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# Comparative morphemes are additive particles 

English -er/more vs. Chinese gèng

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## 1 Introduction

Human languages support the expression of measurement and comparison. The notion of comparison is based on the notion of measurement. Measurement means mapping an entity/individual or event to a value on a relevant scale (e.g., a scale of height, weight, temperature, or timeline, see Stevens 1946), and comparison means establishing an ordering relation between scalar values.

As illustrated in (1) and (2), intuitively, two entities (here me and my cat) can be compared along different scales. In (1a/2a), comparison is conducted between height values, while in $(1 \mathrm{~b} / 2 \mathrm{~b})$, comparison is between weight values. ${ }^{1}$
(1) a. I am taller than my cat (is).

Comparing heights
b. I am heavier than my cat (is).

Comparing weights
(2) Comparatives in (Mandarin, same below) Chinese
a. wǒ bǐ wǒ-de māo gāo.

1SG STDD 1SG-POSS cat tall(er)
'I am taller than my cat.'
Comparing heights
b. wǒ bǐ wǒ-de māo zhòng.

1SG STDD 1SG-Poss cat heavy(er)
'I am heavier than my cat.'
Comparing weights

[^0][^1]Cross-linguistically, comparatives are often used to encode the meaning of a comparison that results in strict inequality relation (i.e., ' $>$ ').

As illustrated by (3), an English comparative contains these 5 elements (see e.g., Ultan 1972, Stassen 1985): (comparison) target (here Lucy), (comparison) standard (here Mary('s height)), gradable adjective (here tall), comparative morpheme -er/more, and standard marker than. A numerical differential (here 2 inches) is optional.
(3) $\underbrace{\text { Lucy }}_{\text {target }}$ is $\underbrace{(2 \text { inches })}_{\text {differential gradable adj. comparative morpheme standard marker standard }} \underbrace{\text { than }}_{\text {tall }} \underbrace{\text { ter }}_{\text {Mary }}$.

Intriguingly, human languages demonstrate great variation in comparatives. One much-discussed variation is whether comparatives require the use of morphemes like English -er/more (see e.g., Klein 1980, Bobaljik 2012).

As illustrated in (4-6), in languages like English and French, the morphosyntax of the positive and comparative use of gradable adjectives (e.g., tall, many, French grand) is distinguished by whether a comparative morpheme (e.g., -er/more, French plus) is obligatorily required. In the positive use (4a-6a), the presence of a comparative morpheme is forbidden, while in comparatives (4b-6b), omitting this comparative morpheme would lead to ungrammaticality.
(4) a. Lucy is tall.

Positive: tall
b. Lucy is (1 inch) taller than Mary is.

Comparative: tall $+e r$
(5) a. Lucy has many books.

Positive: many
b. Lucy has (three) more books than Mary does.

Comparative: many+er
(6) French
a. Jean est grand.

John be.3SG tall
'John is tall.'
Positive: grand 'tall'
b. Jean est (trois centimetres) plus grand que Pierre.

John be.3SG three cm more tall what Peter.
'John is ( 3 cm ) taller than Peter.' Comparative: plus + grand 'taller'

In contrast, as illustrated in (7) and (8), languages like Chinese and Japanese apparently lack comparative morphemes like English -er/more. For a gradable
adjective (e.g., Chinese gāo ('tall(er)'), Japanese taka- ('tall(er)')), the same form is adopted for both the positive and comparative use. ${ }^{2}$

## (7) Chinese

a. Lèlè gāo ma?

Lèlè tall Q
'Is Lèlè tall?'
Positive: $g \bar{a} o$ 'tall'
b. Lèlè bǐ Mǐmǐ gāo (wǔ límǐ) ma?

Lèlè STDD Mǐmǐ taller five $\mathrm{cm} \quad \mathrm{Q}$
'Is Lèlè ( 5 cm ) taller than Mǐmǐ?'
Comparative: $g \bar{a} o$ 'taller'
(8) Japanese
a. Rika-wa (se-ga) taka-i.

Rika-TOP back-NOM tall-PRES
'Rika is tall.' Positive: taka- 'tall'
b. Rika-wa Makoto-yori (go senti se-ga) taka-i.

Rika-TOP Makoto-StdD five cm back-NOM tall-PRES
'Rika is ( 5 cm ) taller than Makoto.' Comparative: taka- 'taller'
Starting with this empirical, theory-neutral observation on the morphosyntax of cross-linguistic comparatives (i.e., whether the presence of -er/morelike morphemes is required), this paper provides a novel perspective on the universals and variation underlying comparison. In a nutshell, we propose that:
(9) a. Comparison is universally conducted by gradable adjectives, rather than morphemes like -er/more (cf. the canonical view in the formal semantics literature on English comparatives, see $\S 2$ for details).
b. Languages with vs. without -er-like morphemes (e.g., English vs. Chinese) differ with regard to whether the lexical semantics of gradable adjectives encodes non-strict vs. strict inequalities (i.e., ' $\geq$ ' vs. ' $>$ ').
c. Morphemes like -er/more are additive particles, and crosslinguistically, different types of comparative morphemes contribute to achieve different kinds of additivity effects.

[^2]In particular, we highlight two kinds of comparative morphemes (or rather additive particles), English -er/more and Chinese gèng, and argue that
(10) a. English -er/more is similar to (an)other, denoting a positive value, an increase anaphoric to a contextually salient base item.
b. Chinese gèng is similar to moreover, indicating a threshold with enhanced positiveness for the positive use of gradable adjectives.

It is likely that cross-linguistically, there are other morphemes that achieve other kinds of additivity effects in expressions of comparison (e.g., see $\S 5.3$ for discussion on Chinese hái vs. Chinese gèng). The current paper does not aim to be exhaustive, but rather (i) initiate a new perspective on addressing the universals and variation underlying comparatives and (ii) connect comparatives with our existing understanding on additivity-related phenomena. Along the discussion, we try to be theory-neutral and make our analysis not overly technical. Many formal details as well as detailed investigation on more cross-linguistic phenomena will be for future work.

The rest of the paper is organized as follows. §2 presents challenges to the canonical view, paving the background for the current proposal. §3 presents our proposal: comparison is conducted by gradable adjectives. $\S 4$ analyzes English data, showing the division of labor between gradable adjectives and -er/more: the latter works as an additive particle similar to (an)other, denoting an increase and demonstrating anaphoricity. $\S 5$ extends the empirical scope to crosslinguistic phenomena, addressing what kind of additivity effects can appear in -er-less languages like Chinese. We analyze Chinese gèng as an additive particle similar to moreover, indicating enhanced positiveness for the positive use of gradable adjectives. $\S 6$ discusses further theoretical implications and concludes.

## 2 The canonical view and challenges

Within the canonical view on English comparatives (see §2.1), comparison, i.e., establishing the ordering relation ' $>$ ', is contributed by morpheme -er/more. We argue that this view on -er/more meets challenges both within and across languages (see §2.2). The discussion suggests that cross-linguistically, comparison should rather be conducted by gradable adjectives.

## 2．1 The canonical analysis on English comparatives

Within formal semantics，the canonical analysis of English comparatives （see e．g．，von Stechow 1984，Heim 1985，Kennedy 1999，Schwarzschild 2008， Beck 2011，among others）is built on these assumptions：
（11）a．A gradable adjective conveys the meaning of a scale，a totally or－ dered set of degrees（which are of type $d$ ）．
b．Comparison is between the measurements of the target and the stan－ dard along a scale，i．e．，between degrees，not between entities．
c．Comparative morpheme－er／more performs comparison by ex－ pressing the relation＇$>$＇between two degrees．

As shown in（12），the meaning of a gradable adjective contains a measure function，mapping an entity to a degree（see（12a）and Kennedy 1999）．Usually an operator＇$\geq$＇is also included，making 【tall】 a relation between a degree $d$ and an entity $x$（see（12b）and Cresswell 1976，Hellan 1981，von Stechow 1984， Heim 1985）．${ }^{3}$
a．$\llbracket \operatorname{tall} \rrbracket_{\langle e d\rangle} \stackrel{\text { def }}{=} \lambda x \cdot \operatorname{HEIGHT}(x) \quad$ a measure function of type $\langle e d\rangle$
b．$\llbracket \operatorname{tall} \rrbracket_{\langle d, e t\rangle} \stackrel{\text { def }}{=} \lambda d . \lambda x \cdot \operatorname{HEIGHT}(x) \geq d \quad$ a relation between $d$ and $x$ $\rightsquigarrow$ the height of $x$ reaches the degree $d$ ，i．e．，$x$ is tall to degree $d$

Based on（12b），the positive use（see（13））and measure construction （see（14））of a gradable adjective can be immediately accounted for．

In（13）and（14），【tall】 takes two arguments：a degree argument（here POS in（13）and $5^{\prime} 8^{\prime \prime}$ in（14））and an entity argument（here Lucy）．${ }^{4}$
（13）【Lucy is POS tall】 $\Leftrightarrow$ HEIGHT（Lucy）$\geq$ POS
Positive use （i．e．，the height measurement of Lucy reaches the threshold of being tall．） （POS：a silent，context－dependent free variable that represents the thresh－ old of being tall，see Bartsch \＆Vennemann 1972，Cresswell 1976，von Stechow 1984，Kennedy 1999）

[^3]（14）【Lucy is 5 feet 8 inches tall】 $\Leftrightarrow \operatorname{HEIGHT}($ Lucy $) \geq 5^{\prime} 8^{\prime \prime}$

## Measure

 （i．e．，the height measurement of Lucy reaches $5^{\prime} 8^{\prime \prime}$ ．）The meaning of a degree question（see（15））is naturally built on degree abstraction．（15）means the set of degrees reached by the height of Lucy（see Hausser \＆Zaefferer 1978，Hausser 1983＇s categorial approach to questions）．
（15）【how tall is Lucy】 $\Leftrightarrow \lambda d$ ． $\mathrm{HEIGHT}(\mathrm{Lucy}) \geq d$
Degree question
（This set is equivalent to $\{d \mid d \leq \operatorname{HEIGHT}($ Lucy $)\}$ ）
Inspired by subcomparatives like（16），the canonical analysis of compara－ tives assumes an elided gradable adjective in the than－clause（see Bresnan 1973， Bresnan 1975，Chomsky 1977）．${ }^{5}$ As shown in the LF in（17），the derivation of a comparative involves degree abstraction in both the matrix and the than－clause．
（16）The bathtub is wider than the door is tall．

## Subcomparative

（17）【Lucy is taller than Mary is tall』 $\Leftrightarrow$ HEIGHT（Lucy）$>$ HEIGHT（Mary）
LF：［－er［ $\lambda d$ ．Mary is $d$－tall ］］［ $\lambda d^{\prime}$ ．Lucy is $d^{\prime}$－tall ］
Eventually，comparative morpheme－er conducts comparison（see（18））．The core semantics of $-e r$ is thus a＇$>$＇relation between two degrees．To take care of semantic composition under the canonical analysis，－er is often defined as a relation between two sets of degrees，comparing the largest degree of each set （see（18a）and（18b）for two slightly different implementations）．${ }^{6}$
（18）－er essentially performs comparison between two degrees：
$\llbracket-\mathrm{er} \rrbracket_{\langle d,\langle d, t\rangle\rangle} \stackrel{\text { def }}{=} \lambda d_{1} \cdot \lambda d_{2} \cdot d_{2}>d_{1}$
a．$\llbracket-\mathrm{er} \rrbracket_{\langle\langle d t\rangle,\langle d t, t\rangle\rangle} \stackrel{\text { def }}{=} \lambda D_{1} \cdot \lambda D_{2} \cdot \operatorname{MAX}\left(D_{2}\right)>\operatorname{mAX}\left(D_{1}\right)$ $\left(\operatorname{MAX} \stackrel{\text { def }}{=} \lambda D . \iota d\left[d \in D \wedge \forall d^{\prime}\left[d^{\prime} \in D \rightarrow d^{\prime} \leq d\right]\right]\right) \quad$（see e．g．，Beck 2011）
b．$\llbracket-\mathrm{er} \rrbracket\langle\langle d t\rangle,\langle d t, t\rangle\rangle \stackrel{\text { def }}{=} \lambda D_{1} \cdot \lambda D_{2} . \exists d\left[d \in D_{2} \wedge d \notin D_{1}\right]$
（see e．g．，Schwarzschild 2008）
（For the LF in（17）$\rightsquigarrow \exists d$ s．t．Lucy is $d$－tall but Mary isn’t）

