 witnesses, namely $b_2 \oplus b_3 \oplus b_4$ and $b_1 \oplus b_2 \oplus b_4$, and for each of these two boy-sums,
118 (i) their cardinality is 3, and (ii) the maximal sum of movies seen between them
119 has the cardinality of 5 ($m_2 \oplus m_3 \oplus m_4 \oplus m_5 \oplus m_6$ and $m_1 \oplus m_2 \oplus m_4 \oplus m_5 \oplus m_6$,
120 respectively). There are no larger boy-sums such that they saw in total 5 movies
121 between them. Thus the contrast of intuition (i.e., (7) is true under Fig. 1, but
122 false under Fig. 2) means that (i) the genuine cumulative reading shown in (7b)
123 is distinct from the unattested pseudo-cumulative reading shown in (8), and (ii)
124 there is no scope-taking between the two modified numerals in (7), *exactly 3 boys*
125 and *exactly 5 movies* (see Brasoveanu 2013, Charlow 2017).

126 (8) **Unattested pseudo-cumulative reading** of (7): Not attested!

$$127 \quad \underbrace{\sigma x [\text{BOY}(x) \wedge \underbrace{\sigma y [\text{MOVIE}(y) \wedge \text{SEE}(x, y)]}_{\text{the mereologically maximal } y}}] \wedge |y| = 5}_{\text{the mereologically maximal } x} \wedge |x| = 3$$

128 (The maximal plural individual x satisfying the restrictions (i.e., atomic
129 members of x are boys, each atomic boy saw some movies, and the boys
130 in x saw a total of 5 movies between them) has the cardinality of 3.)

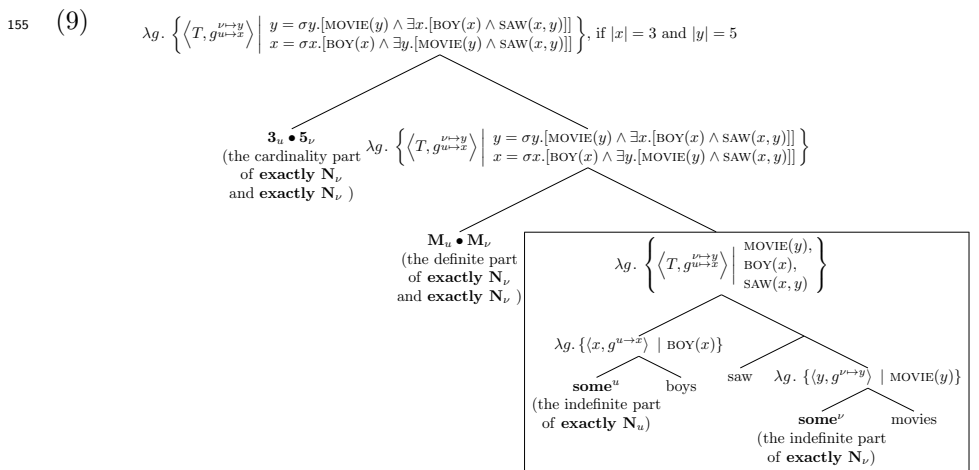
131 **True** under the context of Fig. 2 (see $b_2 \oplus b_3 \oplus b_4$ and $b_1 \oplus b_2 \oplus b_4$)!

132 As already pointed out by Krifka (1999), the semantic contribution of both
133 modified numerals in (7), *exactly 3 boys* and *exactly 5 movies*, should take place
134 simultaneously, at the sentential level, beyond their hosting DPs themselves:

135 The problem cases discussed here clearly require a representation in
 136 which NPs are not scoped with respect to each other. Rather, they ask
 137 for an interpretation strategy in which all the NPs in a sentence are
 138 somehow interpreted on a par. (Krifka 1999)

139 Given Fig. 1, in interpreting (7), we count the cardinalities of all boys who
 140 saw any movies and all movies seen by any boys, instead of the total cardinalities
 141 of all boys and movies in the domain (here in Fig. 1, it's 4 boys and 6 movies).
 142 Therefore, the application of maximality operators is subject to more restrictions
 143 (here in our context, not just boys, but boy who saw movies; not just movies,
 144 but movies seen by boys), leading to a **relativized maximization** effect.

145 A compositional analysis à la Bumford (2017) is sketched in (9). Within dynamic
 146 semantic semantics, meaning derivation is considered a series of updates from an
 147 information state to another. The semantic contribution of modified numerals
 148 is split. They first introduce discourse referents (drefs), x and y . Restrictions
 149 like MOVIE(y), BOY(x), and SAW(x, y) are added onto these drefs. Eventually, it
 150 is after all these restrictions are applied that maximality and cardinality tests,
 151 $\mathbf{M}_u/\mathbf{M}_\nu/\mathbf{3}_u/\mathbf{5}_\nu$, as delayed evaluations, i.e., post-suppositional tests, come into
 152 force. \mathbf{M}_u and \mathbf{M}_ν check whether u and ν are assigned the mereologically maximal
 153 plural individuals x and y that satisfy all the restrictions, and $\mathbf{3}_u$ and $\mathbf{5}_\nu$
 154 check whether the cardinalities of maximal x and y are 3 and 5 respectively.



156 (Here $\mathbf{M}_\nu \stackrel{\text{def}}{=} \lambda m. \lambda g. \{ \langle \alpha, h \rangle \in m(g) \mid \neg \exists \langle \beta, h' \rangle \in m(g). h(\nu) \sqsubset h'(\nu) \}$.¹
 157 • is used to simplify the notation in bundling two tests together.)

158 2.2 Bumford (2017): Definite descriptions as post-suppositions

159 Not only modified numerals bring post-suppositions, Bumford (2017)'s analysis
 160 for Haddock (1987)'s example (see Fig. 3) shows that **definite descriptions**

¹ The type of \mathbf{M}_ν is $(g \rightarrow \{ \langle \alpha, g \rangle \}) \rightarrow (g \rightarrow \{ \langle \alpha, g \rangle \})$, with g meaning the type for assignment functions, and α standing for the type of the denotation corresponding to the constituent. The usual notation for types $\langle \alpha, \beta \rangle$ is written as $\alpha \rightarrow \beta$ here.

161 like *the rabbit in the hat* also involve post-suppositions, i.e., delayed tests that
 162 lead to **relativized definiteness** effects.

163 Under the scenario shown in Fig. 3, there are multiple rabbits (R1, R2, R3)
 164 and multiple hats (H1, H2). Thus, the uniqueness requirement of *the rabbit* or
 165 *the hat* cannot be met in an absolute sense. However, *the rabbit in the hat* is still
 166 perfectly felicitous in this context.

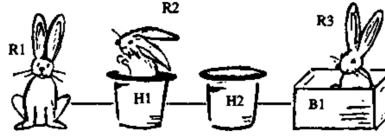


Fig. 3. The rabbit in the hat

167 Bumford (2017) argues that Haddock (1987)'s definite description is exactly
 168 parallel to the case of *exactly 3 boys saw exactly 5 movies*, where maximality
 169 tests are applied on drefs satisfying all these restrictions including MOVIE(y),
 170 BOY(x), and SAW(x, y), resulting in relativized maximization.