[^4]
## 2．2 Challenges to the canonical view

If，as shown in the above canonical analysis of English comparatives，the seman－ tics of－er／more is indeed to perform comparison（see（18）），it is puzzling how comparison is performed in－er－less languages like Chinese and Japanese（see（7） and（8））．Here we argue that even in－er－ful languages like English，comparison is performed by gradable adjectives，rather than morpheme－er／more．

First，although the use of－er／more is required in comparatives，actually all uses of gradable adjectives involve comparison，and in general，conducting comparison does not rely on the use of－er／more．

As illustrated in（19），these uses of gradable adjective tall all involve the comparison between the height of Lucy and a certain height degree，resulting in a＇$\geq$＇relation between degrees，but－er／more is not used．Thus，－er／more is not a necessary component for operating comparison．
a．$\llbracket$ Lucy is POS tall】 $\Leftrightarrow$ HEIGHT（Lucy）$\geq$ POS Positive use $(=(13))$
b．【Lucy is $5^{\prime} 8^{\prime \prime}$ inches tall】 $\Leftrightarrow \operatorname{HEIGHT}($ Lucy $) \geq 5^{\prime} 8^{\prime \prime}$
Measure（＝（14））
c．【how tall is Lucy】 $\Leftrightarrow \lambda d$ ． $\mathrm{HEIGHT}($ Lucy $) \geq d$
Degree Question（＝（15））
d．【Lucy is as tall as Bill（is）】 $\Leftrightarrow \operatorname{HEIGHT}($ Lucy $) \geq \operatorname{HEIGHT}$（Bill）

## Equative

Second，intuitively，the meaning distinction between the presence vs．absence of－er／more is not about whether there is a comparison，but often about（i）what constitutes the comparison standard and／or（ii）the size of the differential．

In the minimal pair in（20），without the use of－er，（20a）means that Lucy＇s height is compared with POS，a context－dependent threshold of being tall，while with the use of－er，（20b）means that Lucy＇s height is compared with Mary＇s． Thus（20a）and（20b）differ with regard to what the comparison standard is．
a．Mary is not tall．Lucy is POS tall．$\rightsquigarrow \operatorname{HEIGHT}($ Lucy $) \geq$ POS
b．Mary is not tall．Lucy is taller．$\rightsquigarrow \operatorname{HEIGHT}$（Lucy）$\geq$ HEIGHT（Mary）
In the minimal pair in（21），as addressed in the literature on crisp judgment （see Kennedy 2007），with the use of－er，（21b）is true under any scenario where Lucy＇s height exceeds Mary＇s，i．e．，（21b）has the same meaning as（17）．However， without the use of－er，（21a）is true only in scenarios where Lucy＇stands out＇ enough，i．e．，Lucy＇s height exceeds Mary＇s by a large enough difference．

Intuitively，in interpreting（21a），we also feel that Mary＇s height plays the role of an＇anchor＇or comparison class，having an influence on the value of the context－dependent POS，which Lucy＇s height is compared with．Thus we feel that （21a）and（21b）differ with regard to both comparison standard and differential．
a．Compared to Mary，Lucy is tall．
Implicit comparison
（i）Compared to 2－year－old toddlers，Lucy is tall．
（ii）（Even）compared to professional basketball players，Lucy is tall．
b．Compared to Mary，Lucy is taller．
Explicit comparison
Third，more fundamentally，gradable adjectives contribute the meaning of a scale，i．e．，a totally ordered set of degrees，and this ordering is the base of comparison．

Cross－linguistically，gradable adjectives have antonyms，indicating that in addition to mapping an entity to a scalar value（e．g．，a degree）along a scale， the lexical semantics of gradable adjectives also includes a component reflecting the direction of comparison．

As illustrated in（22），tall and short are antonyms in English，thus 【tall】 and【short】 basically share the same measure function，i．e．，mapping the same entity $x$ to the same scalar value， $\operatorname{HEIGHT}(x)$ ．However，the lexical meaning of 【tall】 and 【short】 involves different directions，represented as different comparison operators in（22a）and（22b）：＇$\geq$＇vs．＇$\leq$＇．

$$
\begin{align*}
& \text { a. } \quad \llbracket t \operatorname{tall} \rrbracket_{\langle d, e t\rangle} \stackrel{\text { def }}{=} \lambda d . \lambda x \text {. } \operatorname{HEIGHT}(x) \geq d  \tag{22}\\
& \text { ( }=12 \mathrm{~b}) \\
& \text { b. } \llbracket \text { short } \rrbracket\langle d, e t\rangle \stackrel{\text { def }}{=} \lambda d . \lambda x \text {. } \operatorname{HEIGHT}(x) \leq d
\end{align*}
$$

Overall，the above discussion suggests that（i）performing comparison does not necessarily involve the use of－er，（ii）the use of－er is more relevant to the interpretation of standard or differential，and（iii）the meaning of gradable adjectives already includes comparison operators which are direction－sensitive． Thus，most naturally，comparison should be performed by gradable adjectives， not morphemes like－er．

In this sense，various uses of gradable adjectives are fundamentally mak－ ing comparison．Across languages and within one language，various gradable－ ajective－based constructions differ rather with regard to the parameters of（i） comparison standard and（ii）differential．Below，we present detailed formal im－ plementation of this unfied perspective on comparison，along with the discussion on how English－er／more and Chinese gèng affect the standard and differential．


Fig. 1: The meaning of tall (see (24))
Fig. 2: The meaning of short (see (25))

## 3 Proposal: gradable adjectives and comparison

We follow Zhang \& Ling (2021) to present a unified perspective on comparison, using interval subtraction, instead of inequalities between two degrees, to characterize comparison. §3.1 addresses how the meaning of gradable adjectives encodes comparison, and then $\S 3.2$ §§3.6 demonstrates the meaning derivation of various gradable-adjective-based constructions in English. ${ }^{7}$

### 3.1 The semantics of gradable adjectives

As shown in (24/25) and illustrated in Fig. 1 and Fig. 2, the semantics of gradable adjective tall/short can be characterized as a subtraction relation among three scalar values, which are all represented as intervals (of type $\langle d t\rangle$ ), i.e., convex sets of degrees (of type $d$ ): ${ }^{8}$
7. The current paper is distinct from Zhang \& Ling (2021) in two aspects. First, we explicitly encode the parameters of comparison standard and differential in the semantics of gradable adjectives. Second, we address the direction difference between tall and short. 8. A totally ordered set $P$ is convex iff for any elements $a$ and $b$ in the set (suppose $a \leq b$ ), any element $x$ such that $a \leq x \leq b$ is also in the set $P$. Thus intervals can be written with their upper and lower bounds: square brackets '[' and ']' mean closed lower and upper bounds, and round parentheses '(' and ')' mean open lower and upper bounds. E.g.,
(i) $\left\{x \mid I_{\text {min }} \leq x \leq I_{\text {max }}\right\}=\left[I_{\text {min }}, I_{\text {max }}\right]$
$\left\{x \mid I_{\min }<x \leq I_{\max }\right\}=\left(I_{\text {min }}, I_{\text {max }}\right]$ $\left\{x \mid I_{\text {min }} \leq x<I_{\text {max }}\right\}=\left[I_{\text {min }}, I_{\text {max }}\right)$ $\left\{x \mid I_{\text {min }}<x<I_{\text {max }}\right\}=\left(I_{\text {min }}, I_{\text {max }}\right)$

A left- and right-closed interval A left-open and right-closed interval A left-closed and right-open interval A left- and right-open interval

A singleton set like $\left\{x \mid x=3^{\prime \prime}\right\}$ can be written as $\left[3^{\prime \prime}, 3^{\prime \prime}\right]$. We write positive and negative infinity as ' $+\infty$ ' and ' $-\infty$ '. Thus 'неIGHT $(x) \subseteq\left(-\infty, d_{\text {POS }}^{c}\right.$ )' means that the height of $x$ does not reach the threshold degree $d_{\text {Pos }}^{c}$. Although in our actual world, somebody's height cannot be a value below zero, it is not logically or linguistically impossible.
(23) a. the height measurement of comparison target, $x$ : $\operatorname{HEIGHT}_{\langle e, d t\rangle}(x)$
b. the interval standing for the comparison standard: $I_{\text {STDD }}$
c. the interval standing for the distance between the above two: $I_{\text {DIFF }}$.
(i) The lower bound of $I_{\text {DIFF }}$ is the minimal difference
(ii) The upper bound of $I_{\text {DIFF }}$ is the maximal difference

$$
\begin{equation*}
\llbracket \mathrm{tall} \rrbracket \stackrel{\text { def }}{=} \lambda I_{\mathrm{DIFF}} \cdot \lambda I_{\text {STDD }} \cdot \lambda x \cdot \underbrace{I_{\text {DIFF }} \subseteq[0,+\infty)}_{\text {non-negative presupposition }} \operatorname{cf.}(70)) \tag{24}
\end{equation*}
$$

$$
\begin{equation*}
\llbracket \mathrm{short} \rrbracket \stackrel{\text { def }}{=} \lambda I_{\mathrm{DIFF}} \cdot \lambda I_{\mathrm{STDD}} \cdot \lambda x \cdot \underbrace{I_{\mathrm{DIFF}} \subseteq[0,+\infty)}_{\text {non-negative presupposition }} \operatorname{HGHT}(x) \subseteq \iota I\left[I_{\mathrm{STDD}}-I=I_{\mathrm{DIFF}}\right] \tag{25}
\end{equation*}
$$

The lexical semantics in $(24 / 25)$ is distinct from the canonical analysis (see (12b), repeated here as (26)) mainly in three aspects.

$$
\begin{equation*}
\llbracket \operatorname{tall} \rrbracket_{\langle d, e t\rangle} \stackrel{\text { def }}{=} \lambda d \cdot \lambda x \cdot \operatorname{HEIGHT}(x) \geq d \tag{26}
\end{equation*}
$$

$$
(=12 \mathrm{~b})
$$

First, the canonical analysis in (26) contains only one degree argument, but $(24 / 25)$ contains two scalar-value arguments: $I_{\text {DIFF }}$ and $I_{\text {STDD }}$. By explicitly encoding the scalar values standing for (i) the differential and (ii) the standard in the semantics of gradable adjectives, the current analysis shows more clearly the details of the operation of comparison, helping reason about how differentials and standards contribute to comparison and get further modified or restricted.

The interval subtraction between two intervals $I_{1}$ and $I_{2}$ results in the largest range of possible differences between any two points in $I_{1}$ and $I_{2}$ :


Thus, given the subtrahend $[a, b]$ and the difference $[c, d]$,
(iii) Minuend $=[b+c, a+d]$
(defined when $b+c \leq a+d$ )
Given the minuend $[a, b]$ and the difference $[c, d]$,
(iv) Subtrahend $=[b-d, a-c] \quad$ (defined when $b-d \leq a-c)$

See Moore (1979) for details on intervals and interval arithmetic.