171 As shown in (10), under the given scenario in Fig. 3, for *the rabbit in the hat*,
 172 uniqueness tests $\mathbf{1}_\nu/\mathbf{1}_u$ are also applied in a delayed, non-local manner, after
 173 the introduction of all the drefs (i.e., x and y) and restrictions (i.e., HAT(y),
 174 RABBIT(x), and IN(x, y)). More specifically, the test $\mathbf{1}_\nu$ first checks whether there
 175 is a unique hat in the context such that only this hat contains any rabbits. Then
 176 the test $\mathbf{1}_u$ checks whether the rabbit contained in the above-mentioned unique
 177 rabbit-containing hat is unique.²

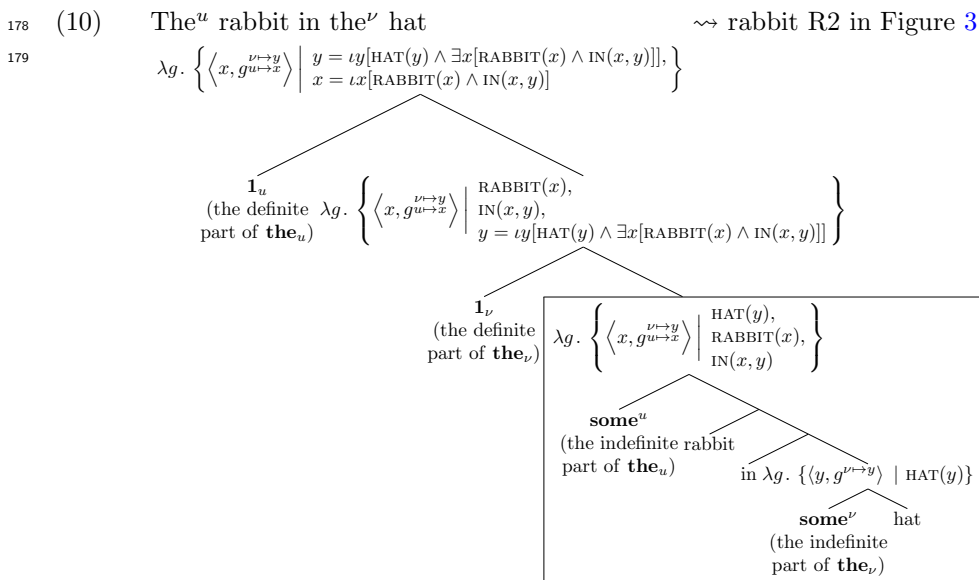
² An anonymous reviewer questions about how we can decide the order of different maximality tests and whether the order of maximality tests in the trees of (9) and (10) indicate scopal relations.

For the order of applying maximality tests in (9) and (10), I basically follow the original analysis of Brasoveanu (2013) and Bumford (2017).

For (9), according to Brasoveanu (2013), the maximality tests on the two plural individual drefs need to be applied **simultaneously**, as delayed tests (i.e., after the introduction of all relevant drefs and the application of relevant restrictions). The simultaneous application of the two maximality tests is intended for the non-scopal cumulative reading (see also Krifka 1999's discussion on this point).

For (10), I also follow Bumford (2017) in applying the two uniqueness tests one after the other. In my view, these two uniqueness tests can also be applied simultaneously in picking out the unique rabbit-hat pair.

The order of applying maximality tests does have an effect similar to QR-styled scope-taking, but via a distinct mechanism. A more detailed discussion is beyond the scope of the current paper (see Charlow 2017).



180 The upshot is that the semantic contribution of modified numerals and definite
 181 descriptions can be considered split, (i) introducing drefs at an earlier stage,
 182 and (ii) then at a later stage, imposing delayed, post-suppositional tests and
 183 leading to a relativized maximization/definiteness effect.

184 Moreover, modified numerals (e.g., *exactly 3 boys*) are distinct from definite
 185 descriptions (e.g., *the 3 boys*) in that the former can only be relatively definite,
 186 while the latter can be either absolutely or relatively definite.³

187 3 A post-suppositional view on *wh*-questions

188 A post-suppositional view on the interpretability of *wh*-questions can be devel-
 189 oped based on the following existing insights.

190 First, *wh*-expressions are parallel to indefinites (as well as other expres-
 191 sions like proper names, definite descriptions, modified numerals, etc.) in in-
 192 troducing drefs, as evidenced by their parallel behavior in supporting cross-
 193 sentential anaphora (see, e.g., Comorovski 1996). As illustrated in (11), the pro-
 194 noun *he* refers back to the dref introduced by *someone/Kevin/the boy/exactly*
 195 *one boy/who* in all these cases. For (11e), the pronoun *he* can also be considered
 196 referring back to the answer to the question *who came?* (see Li 2020).

- 197 (11) a. Someone⁰ came. I heard that he₀ coughed a few times.
 198 b. Kevin⁰ came. I heard that he₀ coughed a few times.
 199 c. The⁰ boy came. I heard that he₀ coughed a few times.
 200 d. Exactly one⁰ boy came. I heard that he₀ coughed a few times.
 201 e. Who⁰ came? I heard that he₀ coughed a few times.

³ I thank an anonymous reviewer for asking me to make this clear.

202 Second, according to Dayal (1996)’s Maximal Informativity Presupposition,
 203 a question presupposes the existence of a maximally informative true answer.
 204 This idea can be combined with the Hamblin-Karttunen semantics of questions
 205 to reason about the (non-)deterministic updates of propositions.

206 According to Hamblin (1973), a *wh*-question denotes a set of propositions,
 207 which are **possible propositional answers** to the question. Then according
 208 to Karttunen (1977), a *wh*-question denotes the set of its **true propositional**
 209 **answers**. As illustrated in (12), we can use an answerhood operator to bridge the
 210 set of possible answers and the maximally informative true answer. Essentially,
 211 this answerhood operator presupposes the existence of a maximally informative
 212 true answer p and picks out this p from Q , a set of propositions. What this
 213 answerhood operator does is reminiscent of the semantics of definite determiner
 214 *the*, which, when defined, contributes definiteness by picking out the unique (e.g.,
 215 *the dog*) or the mereologically maximal (e.g., *the dogs*) item (see (10)).

$$\begin{aligned}
 216 \quad (12) \quad \text{ANS}(Q)(w) &= \exists p[w \in p \in Q \wedge \forall q[w \in q \in Q \rightarrow p \subseteq q]]. \\
 217 \quad & \uparrow p[w \in p \in Q \wedge \forall q[w \in q \in Q \rightarrow p \subseteq q]] \quad \text{Dayal (1996)}
 \end{aligned}$$

218 With the above two ideas combined, an interpretable *wh*-question can be
 219 analyzed in the same dynamic semantics framework as modified numerals and
 220 definite descriptions are analyzed in Section 2.