Second，the canonical analysis in（26）uses inequality to represent compari－ son，while in $(24 / 25)$ ，comparison is represented by interval subtraction．This is related to the previous aspect．Subtraction enables to characterize the relation among three scalar values represented as intervals（i．e．， $\operatorname{HEIGHT}(x), I_{\text {STdD }}$ ，and $I_{\text {DIFF }}$ in $(24 / 25)$ ），instead of two degrees（i．e．， $\operatorname{HEIGHT}(x)$ and $d$ in（26））．

Third，the canonical uses degree semantics，while the current proposal fol－ lows Zhang（2021）and adopts interval semantics．Degrees（of type d）are pointed elements on a scale，while intervals are convex sets of degrees．Thus， intervals represent scalar values in a more generalized way，characterizing both pointed，precise values and not－very－precise values．Human languages naturally support the comparison between not－very－precise values and motivate the use of interval semantics．E．g．，
（27）Lucy is a bit taller than every boy is．
$\rightsquigarrow \operatorname{HEIGHT}$（Lucy）is compared with a range of boys＇heights
A pair of antonyms（e．g．，【tall】 vs．【short】）differ with regard to the direction of comparison／subtraction．Intuitively，for 【tall】（see（24）and Fig．1），HEIGHT（ $x$ ） is compared with a standard interval $I_{\text {STDD }}$ lower than HEIGHT $(x)$ along the scale， while for $\llbracket$ short】（see（25）and Fig．2）， $\operatorname{HEIGHT}(x)$ is compared with a standard interval $I_{\text {STDD }}$ above HEIGHT $(x)$ ．

It is worth noting that in（24）and（25），the non－negative presupposition for the difference（i．e．，$I_{\text {IDFF }} \subseteq[0,+\infty)$ ）means that comparison expressed by En－ glish gradable adjectives corresponds to a non－strict inequality．E．g．，【tall】 and 【short】 essentially address to what extent $\operatorname{HEIGHT}(x)$ occurs at or is above／below the standard $I_{\text {STDD }}$（cf．Chinese gradable adjectives，see $\S 5.1$ ）．

Another thing worth noting is that，as shown in Fig． 1 and 2， $\operatorname{HEIGHT}(x)$ and $I_{\text {STDD }}$ are intervals along the same scale（here a scale of height）．However，$I_{\text {DIFF }}$ is conceptually distinct：it is an interval along a scale of height differences．

This is also evidenced by examples like（28）．The expression o＇clock is used to mark degree positions along a timeline，while units like hour are used to measure differences／distances between time positions．
（28）She arrived at 10 o＇clock，exactly 1 hour earlier than scheduled．
a．The measurement of target（her actual arrival）：$[10: 00,10: 00]$
b．$I_{\text {STDD }}$ ：the scheduled arrival time，i．e．，$[11: 00,11: 00]$
c．$I_{\mathrm{DIFF}}:[1 \mathrm{~h}, 1 \mathrm{~h}]$
The Chinese data in（29）also supports the claim that $I_{\text {DIFF }}$ is conceptually different．To form a question on the position along a timeline，adjective
zăo 'early' is used, as in (29a). ${ }^{9}$ In contrast, if the question is about the time difference, adjective jiǔ 'long' is used, as in (29b). Such phenomena are not unexpected at all if there is a conceptual distinction between $I_{\text {DIFF }}$ and $I_{\text {STDD }}$ : $I_{\text {DIFF }}$ denotes temporal differences, unlike $I_{\text {STDD }}$ and the actual arrival time which mean positions along the timeline (see Xiang 2005 for a similar view).
a. Tā dào-de duó zǎo?

3SG arrive-LNK how-much early
'How early did she arrive?'
b. Tā dào-de (bǐ yùjì) zǎo (le) duó jiǔ? 3SG arrive-LNK STDD expected early ASP how-much long 'By how long did she arrive earlier (than expected)?'

As summarized in (30), various uses of gradable adjectives all express comparison, but differ with regard to what serve as the two scalar-value arguments, i.e., $I_{\mathrm{DIFF}}$ and $I_{\text {STDD }}$. We present more details in§3.2-§3.6.

Various uses of gradable adjectives in English

|  | $I_{\mathrm{STDD}}$ | $I_{\mathrm{DIFF}}$ |
| :--- | :--- | :--- |
| Positive use <br> (see $\S 3.2$ ) | Contextual threshold: <br> $\left[d_{\mathrm{POS}}^{c}, d_{\mathrm{POS}}^{c}\right]$ | $[0,+\infty)$ <br> (or further restricted <br> by a modifier like very) |
| Measure constructions <br> (see $\S 3.3$ ) | Absolute zero point: | restricted by a <br> measure phrase |
| Degree questions | $[0,0]$ | Contextual threshold |
| (see $\S 3.4$ ) | or absolute zero point | (interval abstraction) |
| Equatives | Measurement of the | $[0,+\infty)$ |
| (see $\S 3.5$ ) | standard |  |
| Comparatives | Measurement of the | $\llbracket-$ er $\rrbracket_{\langle d t\rangle}:(0,+\infty)$ |
| (see $\S 3.6$ ) | standard | (or further restricted by a <br> numerical differential) |

### 3.2 The semantics of the positive use

The positive use addresses a comparison with a context-dependent threshold. As illustrated in (31-34), for the positive use of gradable adjectives tall/short,

[^5]（i）the differential argument $I_{\text {DIFF }}$ is a default，unspecified，non－negative interval that stands for the range of height difference，while（ii）the standard argument $I_{\text {STDD }}$ is a context－dependent threshold of being tall or short．
\[

$$
\begin{gather*}
\llbracket \text { Lucy is POS tall } \rrbracket \Leftrightarrow \operatorname{HEIGHT}(\text { Lucy }) \subseteq \iota I[I-\underbrace{\left[d_{\text {POS }}^{c}, d_{\text {POS }}^{c}\right]}_{I_{\text {STDD }}}=\underbrace{[0,+\infty)}_{I_{\text {DIFF }}}]  \tag{31}\\
\Leftrightarrow \operatorname{HEIGHT}\left(\text { Lucy } \subseteq\left[d_{\text {POS }}^{c},+\infty\right)\right. \\
\text { (i.e., the height of Lucy reaches the contextual threshold of being tall) }
\end{gather*}
$$
\]

（32）$\llbracket$ Lucy is not POS tall】 $\Leftrightarrow \llbracket n o t \rrbracket \llbracket$ Lucy is POS tall】

$$
\Leftrightarrow \operatorname{HEIGHT}(\text { Lucy }) \subseteq\left(-\infty, d_{\mathrm{POS}}^{c}\right)
$$

（i．e．，the height of Lucy doesn＇t reach the threshold of being tall）
（33）$\llbracket$ Chloe is $\mathrm{POS}^{\prime} \rrbracket \Leftrightarrow \operatorname{HEIGHT}($ Chloe $) \subseteq \iota I\left[\left[d_{\mathrm{POS}^{\prime}}^{c}, d_{\mathrm{POS}^{\prime}}^{c}\right]-I=[0,+\infty)\right]$

$$
\Leftrightarrow \operatorname{HEIGHT}(\text { Chloe }) \subseteq\left(-\infty, d_{\mathrm{POS}^{\prime}}^{c}\right]
$$

（i．e．，Chloe＇s height is the same as or below the threshold of being short）
（34）$\llbracket$ Chloe is not $\mathrm{POS}^{\prime} \rrbracket \Leftrightarrow \llbracket$ not $\rrbracket \llbracket$ Chloe is Pos＇short】

$$
\Leftrightarrow \operatorname{HEIGHT}(\text { Chloe }) \subseteq\left(d_{\mathrm{POS}^{\prime}}^{c},+\infty\right)
$$

（i．e．，the height of Chloe is above the contextual threshold of being short）
Of course，under a given context，the threshold of being short and the thresh－ old of being tall are usually different，as evidenced by sentences like（35）：
（35）【Mary is neither $\mathrm{POS}_{1}$ tall nor $\mathrm{POS}_{2}$ short】

$$
\begin{aligned}
& \Leftrightarrow \underbrace{\operatorname{HEIGHT}(\text { Mary }) \subseteq\left(d_{\mathrm{POS}_{2}}^{c},+\infty\right)}_{\llbracket \text { not POS }} \wedge \underbrace{\operatorname{HEIGHT}(\text { Mary }) \subseteq\left(-\infty, d_{\mathrm{POS}_{1}}^{c}\right)}_{\llbracket \text { not } \mathrm{POS}_{1} \text { tall】 }} \\
& \Leftrightarrow \operatorname{HEIGHT}(\text { Mary }) \subseteq\left(d_{\mathrm{POS}_{2}}^{c}, d_{\mathrm{POS}_{1}}^{c}\right)
\end{aligned}
$$

In the positive use of gradable adjectives，as illustrated in（37）and（38）， degree modifiers like very，quite，a bit，and extremely can be included to further restrict the range of $I_{\text {DIFF }}$（see（36）），i．e．，to what extent the measurement of the target is above（see（37））or below（see（38））the contextual threshold $d_{\text {Pos }}^{c}$ ．

In this sense，$I_{\text {DIFF }}$ ，as a scalar value on a scale of height differences（not a scale of heights！），can further undergo measurement and comparison along this scale of differences．In（37）and（38），$d_{\text {DIFF－Pos }}^{c}$ and $d_{\text {DIFF－POS }}^{c}{ }^{\prime}$ mean contextual thresholds of being large or small along a scale of height differences．${ }^{10}$

[^6]（36）Degree modifiers like 【very】 ${ }_{\langle d t, d t\rangle}$ take an interval as input and return a more restricted one（by set intersection）．E．g．，【very】takes $[0,+\infty$ ）as input and returns one with a higher lower bound，$\left[d^{\prime},+\infty\right)$（here $d^{\prime}>0$ ）．
a．【Jessica is very POS tall】
$\Leftrightarrow \operatorname{HEIGHT}(J e s s i c a) \subseteq \iota I\left[I-\left[d_{\mathrm{POS}}^{c}, d_{\mathrm{POS}}^{c}\right]=\left[d_{\mathrm{DIFF}-\mathrm{POS}}^{c},+\infty\right)\right]$
$\Leftrightarrow \operatorname{HEIGHT}($ Jessica $) \subseteq\left[d_{\mathrm{POS}}^{c}+d_{\mathrm{DIFF}-\mathrm{POS}}^{c},+\infty\right)$
（i．e．，（i）Jessica＇s height reaches the threshold of being tall，$d_{\text {POS }}^{c}$ ，and （ii）the difference between HEIGHT（Jessica）and $d_{\text {POS }}^{c}$ is large enough， reaching the threshold $d_{\text {DIFF－Pos }}^{c}$ along a scale of height differences）
b．【Jessica is quite POS tall】
$\Leftrightarrow \operatorname{HEIGHT}($ Jessica $) \subseteq \iota I[I-\left[d_{\mathrm{POS}}^{c}, d_{\mathrm{POS}}^{c}\right]=\underbrace{\left[d_{\mathrm{DIFF}}^{c}{ }_{\mathrm{P}}, d_{\mathrm{DIFF}}^{c}{ }^{\prime}{ }^{\prime}\right]}_{\text {i．e．，} I_{\mathrm{DIFF}} \text { is within }}]$
a range of height differences
$\Leftrightarrow \operatorname{HEIGHT}($ Jessica $) \subseteq\left[d_{\mathrm{POS}}^{c}+d_{\mathrm{DIFF}-\mathrm{POS}}^{c}, d_{\mathrm{POS}}^{c}+d_{\mathrm{DIFF}-\mathrm{POS}}{ }^{\prime}\right]$
a．【Betty is a bit POS short】
\[

$$
\begin{align*}
& \Leftrightarrow \operatorname{HEIGHT}(\text { Betty }) \subseteq \iota I[\left[d_{\mathrm{POS}}^{c}, d_{\mathrm{POS}}^{c}\right]-I=\underbrace{\left[0, d_{\mathrm{DIFF}-\mathrm{PoS}}^{c}\right]}_{\begin{array}{c}
\text { i.e., the upper bound of } I_{\mathrm{DFFF}} \\
\text { does not exceed } d_{\mathrm{DIFF}-\mathrm{PoS}}^{c}
\end{array}}  \tag{38}\\
& \Leftrightarrow \operatorname{HEIGHT}(\text { Betty }) \subseteq\left[d_{\mathrm{POS}}^{c}-d_{\mathrm{DIFF-POS}}^{c}, d_{\mathrm{POS}}^{c}\right]
\end{align*}
$$
\]

b．【Betty is extremely POS short】

$$
\begin{aligned}
& \Leftrightarrow \operatorname{HEIGHT}(\text { Betty }) \subseteq \iota I[\left[d_{\mathrm{POS}}^{c}, d_{\mathrm{POS}}^{c}\right]-I=\underbrace{\left[d_{\mathrm{DIFF} \text {-POS }}^{c},+\infty\right)}_{\text {i.e., the lower bound of } I_{\text {DIFF }} \text { is }} \\
& \Leftrightarrow \operatorname{HEIGHT}(\text { Betty }) \subseteq\left(-\infty, d_{\mathrm{POS}}^{c}-d_{\mathrm{DIFF} \text {-Pos }}^{c}\right]
\end{aligned}
$$


#### Abstract

that the latter denotes a property whose meaning is just like the former＇s，except that the relative standard is raised by some amount＇．The current analysis yields the same truth condition as the canonical analysis，but the effect of including a degree modifier like very is to restrict $I_{\text {DIFF }}$ ，rather than to raise the value of the standard $d_{\text {STDD }}$ ．

We believe that conceptually，the current analysis is advantageous at the discourse level． E．g．，for（i），it is reasonable to assume that the height of every girl is compared with the same threshold of being short．


（i）Q：How short are the girls？$\rightsquigarrow$ For every girl $x$ ，compare HEIGHT $(x)$ with $d_{\text {Pos }}^{c}$ A：Lucy is short．Jessica is very short．Mary is also a bit short．

### 3.3 The semantics of the measurement construction

Measurement constructions address a comparison with the absolute zero point.
As illustrated in (39), in a measurement construction, (i) the differential argument $I_{\text {DIFF }}$ is restricted by a measure phrase (here 5 feet 8 inches), while (ii) the standard argument $I_{\text {STDD }}$ is the absolute zero point along a scale. ${ }^{11}$

In natural language, bare numerals can have (i) an 'at least' interpretation and (ii) a strengthened 'exactly' interpretation (see Spector 2013 for a review), projecting to the two readings of measurement sentences (see (39a) and (39b)).
(39) 【Lucy is 5 feet 8 inches tall】
a. 'At least' interpretation of 5 feet 8 inches:

$$
\begin{aligned}
\llbracket 39 \rrbracket & \Leftrightarrow \operatorname{HEIGHT}(\text { Lucy }) \subseteq \iota I\left[I-[0,0]=\left[5^{\prime} 8^{\prime \prime},+\infty\right)\right] \\
& \Leftrightarrow \operatorname{HEIGHT}(\text { Lucy }) \subseteq\left[5^{\prime} 8^{\prime \prime},+\infty\right)
\end{aligned}
$$

b. 'Exactly' interpretation of 5 feet 8 inches:

$$
\begin{aligned}
\llbracket 39 \rrbracket & \Leftrightarrow \operatorname{HEIGHT}(\text { Lucy }) \subseteq \iota I\left[I-[0,0]=\left[5^{\prime} 8^{\prime \prime}, 5^{\prime} 8^{\prime \prime}\right]\right] \\
& \Leftrightarrow \operatorname{HEIGHT}(\text { Lucy }) \subseteq\left[5^{\prime} 8^{\prime \prime}, 5^{\prime} 8^{\prime \prime}\right]
\end{aligned}
$$

As illustrated in (40), for a gradable adjective like short, the subtraction between the standard $I_{\text {STDD }}$ (which is $[0,0]$ ) and the measurement of target (which is HEIGHT(Chloe), a positive value) would result in a negative value, violating the non-negative presupposition of $I_{\mathrm{DIFF}}$ and leading to ungrammaticality.
(40)\# Chloe is 5 feet short. $\quad[0,0]-$ HEIGHT(Chloe) is negative (see Fig. 2)

### 3.4 The semantics of degree questions

Degree questions address a comparison relative to a reference position: e.g., a zero point or a context-dependent threshold. Intuitively, we seek an answer that addresses the position of the target on a scale (see e.g., (29a)) or the distance between the target's position and the reference position (see e.g., (29b)).

[^7]Addressing the distance is straightforward under the current proposal. As illustrated in (41-42), (i) the differential $I_{\text {DIFF }}$ is abstracted to form a degree question, while (ii) the standard argument $I_{\text {STDD }}$ can be either the absolute zero point along a scale (see (41a)) or the context-dependent threshold of being tall (see (41b/42)). Thus a degree question essentially denotes a set of intervals: a set of distances relative to a reference (see Hausser \& Zaefferer 1978, Hausser 1983 for categorial approaches to questions).
(41) $\llbracket$ How tall is Lucy $\rrbracket \Leftrightarrow \lambda I_{\mathrm{DIFF}} \cdot \mathrm{HEIGHT}($ Lucy $) \subseteq \iota I\left[I-I_{\mathrm{STDD}}=I_{\mathrm{DIFF}}\right]$
a. $I_{\text {STDD }}$ is equal to $[0,0]$ : No evaluativity $\llbracket 41 \rrbracket \Leftrightarrow \lambda I_{\text {DIFF }} . \operatorname{HEIGHT}($ Lucy $) \subseteq \iota I\left[I-[0,0]=I_{\mathrm{DIFF}}\right]$
b. $I_{\text {STDD }}$ is equal to $\left[d_{\text {POS }}^{c}, d_{\text {POS }}^{c}\right]$ : Evaluativity

$$
\llbracket 41 \rrbracket \Leftrightarrow \lambda I_{\mathrm{DIFF}} \cdot \mathrm{HEIGHT}(\mathrm{Lucy}) \subseteq \iota I\left[I-\left[d_{\mathrm{POS}}^{c}, d_{\mathrm{POS}}^{c}\right]=I_{\mathrm{DIFF}}\right]
$$

(42) $\llbracket$ How short is Chloe $₫ \Leftrightarrow \lambda I_{\text {DIFF }}$.HEIGHT(Chloe) $\subseteq \iota I\left[I_{\text {STDD }}-I=I_{\mathrm{DIFF}}\right]$ $I_{\text {STDD }}$ is equal to $\left[d_{\mathrm{POS}}^{c}, d_{\mathrm{POS}}^{c}\right]$ :

Evaluativity
$\llbracket 42 \rrbracket \Leftrightarrow \lambda I_{\mathrm{DIFF}} . \mathrm{HEIGHT}($ Chloe $) \subseteq \iota I\left[\left[d_{\mathrm{POS}}^{c}, d_{\mathrm{POS}}^{c}\right]-I=I_{\mathrm{DIFF}}\right]$
For a degree question based on tall, when $I_{\text {STDD }}$ is the zero point (see (41a)), there is no evaluativity in interpreting the degree question. E.g., for (41a), Lucy is not necessarily tall, because HEIGHT(Lucy) does not necessarily reach $d_{\text {POS }}^{c}$.

However, when $I_{\text {STDD }}$ is the context-dependent threshold of being tall/short (see (41b/42)), there is evaluativity in interpreting the degree question. E.g., in interpreting (41b), since $I_{\text {DIFF }}$ is presupposed to be non-negative, HEIGHT(Lucy) must reach the threshold $d_{\text {POS }}^{c}$, i.e., Lucy is tall. Similarly, as illustrated in (42), there is evaluativity in interpreting how short is Chloe, i.e., Chloe is short, and this degree question addresses to what extent Chloe is short.

Answerhood operator $\mathbf{A n s}_{\text {diff }}$ (of type $\langle\langle d t, t\rangle, d t\rangle$, see (43)) takes a set of intervals as input and returns the most informative one (see Dayal 1996 on the notion of answerhood). When $\mathbf{A n s}_{\text {DIFF }}$ is applied to a degree question like (41) or (42), the most informative answer (i.e., an interval) is returned, addressing the distance between HEIGHT(Lucy) (or HEIGHT(Chloe)) and the reference (see Fig. 3).
(43) An answerhood operator $\mathbf{A n s}_{\text {DifF }}$ is defined for a set of intervals $p$ s.t.

$$
\left.\left.\exists I\left[p(I) \wedge \forall I^{\prime}\left[[p] I^{\prime}\right] \wedge I^{\prime} \neq I\right] \rightarrow I \subsetneq I^{\prime}\right]\right]
$$

When defined, $\mathbf{A n s}_{\text {DIFF }} \stackrel{\text { def }}{=} \lambda p_{\langle d t, t\rangle} . \iota I\left[p(I) \wedge \forall I^{\prime}\left[\left[p\left(I^{\prime}\right) \wedge I^{\prime} \neq I\right] \rightarrow I \subsetneq I^{\prime}\right]\right]$


Fig．3：Interpreting how tall is Lucy with the reference position at the zero point

We define two type－shifters，Position－M（see（44），for gradable adjectives like tall）and Position－S（see（45），for gradable adjectives like short），to com－ pute the position of the target from its distance away from the reference position $I_{\text {STDD }}$（i．e．，$[0,0]$ or $\left[d_{\mathrm{POS}}^{c}, d_{\mathrm{POS}}^{c}\right]$ ，see Fig．3）．

Position－ $\mathbf{M} \stackrel{\text { def }}{=} \lambda I_{\mathrm{DIFF}} . L I\left[I-I_{\mathrm{STDD}}=I_{\mathrm{DIFF}}\right]$
$\left(I_{\mathrm{STDD}}\right.$ is $[0,0]$ or $\left.\left[d_{\mathrm{POS}}^{c}, d_{\mathrm{POS}}^{c}\right]\right)$

Position－S $\stackrel{\text { def }}{=} \lambda I_{\mathrm{DIFF}} . \iota\left[I_{\mathrm{STDD}}-I=I_{\mathrm{DIFF}}\right]$
（ $I_{\text {STDD }}$ is $\left[d_{\mathrm{POS}}^{c}, d_{\mathrm{POS}}^{c}\right]$ ）

## Minuend position

（see footnote 8：（iii））

## Subtrahend position

（see footnote 8：（iv））

E．g．，for（41a），if $\mathbf{A n s}_{\text {DIFF }} \llbracket(41 \mathrm{a}) \rrbracket$ is $\left[5^{\prime} 8^{\prime \prime}, 6^{\prime}\right]$ ，it means that HEIGHT（Lucy）is between $5^{\prime} 8^{\prime \prime}$ and $6^{\prime}$ above the zero point．Position－M［Ans $\mathbf{A l F F}^{\text {IF }}[(41 a) \rrbracket]$ means the position where HEIGHT（Lucy）is at along this scale of heights（see Fig．3）．