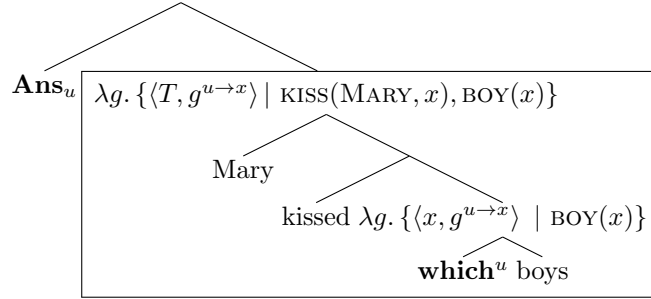
221 As illustrated in (13) (*wh*-movement and head movement are omitted in the
 222 tree), *who* works like *someone* or the indefinite component of *the* in introducing
 223 a dref in a non-deterministic way. After all relevant restrictions are added (here
 224 $\text{BOY}(x)$, $\text{KISS}(\text{MARY}, x)$), the silent operator, \mathbf{Ans}_u , plays the same role as a
 225 maximality operator, bringing a post-suppositional evaluation and checking in
 226 the output information state whether u is assigned the mereologically maximal
 227 plural individual x that satisfies $\text{BOY}(x)$ and $\text{KISS}(\text{MARY}, x)$. Thus the applica-
 228 tion of \mathbf{Ans}_u leads to a deterministic update. As far as a *wh*-question satisfies
 229 Dayal (1996)’s Maximal Informativity Presupposition and is thus interpretable,
 230 the derivation involving the application of \mathbf{Ans} should not fail.⁴⁵

⁴ In this short paper, I focus on the most basic data of *wh*-questions (e.g., *who did Mary kiss*) and degree questions (e.g., *how tall is Brienne*). I leave aside for future work cases like mention-some questions that can have multiple complete true answers (see (i)) or higher-order reading questions (see (ii) and Xiang 2021).

- (i) Where can I buy an Italian newspaper?
- (ii) Which books does John have to read?
The French novels or the Russian poems. The choice is up to him.

⁵ Here I actually implement Dayal (1996)’s Maximal Informativity Presupposition in a post-suppositional way. As pointed to me by Anna Szabolcsi (p.c.), a post-supposition that is not satisfied in its local domain gets imposed on the non-local domain like a traditional presupposition (see Brasoveanu and Szabolcsi 2012), so maybe we could say that all presuppositions start out as post-suppositions. Thus I believe a post-suppositional version of Dayal (1996)’s presupposition is compatible

231 (13) $\lambda g. \{\langle T, g^{u \rightarrow x} \rangle \mid x = \sigma x. [\text{KISS}(\text{MARY}, x) \wedge \text{BOY}(x)]\}$

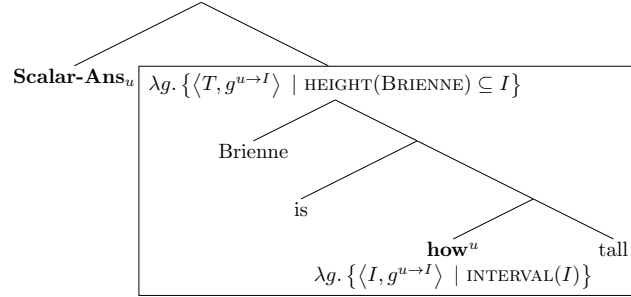


232 Here $\text{Ans}_u \stackrel{\text{def}}{=} \lambda m. \lambda g. \{\langle \alpha, h \rangle \in m(g) \mid \neg \exists \langle \beta, h' \rangle \in m(g). h(u) \sqsubset h'(u)\}$

233 A similar analysis can be developed for degree questions, with an answerhood
 234 operator, **Scalar- Ans_u** , which is adjusted for a set of drefs that are scalar values.

235 (14) $\llbracket \text{tall} \rrbracket_{\langle dt, et \rangle} \stackrel{\text{def}}{=} \lambda I_{\langle dt \rangle} \lambda x. \text{HEIGHT}(x) \subseteq I$ (Zhang and Ling 2021)

236 (15) $\lambda g. \{\langle T, g^{u \rightarrow I} \rangle \mid I = \text{the contextually most informative } I \text{ s.t. } \text{HEIGHT}(\text{BRIENNE}) \subseteq I\}$



237 Here $\text{Scalar-Ans}_u \stackrel{\text{def}}{=} \lambda m. \lambda g. \{\langle \alpha, h \rangle \in m(g) \mid \neg \exists \langle \beta, h' \rangle \in m(g). h(u) \subset h'(u)\}$

238 I adopt the notion of intervals to represent scalar values (see also [Schwarzschild](#)
 239 [and Wilkinson 2002](#), [Abrusán 2014](#), [Zhang and Ling 2021](#), a.o.). An interval is
 240 a convex set of degrees, e.g., $\{d \mid 5'5'' < d \leq 7'1''\}$, which can also be written as
 241 $[5'5'', 7'1'']$. As illustrated in (14), a gradable adjective like *tall* relates an interval
 242 I and an atomic individual x , such that the height measurement of x falls within
 243 the interval I along a scale of height. For example, the meaning of *Brienne is*
 244 *between 5'10'' and 6' tall* is analyzed as $\text{HEIGHT}(\text{BRIENNE}) \subseteq [5'10'', 6']$.

245 As illustrated in (15), I propose that during base generation, *how^u* non-
 246 deterministically introduces an interval dref, I .⁶ After relevant restrictions are
 247 added (here $\text{HEIGHT}(\text{BRIENNE}) \subseteq I$), the application of **Scalar- Ans_u** picks

with this general picture of presuppositions and worth having a try. A thorough investigation of this post-suppositional perspective on *wh*-questions and whether my current analysis is strictly contingent on this post-suppositional perspective is left for future work.

⁶ (i) shows that *how* is parallel with other *wh*-expressions in introducing drefs and supporting cross-sentential anaphora. In (ia), $\mathcal{G}' \mathcal{G}'$ is similar to definite descriptions or proper names (e.g., *Kevin* in (11b)) in introducing a definite scalar value so that

248 out the most informative interval from a set of possible intervals, leading to a
 249 deterministic update. Under an ideal context, where measurements don't involve
 250 any errors, this most informative interval would be a singleton set of degrees (i.e.,
 251 the narrowest interval that entails all intervals satisfying relevant restrictions),
 252 containing the precise height measurement of Brienne (e.g., [6'3'', 6'3'']).

253 This post-suppositional view on the interpretability of *wh*-questions is also
 254 compatible with insights on (i) the cross-linguistic parallelism between *wh*-questions
 255 and *wh*-free relatives (Caponigro 2003, 2004, Chierchia and Caponigro 2013), and
 256 (ii) the categorial approach to *wh*-questions (see Hausser and Zaefferer 1979).

257 As illustrated in (16), *wh*-free relatives can be replaced by truth-conditionally
 258 equivalent DPs, and in most cases (except for the complement position of ex-
 259 istential predicates in some languages, see Caponigro 2004), both *wh*-free rela-
 260 tives and their corresponding DPs exhibit maximality/definiteness.⁷ Under the
 261 current post-suppositional analysis, the semantics of the free relative in (16a),
 262 [[what Adam cooked]], can be derived by applying the silent maximality opera-
 263 tor **Ans_u** to the meaning of the question *what did Adam cook?*, which yields the
 264 maximal sum of things, $\sigma x.[\text{COOK}(\text{ADAM}, x)]$, i.e., the meaning of the DP *the*
 265 *things Adam cooked* (see also Chierchia and Caponigro 2013 for a similar idea).⁸

- 266 (16) a. Jie tasted what^u Adam cooked. (example from Caponigro 2004)
 267 b. Jie tasted [_{DP} the^u things Adam cooked].

268 Within the categorial approach to *wh*-questions (Hausser and Zaefferer 1979),
 269 a *wh*-question denotes a function, which takes its short answer as argument to
 270 generate a (maximally informative) true proposition, as illustrated in (17).