## 3．5 The semantics of equatives

As illustrated in（46－47），in equatives，（i）the differential argument $I_{\text {DIFF }}$ is a default，unspecified，non－negative interval，i．e．，$[0,+\infty$ ），while（ii）the standard $I_{\text {STDD }}$ is essentially the position of the comparison standard along a scale（i．e．， in（46）and（47）：the positions in addressing＇how tall／short Bill／Ann is＇）．
（46）【Lucy is as tall as Bill（is）tall】
$\Leftrightarrow \operatorname{HEIGHT}($ Lucy $) \subseteq \iota I[I-\underbrace{\llbracket \text { as Bill is tall }]}_{I_{\text {STDD }}}=\underbrace{[0,+\infty)}_{I_{\text {DIFF }}}]$
a．【as Bill is Position－M［Ans diff $_{\text {dhow }}$ tall Bill is』］，i．e．， $\operatorname{HGHT}(\mathrm{B})$
b．$\llbracket 46 \rrbracket \Leftrightarrow \operatorname{HEIGHT}($ Lucy $) \subseteq \iota I[I-\operatorname{HEIGHT}($ Bill $)=[0,+\infty)]$
$\rightsquigarrow$ The height of Lucy is equal to or above the height of Bill
（47）【Chloe is as short as Ann（is）short』

$$
\Leftrightarrow \operatorname{HEIGHT}(\text { Chloe }) \subseteq \iota I[\underbrace{[\text { as Ann is short }]}_{I_{\text {sTDD }}}-I=\underbrace{[0,+\infty)}_{I_{\text {DIFF }}}]
$$

a．【as Ann is Short $\rrbracket$ ：Position－S $\left[\mathbf{A n s}_{\text {DIFF }} \llbracket\right.$ how short A．is $\left.\rrbracket\right]$ ，i．e．， HT （A）
b．$\llbracket 47 \rrbracket \Leftrightarrow \operatorname{HEIGHT}($ Lucy $) \subseteq \iota I[\operatorname{HEIGHT}(A n n)-I=[0,+\infty)]$
$\rightsquigarrow$ The height of Chloe is equal to or below the height of Ann
In（46）and（47），we assume that 【as Bill is and 【as Chloe is short】 are embedded clauses that contain an elided gradable adjective．We follow the above recipe for degree questions and apply Ans diff and type－shifters Position－ M／Position－S．Eventually，these embedded clauses denote the position where Bill／Ann is mapped to along a relevant scale，which further serves as the stan－ dard $I_{\text {STDD }}$ in computing the meaning of the matrix clause（see Fleisher 2018， Fleisher 2020，Zhang \＆Ling 2021 for a similar view）．

A welcome consequence is that in interpreting equatives like（46）and（47）， the（un）availability of evaluativity（e．g．，（47）means that both Chloe and Ann are short）corresponds to the（un）availability of evaluativity of the embedded degree questions．Degree question how short Ann is is evaluative，and thus（47） is evaluative．Degree question how tall Bill is is not necessarily evaluative（see （41a）vs．（41b）），and thus（46）is not necessarily evaluative．

## 3．6 The semantics of comparatives

In comparatives，（i）the differential argument $I_{\text {DIFF }}$ is contributed by morpheme －er／more，a positive（not non－negative！）interval，which can further get restricted by a numerical differential，while（ii）the standard $I_{\text {STDD }}$ is similar to that of equatives，i．e．，a position along a relevant scale that addresses the measurement of the comparison standard（e．g．，（48））．
（48）【than every boy is tall】＝Position－M［Ans diff $_{\text {［how tall every boy is } \rrbracket]}$ i．e．$\iota I[\forall x[\operatorname{boy}(x) \rightarrow \operatorname{HEIGHT}(x) \subseteq I]]$
$\rightsquigarrow$ the most informative interval $I$ s．t．，for each boy $x, \operatorname{HEIGHT}(x) \subseteq I$ ， i．e．，the interval ranging from the height of the shortest boy to that of the tallest boy，which can be written as［ $d_{\text {shortest }}, d_{\text {tallest }}$ ］

Based on the analysis of the than－clause in（48），（49）shows how the meaning of a comparative is composed from $\llbracket-\mathrm{er} \rrbracket$ and the meaning of the than－clause． Eventually，（49）means that Lucy＇s height is above that of the tallest boy．
（49）【Lucy is taller than every boy（is）tall】
$\Leftrightarrow \operatorname{HEIGHT}($ Lucy $) \subseteq \iota I[I-\llbracket$ than every boy is tall $\rrbracket=(0,+\infty)]$
$\Leftrightarrow \operatorname{HEIGHT}($ Lucy $) \subseteq \iota I[I-\iota I[\forall x[\operatorname{boy}(x) \rightarrow \operatorname{HEIGHT}(x) \subseteq I]]=(0,+\infty)]$

$$
\begin{aligned}
& \Leftrightarrow \operatorname{HEIGHT}(\text { Lucy }) \subseteq \iota I\left[I-\left[d_{\text {shortest }}, d_{\text {tallest }}\right]=(0,+\infty)\right] \\
& \Leftrightarrow \operatorname{HEIGHT}(\text { Lucy }) \subseteq\left(d_{\text {tallest }},+\infty\right)
\end{aligned}
$$

The default positive interval $\llbracket$－er】can be further restricted by a numerical differential like about 2 inches．As illustrated in（50），the more restricted interval $I_{\text {DIFF }}$ is $\left[2^{\prime \prime}-\varepsilon, 2^{\prime \prime}+\varepsilon\right]$ ．Thus eventually，（50）means that Lucy＇s height is within the interval $\left[d_{\text {tallest }}+2^{\prime \prime}-\varepsilon, d_{\text {shortest }}+2^{\prime \prime}+\varepsilon\right]$ ，and this interval is defined if among the boys，the tallest one does not exceed the shortest one too much．Similarly， in（51），much also plays the role of restricting 【－er】．
（50）«Lucy is about 2 inches taller than every boy（is）tall】

$$
\begin{aligned}
& \Leftrightarrow \operatorname{HEIGHT}(\text { Lucy }) \subseteq \iota I[I-\left[d_{\text {shortest }}, d_{\text {tallest }}\right]=\underbrace{(0,+\infty) \cap\left[2^{\prime \prime}-\varepsilon, 2^{\prime \prime}+\varepsilon\right]}_{I_{\text {Diff }}:[\text { about } 2 \text { inches } \ldots \text {-.er } \mathbb{\rrbracket}}] \\
& \Leftrightarrow \operatorname{HEIGHT}(\text { Lucy }) \subseteq\left[d_{\text {tallest }}+2^{\prime \prime}-\varepsilon, d_{\text {shortest }}+2^{\prime \prime}+\varepsilon\right] \\
& \left(\text { defined when } d_{\text {tallest }}+2^{\prime \prime}-\varepsilon \leq d_{\text {shortest }}+2^{\prime \prime}+\varepsilon\right)
\end{aligned}
$$

（51）【Lucy is much taller than every boy（is） 1 』

$$
\begin{aligned}
& \Leftrightarrow \operatorname{HEIGHT}(\text { Lucy }) \subseteq \iota I[I-\left[d_{\text {shortest }}, d_{\text {tallest }}\right]=\underbrace{(0,+\infty) \cap\left[d_{\text {DIFF-Pos }}^{c},+\infty\right)}_{I_{\text {DIFF }}: \mathbb{I m u c h} \ldots \text {-.er } \mathbb{~}}] \\
& \Leftrightarrow \operatorname{HEIGHT}(\text { Lucy }) \subseteq\left[d_{\text {tallest }}+d_{\text {DIFF-Pos }}^{c},+\infty\right)
\end{aligned}
$$

The default positive interval $\llbracket$－er】can also be modified by an operator like little．As shown in（52），Little turns a positive interval into a negative one． Thus as illustrated in（53），when a comparative contains less，$I_{\text {DIFF }}$ is negative． Eventually，（53）means that Lucy＇s height is below that of the shortest boy．
（52）Little takes a positive interval $I$ as input and outputs $[0,0]-I$ ．

$$
\text { E.g., } \llbracket \operatorname{less} \rrbracket=\operatorname{LITTLE}(\llbracket-\mathrm{er} \rrbracket)=[0,0]-(0, \infty)=(-\infty, 0)
$$

（53）【Lucy is less tall than every boy（is）tall】

$$
\begin{aligned}
& \Leftrightarrow \operatorname{HEIGHT}(\text { Lucy }) \subseteq \iota I[I-\left[d_{\text {shortest }}, d_{\text {tallest }}\right]=\underbrace{(-\infty, 0)}_{I_{\text {DIFF }}: \llbracket \text { less } \rrbracket}] \\
& \Leftrightarrow \operatorname{HEIGHT}(\text { Lucy }) \subseteq\left(-\infty, d_{\text {shortest }}\right)
\end{aligned}
$$

Comparatives based on the use of a gradable adjective like short can be derived in a similar way，as illustrated in $(54-56) .{ }^{12}$

12．Comparatives with a gradable like short are somehow special with regard to eval－ uativity．As illustrated in（i），different from equative sentence（i－a）and the＇less short＇
（54）【Chloe is shorter than every boy（is）tall】
$\Leftrightarrow \operatorname{HEIGHT}($ Chloe $) \subseteq \iota I[\left[d_{\text {shortest }}, d_{\text {tallest }}\right]-I=\underbrace{(0,+\infty)}_{I_{\text {DIFF }} \mathbb{I} \text {－er } \rrbracket}]$
$\Leftrightarrow \operatorname{HEIGHT}($ Chloe $) \subseteq\left(-\infty, d_{\text {shortest }}\right)$
No evaluativity
（i．e．，Chloe is shorter than the shortest boy）
（55）【Chloe is at most 2 inches shorter than every boy（is）tall】
$\Leftrightarrow \operatorname{HEIGHT}($ Chloe $) \subseteq \iota I[\left[d_{\text {shortest }}, d_{\text {tallest }}\right]-I=\underbrace{(0,+\infty) \cap\left(-\infty, 2^{\prime \prime}\right]}_{I_{\text {DIFF }}: \llbracket \text { at most } 2 \text { inches ．．．－er } \rrbracket}]$
$\Leftrightarrow \operatorname{HEIGHT}($ Chloe $) \subseteq\left[d_{\text {tallest }}-2^{\prime \prime}, d_{\text {shortest }}\right)$
No evaluativity
（defined when $d_{\text {tallest }}-2^{\prime \prime}<d_{\text {shortest }}$ ）
（i．e．，Chloe is shorter than every boy，but the difference is at most $2^{\prime \prime}$ ）
（56）【Chloe is less short than every boy（is）short』
$\Leftrightarrow \operatorname{HEIGHT}($ Chloe $) \subseteq \iota I[\left[d_{\text {shortest }}, d_{\text {tallest }}\right]-I=\underbrace{(-\infty, 0)}_{I_{\text {DIFF }}: \llbracket \text { less } \rrbracket}]$
$\Leftrightarrow \operatorname{HEIGHT}($ Chloe $) \subseteq\left(d_{\text {tallest }},+\infty\right)$
Evaluativity
（i．e．，everyone is short，but Chloe is taller than the boys）
sentence（i－c），the sentence with shorter，（i－b），does not have evaluativity．We do not have a firm answer yet，but only a guess．
It is likely that for（i－a）／（i－c），【as Ann is】and 【than Ann is】contain an elided short， thus their meaning inherits the evaluativity of the degree question how short is Ann．

However，for（i－b），it seems possible that 【than Ann is】，which eventually denotes the position standing for $\operatorname{HEIGHT}(\mathrm{Ann})$ along a height scale，contains an elided tall，and thus【than Ann is】 corresponds to the degree question how tall is Ann and has no evaluativity （see（ii）and Büring 2007 for more discussion on this possibility）．
（i）a．Chloe is as short as Ann is．
$\vDash$ Chloe is short $\wedge$ Ann is short
$\checkmark$ evaluativity
b．Chloe is shorter than Ann is．
$\notin$ Chloe is short $\vee$ Ann is short
（similar to（54／55）
No evaluativity！
c．Chloe is less short than Ann is．
（similar to（56））
$\models$ Chloe is short $\wedge$ Ann is short
$\checkmark$ evaluativity
（ii）Unfortunately，the ladder was shorter than the house was high．
（Büring 2007：（2a））

To sum up this section, all uses of gradable adjectives convey the meaning of comparison, and the meaning of comparison is mainly expressed via (i) the direction of subtraction and (ii) the non-negativeness of the difference.

## 4 English -er/more vs. another

Having shown how gradable adjectives take the responsibility of conducting comparison, we now show that English morpheme -er/more works like additive particle (an)other, denoting a positive difference, i.e., an increase. $\S 4.1$ shows the parallelism between -er/more and (an)other. $\S 4.2$ presents a unified account for various uses of -er/more. $\S 4.3$ discusses the anaphoricity of -er/more.