- 271 (17) Categorial approach: [[who did Mary kiss]] = λx . Mary kissed x
 272 a. Short answer: Kate and Kevin.
 273 b. Propositional answer: Mary kissed Kate and Kevin.

that in the subsequent sentence refers back to it. Obviously, the parallelism between
 (ia) and (ib) is similar to that shown in (11).

- (i) a. Brienne is 6'3''⁰ tall. It seems that Jaime is a bit shorter than that₀.
 b. How⁰ tall is Brienne? It seems that Jaime is a bit shorter than that₀.

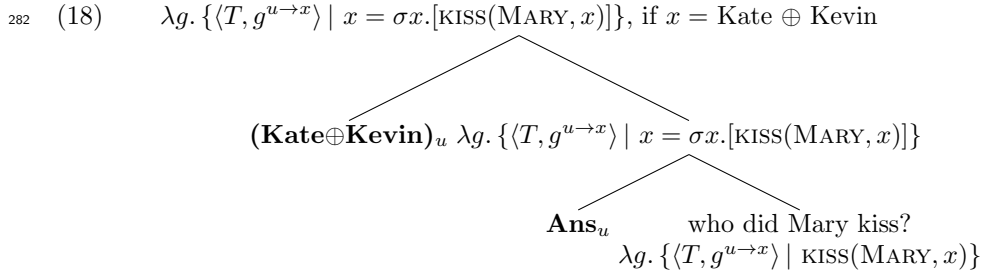
⁷ *Wh*-free choices corresponding to mention-some *wh*-questions are also exceptions
 (see Chierchia and Caponigro 2013) and don't seem to exhibit maximality:

- (i) Mary looked for who can help her.
 = Mary looked for someone that can help her.
 ≠ Mary looked for all the people that can help her.

⁸ In addition to *wh*-free relatives, concealed questions also demonstrate the parallelism
 between definite DPs and *wh*-questions (see e.g., Nathan 2006):

- (i) a. Jaime knows how tall Brienne is.
 b. Jaime knows the height of Brienne.

274 Under the current post-suppositional analysis, as illustrated in (18), this func-
 275 tion $\lambda x.Mary\ kissed\ x$ is considered a restriction on the dref introduced by the
 276 *wh*-expression, x . Then the short answer, here *Kate and Kevin*, can be considered
 277 similar to the cardinality tests in the case of the cumulative-reading sentence *ex-*
 278 *actly 3 boys saw exactly 5 movies*. The test $(\mathbf{kate} \oplus \mathbf{Kevin})_u$ is attached to the
 279 application of the maximality test \mathbf{Ans}_u , checking whether $\sigma x.KISS(MARY, x)$ is
 280 equivalent to the sum ‘Kate \oplus Kevin’. This amounts to turning a short answer
 281 into a corresponding propositional answer to a *wh*-question.



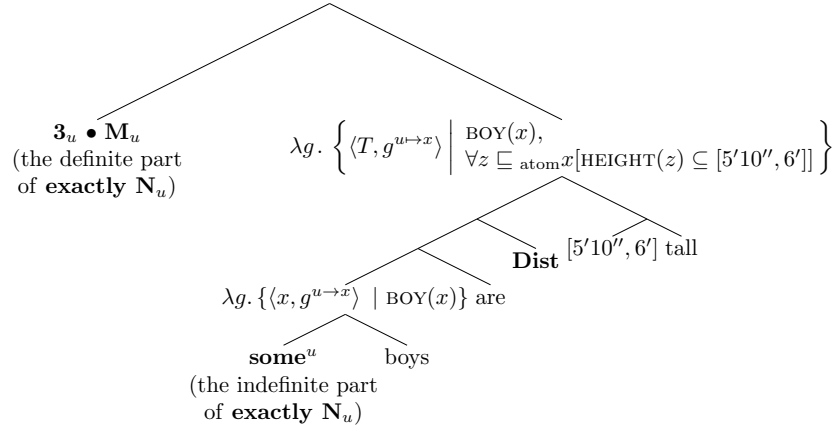
283 Essentially, based on Dayal (1996)’s Maximal Informativity Presupposition,
 284 I propose that for an interpretable *wh*-question, (i) its *wh*-expression introduces
 285 a dref non-deterministically, and (ii) a delayed, post-supposition-like maximality
 286 operator can bring definiteness to this dref, leading to a deterministic update.

287 4 Accounting for uninterpretable questions

288 4.1 Interpreting a modified numeral in a matrix degree question

289 The interpretation of a declarative degree sentence containing a modified nu-
 290 numeral (see (2a), repeated here as (19)) is straightforward.

291 (19) Exactly three^u boys are between 5’10’’ and 6’ tall.⁹ (= (2a))
 292



⁹ Given that $\llbracket \text{tall} \rrbracket$ relates an interval and an atomic individual (see (14)), I assume a distributivity operator $\mathbf{Dist} \stackrel{\text{def}}{=} \lambda x. \lambda P_{\langle et \rangle}. \forall z \sqsubseteq_{\text{atom}} x [P(z)]$ here.

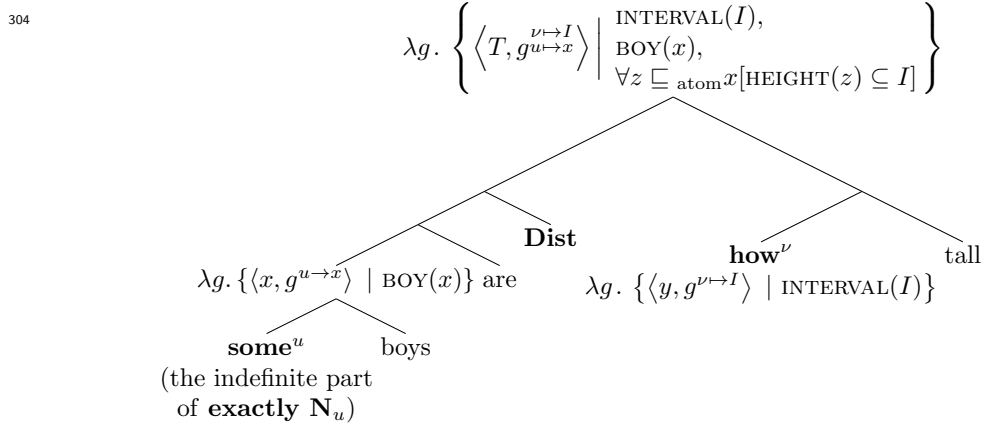
293 In this sentence, only *exactly three* brings post-suppositional tests. As shown
 294 in (19), as post-suppositional tests, \mathbf{M}_u picks out the largest boy-sum x such
 295 that for each atomic boy within x , his height falls within the interval $[5'10'', 6']$,
 296 and $\mathbf{3}_u$ checks whether the cardinality of this boy-sum x is equal to 3.