### 4.1 Parallelism between -er/more and another

As noted by Greenberg (2010) and Thomas (2010), more has an additive use similar to another. As illustrated in (57), both more and another denote an increase on a base item in the domain of entities. The most natural interpretation of (57c) is that more denotes an amount (of chocolate) above zero, which can but does not necessarily exceed the amount of two bars (the base amount).
(57) Increase in the domain of entities: Additive use
a. I ate $\underbrace{\mathrm{an}^{x} \text { apple }}_{\text {base item }}$. Then I ate $\underbrace{\text { another }^{y} \text { (apple). Across sentences }}_{\text {increase }}$
b. $\underbrace{A^{x} \text { girl }}_{\text {base item }}$, Sue, met $\underbrace{\text { another }^{y} \text { girl }}_{\text {increase }}$, Mary. Within the same sentence
c. I ate $\underbrace{\text { two }^{x} \text { bars of chocolate. }}_{\text {base item }}$. Then I ate (a bit) $\underbrace{\text { more }^{y}}_{\text {increase }}$.

We can adopt the same additivity-based perspective in understanding the use of -er/more in comparatives. In (58), more denotes an increase on a base item in the domain of scalar values: moving a lower value for some distance (i.e., an increase conveyed by $\llbracket-\mathrm{er} /$ more $\rrbracket$ ) results in a higher value.
(58) Increase in the domain of scalar values: Comparative use
a. $\underbrace{\text { Mary is tall. Sue is tall } \underbrace{\text { er }}_{\text {increase }} .}_{\text {base item: HEIGHT(Mary) }}$ Across sentences
b．Sue is tall $\underbrace{\text { er }}_{\text {increase }} \underbrace{\text { than Mary is tall．}}_{\begin{array}{c}\text { base item：} \\ \text { HEIGHT（Mary）}\end{array}}$ ．
Thus as shown in（59）and（60），【－er／more】and 【another』 have parallel semantics：denoting an increase（i．e．，a positive difference，cf．the non－negative interval argument $I_{\text {DIFF }}$ in the lexical semantics of gradable adjectives，see（24） and（25）），based on a salient base item in the context．
（59）$\llbracket-\mathrm{er} / \mathrm{more} /(\mathrm{an})$ other】（In the domain of intervals：$\llbracket-\mathrm{er} /$ more $\rrbracket$ def $(0,+\infty))$
a．denotes an increase in the domain of entities or scalar values
b．presuppose there is a salient base that the increase is anaphoric to
（60）The parallelism between the domains of entities and intervals

| Domain | Indefinites | Definites | Additive words | Additivity＋Restriction |
| :--- | :--- | :--- | :--- | :--- |
| $D_{e}$ | someone | Mary | （a）other | another girl，Mary |
| $D_{\langle d t\rangle}$ | some（amount） | 3 feet | －er／more | 3 feet ．．．－er／more |

As additive particles，－er／more and another are also parallel in passing the classical tests for presupposition triggers（see also Zhang \＆Ling 2021 and §4．3）．

## （61）Tests of projection

a．It is possible that another girl came．
b．It is possible that more alcohol was consumed．
Additive use
c．It is possible that Lucy is taller．

## Comparative use

## （62）Tests of local satisfaction

a．Either Mary was not there，or another girl gave a talk．
b．Either they didn＇t have a beer，or more alcohol was consumed．
c．Either Mary is not that tall，or she is taller．

## 4．2 Various uses of－er／more

The correlative use of－er／more，as illustrated in（63）and Fig．4，means a cor－ relation between changes along two dimensions．When the two changes are in the


Fig. 4: Correlation between increases along two dimensions: The more you read, the more you learn.


Fig. 5: Accumulating increases: Lucy is taller and taller.
same direction (i.e., two increases), the correlation is positive (see (63a)). When the two changes are in opposition direction (i.e., an increase and a decrease), the correlation is negative (see (63b) with a sketched analysis).

## (63) Correlative

a. The more you read, the more you learn.
(see Fig. 4)
b. The taller you are, the less mobile and quick you are.
$\approx$ the answer to the degree question ' $\lambda I_{\mathrm{DIFF}} \cdot \operatorname{HEIGHT}(x) \subseteq \iota I\left[I-I_{\mathrm{STDD}}=\right.$ $\left.I_{\text {DIFF }}\right]$ ' determines the answers to the questions ' $\lambda I_{\text {DIFF. }}$ MOBILITY $(x) \subseteq$ $\iota I\left[I_{\mathrm{STDD}}^{\prime}-I=I_{\mathrm{DIFF}}\right]^{\prime}$ and ' $\lambda I_{\mathrm{DIFF} . \operatorname{SPEED}}(x) \subseteq \iota I\left[I_{\mathrm{STDD}}^{\prime \prime}-I=I_{\mathrm{DIFF}}\right]$ '

Multi-head comparatives (see e.g., von Stechow 1984, Zhang 2023b) like (64) can be considered a further extension of the correlative use of -er/more. ${ }^{13}$ (64) expresses a change of the gradient of the correlation: how wealth distribution is more tilted than in the past (see Zhang 2023b for a detailed discussion).
(64) Fewer people own more of the overall wealth, and fewer companies own more market share.

Multi-head comparative
The repetitive use of -er/more involves a series of conjunction, expressing a series of increases. As illustrated in Fig. 5, (65b) means that there are accumulated increases along a height scale, leading to higher and higher position values: from $I_{\text {STDD }}$ to $I_{\text {STDD }}^{\prime}$ to HEIGHT(Lucy).

## (65) Repetitive use of -er/more

a. Janice had a little lamb and another and another and another.
13. (64) is from https://www.deseret.com/opinion/2020/9/14/21436415/guest-opinion-america-capitalism-strengths-dark-side-too-far-inequality-divisiveness-wealth-gap.
b. Lucy is tall $\underbrace{\text { er }}_{I_{\text {DIFF }}}$ and tall $\underbrace{\mathbf{e r}}_{I_{\text {DIFF }}^{\prime}}$

$$
\Leftrightarrow \operatorname{HEIGHT}(\text { Lucy }) \subseteq \iota I[I-\underbrace{I_{\mathrm{DTDP}}^{\prime}}_{\substack{I_{\mathrm{STDD}}^{\prime} \subseteq \iota I\left[I-I_{\mathrm{STDD}}^{\prime}=I_{\mathrm{DIFF}}^{\prime}\right]}}=I_{\mathrm{DFF}}^{\prime}]
$$

Additive particles like -er/more and another can also be used along with universal quantifiers, meaning the accumulation of increases (i.e., the effect is similar to a series of conjunctions, see Bumford 2015). (66) means that along with a timeline, there is a gradual accumulation along a scale of book quality $\mu$ (see (66a)) or an accumulation of stories (see (66b)).
(66) a. Every year Mary wrote a more interesting book. (Bumford 2015) $\approx \forall N \exists I_{\text {IDFF }}\left[\mu(\right.$ book-of-year $N) \subseteq \iota I\left[I-\mu(\right.$ book-of-year $\left.\left.N-1)=I_{\text {DIFF }}\right]\right]$ $\rightsquigarrow$ Towards higher and higher positions along a scale of book quality
b. Everyday there is another story to write. $\rightsquigarrow$ Accumulating stories $\approx \forall N \exists x[$ stories-by-day $N$ - stories-by-day $(N-1)=x]$

### 4.3 The anaphoricity of -er/more

The above discussion reveals a distinction between the additive use (see (57) and the use of another in (65) and (66)) and the comparative use (see (58)).

For the comparative use, an increase is a distance along a scale, and the increase is anaphoric to a base item that is a position along the scale.

On the other hand, for the additive use, both an increase and the base item the increase is anaphoric to are the same kind of things (e.g., in (57c), both the base item $x$ and the increase $y$ denote chocolate).

The theory of QUD (Question under discussion, see Roberts 1996/2012) provides a unified perspective on the anaphoricity of these additive particles (see Beaver \& Clark 2009, Thomas 2011, Zhang \& Ling 2021 for a similar view). For both the additive and comparative use, the increase is anaphoric to a discoursesalient, positive, non-overlap partial answer to the Current Question (CQ), leading to increased informativeness than the partial answer.

In a domain of entities, a positive, partial answer is in a part-whole relation to the complete answer. The lack of a positive partial answer means the lack of a salient base item that can support the additive use of more (see (67b)).
(67) Current question (CQ): What did you eat?
a. I ate $\underbrace{\text { two bars of chocolate }}_{\text {base item: }}$. Then I ate (a bit) $\underbrace{\text { more }}_{\text {increase }} . \quad(=(57 \mathrm{c}))$

[^8]b\# I didn't eat a bar of chocolate. Then I ate more.
In a domain of scalar values, a partial answer indicates a position that addresses the CQ in a less informative way than a complete answer. Thus for gradable adjectives like tall, a partial answer denotes a position lower than the complete answer along a scale; while for short, a partial answer denotes a position higher than the complete answer along a height scale.
(68)

$\begin{gathered}\text { base item - a partial answer } \\ \text { to the CQ: HEIGHT(Mary) }\end{gathered}$ Mary is not tall. Sue is tall $\underbrace{\text { er }}_{\text {increase }} . \quad$ CQ: how tall is Sue?

This QUD-based view on the anaphoricity of -er/more explains an observation about incomplete comparatives, comparatives without an overt thanpart (see Sheldon 1945, Schwarzschild 2010, Li 2023 for relevant discussion).

As illustrated in (69), when a than-phrase is overtly present, the comparison standard can be a degree expression like 6 feet (see (69a)) or an anaphora referring back to a degree (see (69b)). However, in an incomplete comparative like $(69 \mathrm{c} / 69 \mathrm{~d})$, only the measurement of a counterpart to the target, here HEIGHT(Mary), but not a degree expression, can play the role of standard.

Under the current analysis, -er needs to be anaphoric to a discourse-salient position along a height scale. When there is a than-phrase/clause, this thanexpression plays the role of $I_{\text {STDD }}$ (see §3.6), satisfying the anaphoricity requirement of -er. However, for incomplete comparatives like ( $69 \mathrm{c} / 69 \mathrm{~d}$ ), only HEIGHT(Mary) can be a discourse-salient position, playing the role of $I_{\text {STDD }}$. In (69c), the degree expression 6 feet actually denotes the distance between HEIGHT(Mary) and the zero point (see §3.3). In (69d), presumably, the contextual threshold of being tall lacks discourse salience.
a. Lucy is taller than 6 feet. $\quad \operatorname{HEIGHT}($ Lucy $) \subset\left[6^{\prime},+\infty\right)$
b. Mary is not $6^{u}$ feet tall. Lucy is taller than that. $\operatorname{HT}(\mathrm{L}) \subset\left[6^{\prime},+\infty\right)$
c. Mary is not 6 feet tall. Lucy is taller.

$$
\begin{aligned}
& \rightsquigarrow \text { HEIGHT }(\text { Lucy }) \subseteq \iota I[I-\operatorname{HEIGHT}(\text { Mary })=(0,+\infty)] \\
& \nsim \operatorname{HEIGHT}(\text { Lucy }) \subset\left[6^{\prime},+\infty\right)
\end{aligned}
$$

d. Mary is not POS tall. Lucy is taller.

$$
\begin{aligned}
& \rightsquigarrow \operatorname{HEIGHT}(\text { Lucy }) \subseteq \iota I[I-\operatorname{HEIGHT}(\text { Mary })=(0,+\infty)] \\
& \nsim \operatorname{HEIGHT}(\text { Lucy }) \subset\left[d_{\text {PoS }}^{c},+\infty\right)
\end{aligned}
$$

## 5 Comparison in Chinese and the use of gèng

This section extends the above analysis of comparison to languages without morphemes like English -er/more. $\S 5.1$ addresses how comparison is expressed by gradable adjectives in Chinese. We propose that while in English, gradable adjectives essentially encode a non-strict inequality (see §3: (24) and Table (30)), in -er-less languages like Chinese, gradable adjectives encode a strict inequality, making a morpheme like -er/more unnecessary. §5.2 addresses the use of Chinese gèng and Japanese motto, morphemes often used in comparatives, and shows that these morphemes work like additive particle moreover, indicating an enhanced level of positiveness (i.e., increased informativeness in the positive use). $\S 5.3$ compares gèng with hái, another additive particle in Chinese.