297 Then I turn to the core data under discussion, a degree question containing
 298 a modified numeral (repeated in (20)):

299 (20) #How $^\nu$ tall are exactly three u boys? (= (2b))

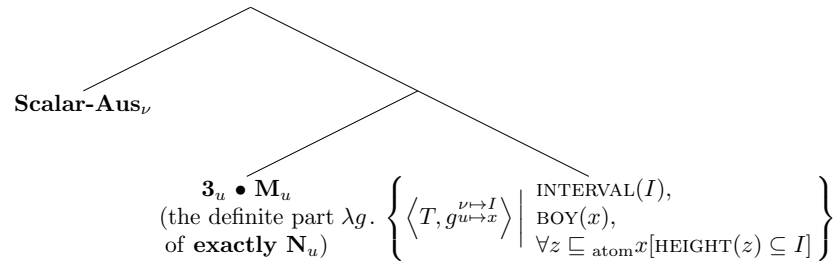
300 According to the post-supposition-based analysis addressed in Sections 2 and
 301 3, in sentence (20), both *wh*-expression *how* and modified numeral *exactly three*
 302 (*boys*) first introduce a dref, as show in (21):

303 (21) Before post-suppositional tests are applied:

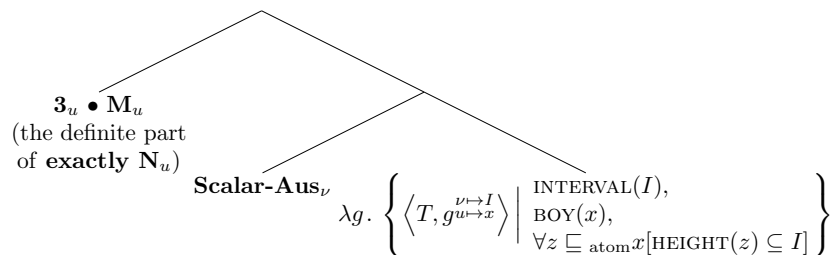


305 Once all the drefs are introduced and relevant restrictions are added, there are
 306 two potential derivation orders: either (i) as shown in (22), the maximality and
 307 cardinality tests of *exactly 3* are applied first, letting the deterministic update
 308 from **Scalar-Aus $_\nu$** take place later, or (ii) as shown in (23), the deterministic
 309 update from **Scalar-Aus $_\nu$** happens first, letting the maximality and cardinality
 310 tests of *exactly 3* be checked later.

311 (22)



312 (23)



313 Suppose we adopt the possibility of (22), then \mathbf{M}_u would select out the
 314 absolute largest boy-sum in the given context, and $\mathbf{3}_u$ would check whether the
 315 cardinality of this absolute largest boy-sum is 3. If the tests \mathbf{M}_u and $\mathbf{3}_u$ don't
 316 fail, the application of **Scalar-Aus $_{\nu}$** would eventually yield the most informative
 317 height interval such that (i) its lower bound is equivalent to the precise height
 318 of the shortest boy in the context, and (ii) its upper bound is equivalent to the
 319 precise height of the tallest boy in the context.

320 However, given that such a question amounts to requesting the height infor-
 321 mation of the absolute largest boy-sum in the given context, speakers would use
 322 the question *how tall are the (three) boys* instead. In other words, *exactly three*
 323 *boys*, which necessarily involves relative definiteness, would be ruled out in the
 324 competition with the definite description *the (three) boys*, which supports the
 325 meaning of absolute definiteness.¹⁰

326 On the other hand, suppose we adopt the possibility of (23), then **Scalar-**
 327 **Aus $_{\nu}$** would select out the absolute most informative height interval such that it
 328 includes the height of some boy(s). As far as boys are considered not of the same
 329 height, there cannot be a unique most informative height interval (e.g., suppose
 330 the heights of two boys are [5'10'', 5'10''] and [6', 6'], respectively. Then there is
 331 no unique interval I such that I entails, i.e., is a subset of, both [5'10'', 5'10''] and
 332 [6', 6']). Thus **Scalar-Aus $_{\nu}$** would not fail only if all the boys are considered of
 333 the same height, and when **Scalar-Aus $_{\nu}$** does not fail, \mathbf{M}_u would also select out
 334 the absolute largest boy-sum in the given context. Obviously, such a question still
 335 amounts to requesting the height information of the absolute largest boy-sum in
 336 the given context, and *exactly three boys* would be ruled out in the competition
 337 with *the (three) boys*.

338 Overall, the interpretation of (20) would be problematic because both \mathbf{M}_u
 339 and **Scalar-Aus $_{\nu}$** need to be checked to result in relative definiteness, i.e., both
 340 wait to be applied as the last post-suppositional test in the derivation. In other
 341 words, without resolving the update of u , **Scalar-Aus $_{\nu}$** cannot work to yield
 342 the most informative height interval for u , but without resolving the update
 343 of ν , \mathbf{M}_u cannot work to pick out the relatively maximal boy-sum. Obviously,
 344 the requirements of \mathbf{M}_u and **Scalar-Aus $_{\nu}$** cannot be both satisfied, and the
 345 unacceptability of the whole sentence thus arises.

¹⁰ An anonymous reviewer asks whether this competition view would weaken the analysis, as it implies that the relative definiteness of *how* and modified numerals in *#How tall are exactly three boys* CAN be satisfied. In Section 4.2, I show that sometimes these post-suppositions that impose relative definiteness indeed can all be satisfied.

346 **4.2 Interpreting a modified numeral in an embedded degree**
 347 **question**

348 As illustrated by (24), in comparative sentences, their *than*-clause can be con-
 349 sidered parallel to a degree question (see Fleisher 2020, Zhang 2020).

- 350 (24) Brienne is taller than Jaime is tall.
 351 \llbracket than Jaime is $\rrbracket \rightsquigarrow$ addressing a degree question: *how tall is Jaime?*

352 According to Zhang and Ling (2021), a comparative sentence basically means
 353 that the scalar value associated with the subject minus the scalar value asso-
 354 ciated with the comparative standard results in a positive difference (i.e., an
 355 increase). As shown in (25), comparative morpheme *-er* is considered denot-
 356 ing a default positive difference, i.e., an increase. The *than*-clause, i.e., *than*
 357 *Jaime is tall* in (24), denotes the short answer to the degree question *how tall is*
 358 *Jaime* and amounts to the most informative interval I' satisfying the restriction
 359 $\text{HEIGHT}(\text{JAIME}) \subseteq I'$, written as $\iota I'[\text{HEIGHT}(\text{JAIME}) \subseteq I']$ here. Eventually, as
 360 shown in (25d), this short answer to the degree question *how tall Jaime is* plays
 361 the role of comparative standard in the derivation of sentential meaning.

- 362 (25) a. $\llbracket \text{tall} \rrbracket_{\langle dt, et \rangle} \stackrel{\text{def}}{=} \lambda I_{\langle dt \rangle} \lambda x. \text{HEIGHT}(x) \subseteq I$ (= (14))
 363 b. $\llbracket \text{-er} \rrbracket \stackrel{\text{def}}{=} (0, +\infty) \rightsquigarrow$ a default positive difference
 364 i.e., the most general positive interval that represents an increase
 365 (With a presupposition of additivity: there is a contextually salient
 366 scalar value serving as the base of the increase)
 367 c. Assuming a silent operator that performs comparison:
 368 $\mathbf{Minus} \stackrel{\text{def}}{=} \lambda I_{\text{STANDARD}} \lambda I_{\text{DIFFERENCE}}. \iota I [I - I_{\text{STANDARD}} = I_{\text{DIFFERENCE}}]$
 369 d. $\llbracket (24) \rrbracket \Leftrightarrow \text{HEIGHT}(\text{BRIENNE}) \subseteq \iota I [I - I_{\text{STANDARD}} = I_{\text{DIFFERENCE}}]$
 370 $\Leftrightarrow \text{HEIGHT}(\text{BRIENNE}) \subseteq$
 371 $\iota I [I - \iota I' [\text{HEIGHT}(\text{JAIME}) \subseteq I'] = (0, +\infty)]$

372 Intriguingly, although the matrix degree question *#how tall are exactly three*
 373 *boys* (see (2b)/(20)) is uninterpretable, comparative sentence (26), which con-
 374 tains a *than*-clause corresponding to the problematic degree question, is good.