### 5.1 Comparison and gradable adjectives in Chinese

Similar to English gradable adjectives (see (24) and (25) in §3.1), the lexical semantics of Chinese gradable adjectives can also be characterized as a subtraction relation among three scalar values, as shown in (70) and (71).

However, we propose that there is a crucial difference between English tall/short and Chinese gāo/ǎi. As shown in $(24 / 25)$, the meaning of English gradable adjectives includes a non-negative presupposition. Thus, English gradable adjectives essentially encode a non-strict inequality: the measurement of the target reaches $I_{\text {STDD }}$. In comparatives (see §3.6), comparative morpheme -er/more brings a positive scalar value, $(0,+\infty)$, leading to strict inequality.

On the other hand, as shown in (70/71), the meaning of Chinese gradable adjectives includes a positive presupposition. Thus, Chinese gradable adjectives essentially encode a strict inequality: the measurement of the target exceeds $I_{\text {STDD }}$. As a consequence, $I_{\text {DIFF }}$ is positive by default and does not need a morpheme like English -er/more for expressing strict inequality.

$$
\begin{equation*}
\llbracket g a \bar{o} \rrbracket \stackrel{\text { def }}{=} \lambda I_{\mathrm{DIFF}} \cdot \lambda I_{\mathrm{STDD}} \cdot \lambda x \cdot \underbrace{I_{\mathrm{DIFF}} \subseteq(0,+\infty)}_{\text {positive presupposition (cf. (24)) }} \operatorname{HEIGHT}(x) \subseteq \iota I\left[I-I_{\mathrm{STDD}}=I_{\mathrm{DIFF}}\right] \tag{70}
\end{equation*}
$$

$$
\begin{equation*}
\llbracket \text { ǎi } \rrbracket \stackrel{\text { def }}{=} \lambda I_{\mathrm{DIFF}} \cdot \lambda I_{\mathrm{STDD}} \cdot \lambda x \cdot \underbrace{I_{\mathrm{DIFF}} \subseteq(0,+\infty)}_{\text {positive presupposition (cf. (25)) }} \operatorname{HGHT}(x) \subseteq \iota I\left[I_{\mathrm{STDD}}-I=I_{\mathrm{DIFF}}\right] \tag{71}
\end{equation*}
$$

Various uses of Chinese gradable adjectives are summarized in (72) and largely parallel to English phenomena (see (30) and §3). ${ }^{14}$

| Various uses of gradable adjectives in Chinese |  |  |
| :--- | :--- | :--- |
|  | $I_{\text {STDD }}$ | $I_{\mathrm{DIFF}}$ |
| Positive use | Contextual threshold: <br> $\left[d_{\mathrm{POS}}^{c}, d_{\mathrm{POS}}^{c}\right]$ | $(0,+\infty)$ <br> (or further restricted <br> by a modifier like hěn) |
| Measure constructions | Absolute zero point: | restricted by a <br> measure phrase |
| [0,0] | Contextual threshold <br> or absolute zero point | (interval abstraction) |
| bǐ-comparatives questions | Measurement of the <br> standard: bǐ-phrase | $(0,+\infty)$ <br> (or further restricted by a <br> numerical differential) |
|  |  |  |

The positive use addresses a comparison with a context dependent threshold. Thus as illustrated in (73), the difference argument $I_{\text {DIFF }}$ is the default positive interval, $(0,+\infty)$, while the standard argument $I_{\text {STDD }}$ is a context-dependent threshold of being tall or short.

Under the current analysis, there is a subtle difference between the positive use in English and Chinese. In English, being tall means reaching the threshold $d_{\text {DIFF }}^{c}$ (see (31)), while in Chinese, being tall means exceeding $d_{\text {DIFF }}^{c}$ (see (73a)). However, given that neither the threshold $d_{\text {STDD }}^{c}$ is overtly expressed nor the difference $[0,+\infty)$ or $(0,+\infty)$ has an overt numerical restriction, this distinction between 'reaching' and 'exceeding' does not apparently affect truth conditions.

## (73) Positive use in Chinese

a. Wǒ hěn gāo.

$$
1 \mathrm{SG} \text { very tall }
$$

'I am tall.'

$$
\begin{aligned}
& \llbracket(73 \mathrm{a}) \rrbracket \Leftrightarrow \operatorname{HEIGHT}(\mathrm{me}) \subseteq \iota I\left[I-\left[d_{\mathrm{POS}}^{c}, d_{\mathrm{POS}}^{c}\right]=(0,+\infty)\right] \\
& \quad \Leftrightarrow \operatorname{HEIGHT}(\mathrm{me}) \subseteq\left(d_{\mathrm{POS}}^{c},+\infty\right) \\
& \text { (i.e., my height exceeds the contextual threshold of being tall) } \\
& \left(\text { cf. } \llbracket(31) \rrbracket \Leftrightarrow \operatorname{HEIGHT}(\text { Lucy }) \subseteq\left[d_{\mathrm{POS}}^{c},+\infty\right)\right)
\end{aligned}
$$

[^9]b. Tā hěn ǎi.

3SG very short
'She is short.'

$$
\begin{aligned}
\llbracket(73 \mathrm{~b}) \rrbracket & \Leftrightarrow \operatorname{HEIGHT}(\mathrm{she}) \subseteq \iota\left[\left[\left[d_{\mathrm{POS}}^{c}, d_{\mathrm{POS}}^{c}\right]-I=(0,+\infty)\right]\right. \\
& \Leftrightarrow \operatorname{HEIGHT}(\mathrm{she}) \subseteq\left(-\infty, d_{\mathrm{POS}}^{c}\right)
\end{aligned}
$$

(i.e., her height is below the contextual threshold of being short)

The measurement construction addresses a comparison with a zero point. Thus as illustrated in (74), the difference argument $I_{\text {DIFF }}$ is expressed via the numerical measurement (e.g., 1.7 m ), while the standard argument $I_{\text {STDD }}$ is the zero point along a height scale. The semantic derivation of (74a) and the ungrammaticality of (74b) are exactly parallel with English data (see §3.3).
(74) Measurement constructions in Chinese (see also Zhang 2019 and Zhang 2023a (Section 2.1) for more patterns)
a. Lèlè (yǒu) yì-mǐ-q̄̄ gāo.

Lèlè EXIST one-meter-seven tall
'Lèlè is 1.7 m tall.'

$$
\begin{aligned}
\llbracket(74 \mathrm{a}) \rrbracket & \Leftrightarrow \operatorname{HEIGHT}(\text { Lèlè }) \subseteq \iota I[I-[0,0]=[1.7 \mathrm{~m},+\infty)] \\
& \Leftrightarrow \operatorname{HEIGHT}(\text { Lèlè }) \subseteq[1.7 \mathrm{~m},+\infty)
\end{aligned}
$$

(i.e., Lèlè's height reaches $1.7 \mathrm{~m} \rightsquigarrow$ the 'at least' reading as in (39a))
b. * Mǐmǐ (yǒu) yì-mǐ-wǔ ǎi.

Mǐmǐ EXIST one-meter-five short
Intended: 'Lèlè is (as short as) 1.5 m .'
$\rightsquigarrow[0,0]-\operatorname{HEIGHT}$ (Mǐmǐ) is negative (see also Fig. 2 and (40))
Degree questions address a comparison relative to a reference position: e.g., a zero point or a context-dependent threshold, seen in (75). Thus, just like in English (see §3.4), degree questions in Chinese involve an abstraction of the difference variable $I_{\text {DIFF }}$ and denote a set of intervals: a set of distances relative to a reference position.

When $I_{\text {STDD }}$ is the context-dependent threshold of being tall/short, there is evaluativity in interpreting the degree question. When $I_{\text {STDD }}$ is the zero point (only for gradable adjectives like tall, but not for short), there is no evaluativity.

Like in English, Ans $_{\text {diff }}$ (see (43)) can be applied to return the most informative interval $I_{\text {DIFF }}$. Two type-shifters, Position-M (see (44), for gradable adjectives like tall/gāo) and Position-S (see (45), for gradable adjectives like short/ǎi), can be applied to compute the position of the target from its distance away from the reference position $I_{\text {STDD }}$ (i.e., $[0,0]$ or $\left[d_{\mathrm{POS}}^{c}, d_{\mathrm{POS}}^{c}\right]$, see Fig. 3).

## Degree questions in Chinese

a. Lèlè (yǒu) duó gāo?

Lèlè ExIST how-much tall
'How tall is Lèlè?' With or without evaluativity (see (41)) $\llbracket(75 \mathrm{a}) \rrbracket \Leftrightarrow \lambda I_{\mathrm{DIFF}}$. HEIGHT(Lèlè) $\subseteq \iota I\left[I-I_{\mathrm{STDD}}=I_{\mathrm{DIFF}}\right]$
b. Mǐmǐ (yǒu) duó ǎi?

Mǐmǐ EXIST how-much short
'How short is Mǐmı̌?' With evaluativity (see (42))
$\llbracket(75 \mathrm{~b}) \rrbracket \Leftrightarrow \lambda I_{\mathrm{DIFF}} \cdot \mathrm{HEIGHT}\left(\mathrm{Mǐmǐ)} \subseteq \iota I\left[I_{\mathrm{STDD}}-I=I_{\mathrm{DIFF}}\right]\right.$
In Chinese $b \check{\imath}$-comparatives, the difference argument $I_{\mathrm{DIFF}}$ is the default positive interval, $(0,+\infty)$, which can further get restricted by a numerical differential (see (76)). The standard $I_{\text {STDD }}$ is provided by the $b \check{\imath}$-phrase, i.e., a position along a relevant scale that addresses the measurement of the comparison standard. ${ }^{15}$
(76) Comparatives in Chinese
a. Lèlè bǐ Mǐmǐ gāo (wǔ límǐ)

Lè̀è STDD Mǐmǐ taller five centimeter
'Lèlè is ( 5 cm ) taller than Mǐmǐ.'
$\llbracket(76 \mathrm{a}) \rrbracket \Leftrightarrow \operatorname{HEIGHT}($ Lèlè $) \subseteq \iota I[I-\operatorname{HEIGHT}($ Mǐmǐ $)=(0,+\infty) \cap[5 \mathrm{~cm},+\infty)]$
b. Mǐmǐ bǐ Lèlè ǎi (wǔ límǐ).

Mǐmǐ STDD Lèlè short five centimeter
'Mǐmǐ is ( 5 cm ) shorter than Lèlè.'
$\llbracket(76 \mathrm{~b}) \rrbracket \Leftrightarrow \operatorname{HEIGHT}($ Mǐmǐ $) \subseteq \iota I[\operatorname{HEIGHT}($ Lèlè $)-I=(0,+\infty) \cap[5 \mathrm{~cm},+\infty)]$

### 5.2 The use of Chinese gèng (and Japanese motto)

We have shown that in languages like Chinese and Japanese, comparatives do not require the use of a morpheme like English -er/more (see §5.1 and (7b/8b)).

However, in Chinese and Japanese, comparatives can contain a sometimes optional morpheme. In Japanese comparatives, motto can be optionally inserted before a predicative (see (77)) or an attributive gradable adjective (see (78)).