- 375 (26) Mary is taller than ^{ν} exactly three ^{u} boys are tall.

376 I have proposed an analysis for (26) in Zhang (2020). As mentioned in Section
 377 4.1, for the matrix degree question *#how ^{ν} tall are exactly three ^{u} boys*, **Scalar-**
 378 **Aus _{ν}** and **M _{u}** , both tests that bring relative definiteness, require to be applied
 379 as the last test, and both requirements cannot be satisfied at the same time.

380 For (26), however, information outside the *than*-clause contributes to resolve
 381 the deterministic update of ν independent of the update of u .

382 As mentioned above (see (25c)), the semantics of a comparative addresses the
 383 relation among three definite scalar values: (i) the scalar value associated with
 384 the subject, which serves as the **minuend**; (ii) the scalar value associated with
 385 the *than*-clause, which serves as the **subtrahend**; and (iii) the difference between
 386 the minuend and the subtrahend. Given the subtraction relation between these

387 three definite values (see (25c)), we can use two of the three values to reason
 388 about the third one.

389 Thus, for (26), given the minuend (i.e., HEIGHT(MARY)) and the difference
 390 (i.e., $(0, +\infty)$), the deterministic update of ν (i.e., the value of the subtrahend)
 391 can be settled first: it is the largest interval below HEIGHT(MARY), which can be
 392 written as $(-\infty, \text{the precise height measurement of Mary})$.¹¹ This update of ν
 393 satisfies relative definiteness in the sense that it is checked at the sentence-level,
 394 beyond the *than*-clause itself, as a delayed test after more restrictions are added
 395 (i.e., μ is assigned to an interval *dref* I satisfying ‘ I is below HEIGHT(MARY)’).

396 Then similar to the case of (19), \mathbf{M}_μ is applied to pick out the largest boy-sum
 397 x such that $\forall z \sqsubseteq_{\text{atom}} x [\text{HEIGHT}(z) \subseteq (-\infty, \text{the precise height measurement of Mary})]$,
 398 and $\mathbf{3}_\nu$ is applied to check whether the cardinality of x is 3. Therefore, through
 399 the derivation of the meaning of (26), the relative maximality of *exactly three*
 400 *boys* is achieved.

401 It is worth noting that for this x , the interval $(-\infty, \text{the precise height of Mary})$
 402 can still be the most informative short answer to the degree question *how tall is*
 403 x (i.e., with **Scalar-Aux** $_\nu$ applied to *how tall is* x). Imagine an extreme case:
 404 one of the boys in x is just slightly shorter than Mary is, and another one of the
 405 boys in x is extremely short. Then the application of **Scalar-Aux** $_\nu$ would lead to
 406 exactly this interval $(-\infty, \text{the precise height of Mary})$. In other words, the above
 407 analysis of (26) is not incompatible with the view that the *than*-clause addresses
 408 the short answer to a corresponding degree question. It’s just that in this case,
 409 the information of this short answer (i.e., $(-\infty, \text{the precise height of Mary})$) is
 410 derived first, and then this definite interval is made use of in checking the post-
 411 suppositional requirements of the modified numeral here (i.e., *exactly three boys*).

412 5 Discussion

413 In Section 4, I have shown that the uninterpretability of the pattern ‘modified
 414 numeral + degree question’ is essentially due to a conflict between different
 415 items that bring post-suppositions (i.e., both need to be applied as the last test
 416 to result in relative definiteness) and how this conflict can be circumvented (i.e.,
 417 additional information is available to resolve the definiteness of one of the items
 418 and thus remove the conflict). Here I compare the current proposal with three
 419 existing lines of research on intervention effects or weak island effects.

420 5.1 Intervention effects: Beck (2006) and Li and Law (2016)

421 Both Beck (2006) and Li and Law (2016) address intervention effects related to
 422 focus, but their empirical coverages are different. As shown in (27) and (28),
 423 their analyses target different problematic configurations.

¹¹ In our actual world, the height of a person cannot be a negative value. This should be considered a physical constraint in our world knowledge, not a linguistic constraint. Linguistically, we can imagine characters with a negative height in fantasy works.

- 424 (27) The problematic configuration analyzed by Beck (2006):
 425 ?* [Q ...[focus-sensitive operator [Y_P ...WH...]]]
- 426 (28) The problematic configuration analyzed by Li and Law (2016):
 427 ?* [...focus-sensitive operator [focus alternatives...ordinary alternatives...]]
 428 (or ?* [...focus-sensitive operator [XP_F ...WH...]])

429 Beck (2006) is based on Rooth (1985)'s focus semantics. A *wh*-expression has
 430 its focus semantic value (i.e., a set of alternatives), but lacks an ordinary semantic
 431 value. A Q operator is needed to turn the focus semantic value of a *wh*-expression
 432 into an ordinary semantic value. However, in the problematic configuration in
 433 (27), (i) a focus-sensitive operator blocks the association between the Q operator
 434 and the *wh*-expression, and moreover, (ii) the focus-sensitive operator needs to
 435 be applied on an item that has both a focus semantic value and an ordinary
 436 value, which the *wh*-expression lacks. Thus the derivation crashes.

437 According to Li and Law (2016), given that both XP_F and WH introduce
 438 alternatives, embedding WH within the scope of XP_F makes [[XP_F ...WH...]] a
 439 set of sets of alternatives, which becomes an illicit input for the focus-sensitive
 440 operator, resulting in a derivation crash.

441 Both Beck (2006) and Li and Law (2016) explain the uninterpretability of
 442 intervention patterns as derivation crash. Different from these approaches, the
 443 current account for the uninterpretability of the pattern ‘modified numeral +
 444 degree question’ is based on a potential failure of achieving relative definiteness.

445 As shown in Section 4, for the pattern ‘modified numeral + degree ques-
 446 tion’, the potential failure of achieving relative definiteness exists for matrix
 447 degree questions, but not for embedded degree questions (i.e., *than*-clauses of
 448 comparatives). Thus empirically, the current account works better than existing
 449 approaches that explain uninterpretability as derivation crash.

450 It is worth investigating whether/how the current approach can be further
 451 extended to cover the data of intervention effects. As shown in (29), the matrix
 452 *wh*-question (29a) is problematic. Indeed, it has a problematic configuration in
 453 both the theories of Beck (2006) and Li and Law (2016). However, once this
 454 configuration is embedded in a *wh*-conditional, as shown in (29b), there is no
 455 longer uninterpretability. The acceptability contrast between (29a) and (29b)
 456 suggests that the problem of (29a) might not be due to a derivation crash.

- 457 (29) a. * zhīyǒu Mary_F dú-le shénme shū?
 only Mary read-PFV what book
 458 Intended: ‘What book(s) did only Mary_F read?’ Chinese
- 459 b. Context: Only Mary is interested in the books I read and follows
 460 me to read them.
- 461 wǒ dú shénme shū, zhīyǒu Mary_F (yě) gen-zhe wǒ dú
 I read what book only Mary (also) follow I read
 462 shénme shū
 what books
 463 ‘Only Mary follows me to read whatever books I read.’ Chinese

464 Actually, the case of (29b) seems similar to embedded degree questions with a
 465 modified numeral (see (26) in Section 4.2). For (29b), suppose both the *wh*-item
 466 (i.e., *shénme*) and the focused part (i.e., *zhǐyǒu Mary* ‘only Mary’) introduce
 467 drefs first and bring post-suppositional tests later. Then within a *wh*-conditional,
 468 the deterministic update of the *wh*-expression can be resolved independent of the
 469 focused part, helping to circumvent the issue of which post-suppositional test
 470 needs to be applied the last. I leave the details of this analysis for future work.

471 5.2 Abrusán (2014)’s analysis of weak island effects

472 As mentioned in Section 1, the uninterpretable pattern addressed in this paper,
 473 i.e., ‘modified numeral + degree question’, is also reminiscent of weak island
 474 effects. However, the difference between (30) and (31) shows that the uninter-
 475 pretable pattern under discussion (see (31a)) is still somewhat distinct from
 476 typical weak island effects (see (30a)).

477 In particular, weak island effects are observed for both matrix and embed-
 478 ded degree questions (see the parallelism between (30a) and (30b)), while the
 479 major pattern addressed in this paper only leads to uninterpretable matrix de-
 480 gree questions, but not to uninterpretable embedded degree questions (see the
 481 contrast between (31a) and (31b) and the discussion in Section 4.2).

482 The contrast between embedded degree questions in (30b) and (31b) is likely
 483 due to a further requirement of degree questions: the request of height informa-
 484 tion brings an existential presupposition for items undergoing height measure-
 485 ment – here only *exactly 3 boys*, but not *few boys*, guarantees that this existential
 486 presupposition be satisfied (see also Zhang 2020 for more discussion).

487 On the other hand, as illustrated in (30)-(31), it seems that DE quantifiers
 488 and modified numerals do not lead to uninterpretability in *wh*-questions that
 489 are not degree questions (see (30c) and (31c)).

490 Presumably, the contrast between (31a) and (31c) is parallel with the contrast
 491 between (30a) and (30c) and thus can be explained by an extension of accounts
 492 that aim to account for weak island effects. For the contrast between (31a) and
 493 (31c), a detailed analysis along this line is left for future work.¹²

- | | | | |
|-----|------|--|--|
| 494 | (30) | DE quantifiers in <i>wh</i> -questions | (Weak island effects: (30a) and (30b)) |
| 495 | | a. #How tall are few boys? | Matrix degree question |
| 496 | | b. #Mary is taller than few boys are. | Embedded degree question |
| 497 | | c. Which books did few boys read? | <i>which</i> -question (cf. (30a)) |
| 498 | (31) | Modified numeral in <i>wh</i> -questions | |
| 499 | | a. #How tall are exactly 3 boys? | Matrix degree question |
| 500 | | b. Mary is taller than exactly 3 boys are. | Embedded degree question |
| 501 | | c. Which books did exactly 3 boys read? | <i>which</i> -question (cf. (31a)) |

¹² I thank an anonymous reviewer for bringing up this issue, i.e., the contrast between (31a) and (31c).

502 Among existing studies on weak island effects, Abrusán (2014)’s account is
 503 also based on the idea that an interpretable *wh*-question needs to meet Dayal
 504 (1996)’s Maximal Informativity Presupposition. As illustrated in (4a) (repeated
 505 here in (32)), since there does not exist a maximally informative interval I such
 506 that $\neg\text{HEIGHT}(\text{JOHN}) \subseteq I$, (32) does not meet the presuppositional requirement,
 507 leading to uninterpretability.

508 (32) #How tall isn’t John? (= (4a))

509 The current analysis is essentially in the same spirit as Abrusán (2014).
 510 Although Abrusán (2014) focuses on weak island effects, she raises the issue of
 511 how intervention effects and weak island effects can be connected. As addressed
 512 in Section 5.1, the current analysis has the potential of explaining intervention
 513 effects as well. It is also worth investigating whether the current analysis can
 514 eventually be extended to bridge between the phenomena of intervention effects
 515 and those of weak island effects.

516 6 Conclusion

517 In this paper, I have adopted a dynamic semantics perspective to explain why a
 518 degree question like #*how tall are exactly three boys?* is unacceptable. The ac-
 519 count crucially relies on the ideas that (i) both *wh*-items (e.g., *how*) and modified
 520 numerals (e.g., *exactly three boys*) introduce drefs and bring post-suppositional
 521 tests that result in relative definiteness, and (ii) when different post-suppositional
 522 tests are present, and their relative definiteness cannot be all achieved, uninter-
 523 pretability arises.

524 Presumably, the current account will bring new insights on more empirical
 525 phenomena, in particular, intervention effects and weak island effects. How the
 526 current account will influence our understanding on the scope-taking issue within
 527 a *wh*-question is also left for future research.

528 References

- 529 Abrusán, M.: Weak island effects. OUP (2014) <https://doi.org/10.1093/acprof:oso/9780199639380.001.0001>
- 530 Beck, S.: Wh-constructions and transparent logical form. Ph.D. thesis, Uni-
 531 versität Tübingen (1996) <http://hdl.handle.net/11858/00-001M-0000-0012-900B-9>
- 532 Beck, S.: Intervention effects follow from focus interpretation. *Nat. Lang. Semant.* **14**, 1–56 (2006) <https://doi.org/10.1007/s11050-005-4532-y>
- 533 Brasoveanu, A.: Modified numerals as post-suppositions. *J. Semant.* **30**, 155–209
 534 (2013) <https://doi.org/10.1093/jos/ffs003>
- 535 Brasoveanu, A., Szabolcsi, A.: Presuppositional *too*, postsuppositional
 536 *too*. In: Aloni, M., Franke, F., and Roelofsen, F. (eds) *The dy-*
 537 *dynamic, inquisitive, and visionary life of ϕ , $?\phi$, and $\diamond\phi$: A festschrift*

- 541 for Jeroen Groenendijk, Martin Stokhof, and Frank Veltman, 55–64.
 542 <https://festschriften.illc.uva.nl/Festschrift-JMF/>.
- 543 Bumford, D.: Split-scope definites: Relative superlatives and Haddock descrip-
 544 tions. *Linguist. Philos.* **40**, 549–593 (2017) [https://doi.org/10.1007/s10988-](https://doi.org/10.1007/s10988-017-9210-2)
 545 [017-9210-2](https://doi.org/10.1007/s10988-017-9210-2)
- 546 Caponigro, I.: Free not to ask: On the semantics of free rela-
 547 tives and *wh*-words cross-linguistically. Ph.D. thesis, UCLA (2003)
 548 [https://idiom.ucsd.edu/~](https://idiom.ucsd.edu/~ivano/Papers/2003_dissertation_revised_2019-4-10.pdf)
 549 [ivano/Papers/2003_dissertation_revised_2019-4-](https://idiom.ucsd.edu/~ivano/Papers/2003_dissertation_revised_2019-4-10.pdf)
 550 [10.pdf](https://idiom.ucsd.edu/~ivano/Papers/2003_dissertation_revised_2019-4-10.pdf)
- 550 Caponigro, I.: The semantic contribution of *wh*-words and type shifts: Evidence
 551 from free relatives crosslinguistically. In: Young, R. B. (eds) *Proc. SALT* **14**,
 552 38–55 (2004) <https://doi.org/10.3765/salt.v14i0.2906>
- 553 Charlow, S.: Post-suppositions and semantic theory. *J. Semant.* In press (2017)
 554 <https://ling.auf.net/lingbuzz/003243>
- 555 Chierchia, G., Caponigro, I.: Questions on questions and
 556 free relatives. *Handout of Sinn und Bedeutung* **18** (2013)
 557 [https://scholar.harvard.edu/chierchia/publications/demo-presentation-](https://scholar.harvard.edu/chierchia/publications/demo-presentation-handout)
 558 [handout](https://scholar.harvard.edu/chierchia/publications/demo-presentation-handout)
- 559 Comorovski, I.: Interrogative phrases and the syntax-semantics interface. Kluwer
 560 (1996) <https://doi.org/10.1007/978-94-015-8688-7>
- 561 Dayal, V.: Locality in Wh Quantification. Kluwer. (1996)
 562 <https://doi.org/10.1007/978-94-011-4808-5>
- 563 Fleisher, N.: Nominal quantifiers in *than* clauses and degree questions. *Syntax*
 564 *Semant.* **42**, 364–381 (2020) <https://doi.org/10.1163/9789004431515>
- 565 Fox, D., Hackl, M.: The universal density of measurement. *Linguist. Philos.*
 566 **29**(5), 537–586 (2007) <https://doi.org/10.1007/s10988-006-9004-4>
- 567 Haddock, N.: Incremental interpretation and combinatory categorial
 568 grammar. *The 10th international joint conference on artificial in-*
 569 *telligence* **2**, 661–663 (1987) Morgan Kaufmann Publishers Inc.
 570 <https://www.ijcai.org/Proceedings/87-2/Papers/012.pdf>
- 571 Hamblin, C.: Questions in Montague grammar. *Foundations of Language* **10**,
 572 41–53 (1973) <http://www.jstor.org/stable/25000703>
- 573 Hausser, R., Zaefferer, D.: Questions and answers in a context-dependent Mon-
 574 tague grammar. In *Formal semantics and pragmatics for natural languages*,
 575 339–358. Springer (1979) https://doi.org/10.1007/978-94-009-9775-2_12
- 576 Honcoop, M.: Towards a dynamic semantics account of weak islands.
 577 In: Galloway, T., Spence, J. (eds) *Proc. SALT* **6**, 93–110 (1996)
 578 <http://dx.doi.org/10.3765/salt.v6i0.2773>
- 579 Karttunen, L.: Syntax and semantics of questions. *Linguist. Philos.* **1**, 3–44
 580 (1977) <https://www.jstor.org/stable/pdf/25000027.pdf>
- 581 Krifka, M.: At least some determiners aren't determiners. In:
 582 Tuner, K. (eds) *The semantics/pragmatics interface from*
 583 *different points of view*, vol. 1, 257–291. Elsevier (1999)
 584 <https://semantics.uchicago.edu/kennedy/classes/w14/implicature/readings/krifka99.pdf>
- 585 Li, H., Law, J. H.-K.: Alternatives in different dimensions: A case
 586 study of focus intervention. *Linguist. Philos.* **39**, 201–245 (2016)
 587 <http://dx.doi.org/10.1007/s10988-016-9189-0>

- 588 Li, H.: A dynamic semantics for *wh*-questions. Ph.D. thesis, NYU (2020)
589 [https://www.researchgate.net/publication/348920343_A_dynamic_semantics_for_wh-](https://www.researchgate.net/publication/348920343_A_dynamic_semantics_for_wh-questions)
590 [questions](https://www.researchgate.net/publication/348920343_A_dynamic_semantics_for_wh-questions)
- 591 Nathan, L. E.: On the interpretation of concealed questions. Ph.D. thesis, MIT
592 (2006) <https://dspace.mit.edu/handle/1721.1/37423>
- 593 Rooth, M.: Association with focus. Ph.D. thesis, UMass Amherst (1985)
594 [https://ecommons.cornell.edu/bitstream/handle/1813/28568/Rooth-1985-](https://ecommons.cornell.edu/bitstream/handle/1813/28568/Rooth-1985-PhD.pdf)
595 [PhD.pdf](https://ecommons.cornell.edu/bitstream/handle/1813/28568/Rooth-1985-PhD.pdf)
- 596 Rullmann, H.: Maximality in the semantics of *wh*-constructions.
597 Ph.D. thesis, University of Massachusetts-Amherst (1995)
598 <https://scholarworks.umass.edu/dissertations/AAI9524743/>
- 599 Schwarzschild, R., Wilkinson, K.: Quantifiers in Comparatives: A Seman-
600 tics of Degree Based on Intervals. *Nat. Lang. Semant.* **10**, 1–41 (2002)
601 <https://doi.org/10.1023/A:1015545424775>
- 602 de Swart, H.: Indefinites between predication and reference. *Proc. SALT* **9**, 273–
603 297 (2006) <http://dx.doi.org/10.3765/salt.v9i0.2823>
- 604 Szabolcsi, A., Zwarts, F.: Weak islands and an algebraic seman-
605 tics for scope taking. *Nat. Lang. Semant.* **1**(3), 235–284 (1993)
606 <http://www.jstor.org/stable/23748421>
- 607 Szabolcsi, A.: Strategies for scope taking. In: Szabolcsi, A. (eds) *Ways of scope*
608 *taking*, 109–154. Springer (1997) https://doi.org/10.1007/978-94-011-5814-5_4
- 609 Szabolcsi, A.: Strong vs. weak island. *The Blackwell Companion to Syntax*. Vol.
610 **4**, 479–531. Blackwell (2006) <https://doi.org/10.1002/9780470996591.ch64>
- 611 Umbach, C.: Why do modified numerals resist a referential interpretation. *Proc.*
612 *SALT* **15**, 258–275 (2006) <http://dx.doi.org/10.3765/salt.v15i0.2931>
- 613 Xiang, Y.: Higher-order readings of *wh*-questions. *Nat. Lang. Semant.* **29**, 1–45
614 (2021) <https://doi.org/10.1007/s11050-020-09166-8>
- 615 Zhang, L.: Modified numerals revisited: The cases of *fewer than 4* and
616 *between 4 and 8*. *Proc. Sinn und Bedeutung* **21**(2), 1371–1388 (2018)
617 <https://doi.org/10.18148/sub/2018.v21i2.204>
- 618 Zhang, L.: Scopelessness and uninterpretable degree questions. In: Bekki, D.
619 (eds.) *Proc. International Workshop of Logic and Engineering of Natural Lan-*
620 *guage Semantics (LENLS)* **16** (2019) <https://www.academia.edu/43799952>
- 621 Zhang, L.: Split semantics for non-monotonic quantifiers in *than*-clauses. *Syntax*
622 *Semant.* **42**, 332–363 (2020) <https://doi.org/10.1163/9789004431515>
- 623 Zhang, L., Ling, J.: The semantics of comparatives: A difference-based approach.
624 *J. Semant.* **38**, 249–303 (2021) <https://doi.org/10.1093/jos/ffab003>