[^10](77) Rika-wa Makoto-yori (motto) taka-i.

Rika-TOP Makoto-STDD MOREOVER tall-PRES
'Rika is taller than Makoto.' (cf. (8b): without motto)
(78) Mary-wa John-yori (motto) takusan-no ronbun-o kaita. Mary-TOP John-StDD MOREOVER many-GEN paper-ACC wrote 'Mary wrote more papers than John.' (Beck, Oda \& Sugisaki 2004: (1))

In Chinese comparatives, gèng is optional before a predicative gradable adjective (see (79)), while it is required before an attributive one (see 80)).
(79) Lèlè bǐ Mǐmǐ (gèng) gāo.

Lèlè STDD Mǐmǐ moreover tall
'Lèlè is taller than Mǐmǐ.' (cf. (7b/76a): without gèng)
(80) Lèlè bǐ Mǐmǐ mǎi-le *(gèng) duō de shū.

Lèlè stdd Mǐmǐ buy-ASP moreover many relz book
'Lèlè bought more books than Mǐmǐ.' (gèng: required for an attributive)
The literature on Chinese gèng and Japanese motto notes three distinctions between these morphemes and English -er/more.

First, the interpretation of comparatives with the presence of gèng/motto seems to involve evaluativity. According to Beck, Oda \& Sugisaki (2004), with the presence of motto, (77) means that Rika is even taller than Makoto, i.e., there is an evaluative meaning that Makoto already exceeds the threshold of being tall. Similarly, according to Liu (2010) and Chen (2023), with the presence of gèng, (79) suggests that Mǐmǐ is tall.

Second, as pointed by Beck, Oda \& Sugisaki (2004), Ma (2019), and Zhang (2023a), the use of Chinese gèng / Japanese motto in comparatives is incompatible with the presence of a numerical differential, as illustrated in $(81) /(82)$.

It is worth noting that English even is actually compatible with the overt presence of a numerical differential in a comparative, as indicated by the corresponding English sentences in $(81) /(82)$.
(81) *Rika-wa Makoto-yori motto go senti se-ga taka-i. Rika-TOP Makoto-Stdd moreover five centimeter back-nom tall-pres Intended: 'Rika is even 5 cm taller than Makoto.' (cf. (8b/77))


Fig. 6: 【Lèlè bǐ Mǐmǐ gèng gāo】: compared with Mǐmǐ, Lè̀è is tall (see (87a)).
$(82)$ *Lèlè bǐ Mǐmǐ gèng gāo wǔ líimǐ.
Lèlè STDD Mǐmǐ moreover taller five cm
Intended: 'Lèlè is even 5 cm taller than Mǐmǐ.'
(cf. (76a/79))
Third, as pointed out by Chen (2023), Chinese gèng has an additive use. Example (83) involves no overt use of gradable adjectives at all. ${ }^{16}$
(83) Jīnqián mǎi-bú-dào yǒu-yì, gèng mǎi-bú-dào àiqíng money buy-NEG-get friendship MOREOVER buy-NEG-get love 'Money cannot buy friendship. Moreover, it cannot buy love.'

Thus, comparatives with Chinese gèng or Japanese motto are reminiscent of English implicit comparison (see (84)) and sentences with moreover (see (85)).

Implicit comparison like (84) is essentially a positive use (see $\S 3.2$ ), meaning that (even) compared with a contextually enhanced threshold of being tall, Lucy's height still reaches this new threshold. Similarly, the use of moreover in (85) suggests that chaos indicates a new level of how the situation is bad.
a. (Even) compared to Mary, Lucy is tall. Implicit (= (21a))
b. Compared to Mary, Lucy is still tall. Implicit comparison $\rightsquigarrow$ Lucy's height reaches a threshold that Mary's height doesn't.
(85) War brings depression. Moreover, it brings chaos.
$\rightsquigarrow$ Chaos reaches a badness level that depression doesn't.
Based on the above observations, we propose that gèng/motto are additive particles of the type of also/even/still/moreover, operating on a prejacent proposition and addressing the connection between the prejacent and alternatives.

Specifically, as shown in (86), $\llbracket$ gèng $/ \operatorname{motto} \rrbracket(p)$ (i) asserts their prejacent $p$ and (ii) presupposes the existence of a contextual threshold with enhanced positiveness (i.e., increased informativeness) that $p$ exceeds but alternatives don't.

[^11]
## 【gèng／motto】（ $p$ ）

a．asserts the prejacent $p$
b．presupposes that the prejacent $p$ and alternatives are associated with scalar values on a scale，and compared with alternatives，$p$ exceeds a positive level that alternatives don＇t（see Fig．6）

As sketched out in（87）and illustrated in Fig．6，a Chinese bǐ－comparative with gèng（i）presupposes a contextual threshold of being tall／short，$I_{\mathrm{POS}}^{c_{\text {＞}}^{\text {нr（Mǐmi）}}}$ （or $I_{\text {POS }}^{\left.c_{\text {＜hr }}^{\text {Lèlè }}\right)}$ ），which exceeds the informativeness level indicated by the height of the comparison standard for being tall／short，and（ii）asserts that the mea－ surement of the target further exceeds this threshold $I_{\text {POS }}^{c>\operatorname{mi}(\text { Mimi })}$（or $I_{\text {POS }}^{c<\operatorname{Hr}(\text { Lèle })}$ ）．

$$
\begin{align*}
& \text { a. 【Lèlè bǐ Mǐmǐ gèng gāo】 }  \tag{87}\\
& \approx \text { Compared with Mǐmǐ, } \\
& (=(79), \text { see Fig. 6) } \\
& \underbrace{\text { Lèlè is tall }} \\
& \text { prejacent of gèng, associated with an enhanced threshold } \\
& \left.\approx \operatorname{HEIGHT}(\text { Lèlè }) \subseteq \iota I\left[I-I_{\mathrm{POS}}^{c_{>\text {HT(Mǐmi) }}^{\text {( }}}=(0,+\infty)\right]\right) \\
& \text { (here } \left.I_{\mathrm{POS}}^{c>\text { нT(Mîmi) }} \subseteq \iota I[I-\operatorname{HEIGHT}(\text { Mǐmĭ })=(0,+\infty)]\right) \\
& \text { i.e., the contextual threshold of being tall is above HEIGHT(Mǐmǐ), } \\
& \text { and HEIGHT(Lèlè) is above this threshold } I_{\mathrm{POS}}^{c_{\text {>hr (Mími) }}} \\
& \text { b. 【Mǐmǐ bǐ Lèlè gèng ǎi } \rrbracket \\
& \approx \text { Compared with Lèlè, is short } \\
& \left.\approx \operatorname{HEIGHT}(\text { Mǐmǐ }) \subseteq \iota\left[I I_{\text {POS }}^{c} c_{\text {нrt(Lè̀è })}-I=(0,+\infty)\right]\right) \\
& \text { (here } \left.I_{\mathrm{POS}}^{c_{\text {人Hf(Lè̀è }}} \subseteq \iota I[\operatorname{HEIGHT}(\text { Lèlè })-I=(0,+\infty)]\right) \\
& \text { i.e., the contextual threshold of being short is below HEIGHT(Lèlè), } \\
& \text { and HEIGHT(Mǐmǐ) is below this threshold } I_{\text {POS }}^{c_{\text {<rr }}} \text { (Lèlè) }
\end{align*}
$$

The proposal in（86）is apparently similar to an implementation of the canonical analysis，as illustrated in（88）（see also（18b）in §2．1）．However，there is a crucial difference．In（88），degrees which the target＇s measurement reaches but the standard doesn＇t are not necessarily considered contextual thresholds of being tall．Thus the interpretation of（88）does not involve evaluativity：it might be the case that neither Lucy nor Mary is tall．

In contrast，the interpretation of（87）（see also Fig．6）involves evaluativity： the target＇s measurement exceeds a contextual threshold of being tall，and it is even an enhanced threshold．In other words，in（87），Lèlè is definitely tall．

【Lucy is taller than Mary is】 （see（18b））
$\Leftrightarrow \exists d[d \in\{d \mid$ Lucy is $d$－tall $\} \wedge d \notin\{d \mid$ Mary is $d$－tall $\}]$
i．e．，there is a height $d$ that Lucy＇s height reaches but Mary＇s height doesn＇t

The proposal in (86) naturally explains our intuitions on the use of gèng.
First, including gèng/motto often seems semantically optional, without apparently affecting truth conditions. This is because, under the current proposal, gèng/motto affects the threshold $d_{\text {POS }}^{c}$ and enhances it to a higher value, but this kind of threshold is never overtly expressed in natural language anyway.

Second, the current proposal explains the seeming evaluativity in interpreting gèng-sentences. In (87a) and Fig. 6, given that the target's measurement exceeds an enhanced threshold, it naturally follows that Lèlè is tall.

However, the reported evaluative meaning for the standard (here Mǐmǐ is tall for (87a)) is an implicature, rather than a presupposition, as evidence by the cancellability shown in (89) (cf. Liu 2010, Chen 2023).
(89) Lèlè bǐ Mǐmǐ gèng gāo, dāngrán, Mǐmǐ bú suàn gāo.

Lèlè stdd Mǐmǐ moreover tall of-course Mǐmǐ NEG count tall
'Lèlè is taller than Mǐmǐ, but of course, Mǐmı̌ cannot be considered tall.'
(90) is a naturally occurring example found on the internet. ${ }^{17}$ The most natural interpretation of (90) is that the speaker wants to become taller, i.e., above a contextual threshold that is above his current height (which is quite low). It is likely that the speaker would be satisfied with an average height. In this sense, alternatives to the prejacent of gèng play the role of 'anchor', affecting the positive threshold (see also discussion on implicit comparison (21)).
(90) Zhǎng-de hěn ǎi, zěnyàng cái kěyǐ biàn-de gèng gāo? grow-LNK very short, how only can become-LNK MOREOVER tall 'I am short, and how can I become taller?'

Similarly, the evaluative meaning is also cancelable for Japanese motto:
(91) Rika-wa Makoto-yori motto takusan-no ronbun-o kai-ta. Rika-TOP Makoto-StDD MOREOVER many-GEN paper-ACC write-PST Shikashi Makoto-ga sore-hodo takusan-no ronbun-o kai-ta but Makoto-NOM that-degree many-NO paper-ACC write-PST wake-de-wa-nai
meaning-COP-TOP-NEG.
'Rika wrote even more papers than Makoto, but it doesn't mean that Makoto wrote so many papers.' (Toshiko Oda: personal communication)
17. (90): https://www.chunyuyisheng.com/pc/qa/0bqUEp80ZHyf_qHw8yoXtg/

It is worth noting that in Chinese, an attributive expression with a comparative meaning (e.g., a longer novel, more books in (80)) requires the presence of gèng. For a sentence like (80), the presence of gèng is legitimate even if Mǐmǐ only bought one book. Thus gèng does not bring an evaluative presupposition. ${ }^{18}$

Third, under the current proposal, the prejacent of gèng (see (87)) actually involves the positive use of a gradable adjective: for (87a), Lèlè is tall. Thus the incompatibility of gèng/motto with a numerical differential (see $(81 / 82)$ ) is also naturally accounted for. A contextual threshold for the positive use is never overt in natural language. Consequently, the positive use is never compatible with a specific numerical differential (see also the tables in (30) and (72)).

However, just like degree modifiers like very / a bit can be used to vaguely characterize how the measurement of the target is above the contextual threshold (i.e., the size of $I_{\mathrm{DIFF}}$ ) in the positive use (e.g., Jessica is very tall, see (37/38)), the use of gèng is compatible with degree modifiers like yì-diǎn (see (92)).
(92) a. Lèlè bǐ Mǐmǐ gèng gāo yì-diǎn.

Lèlè STDD Mǐmǐ MOROVER tall one-bit
'Lèlè is a bit taller than Mǐmǐ.'
b. gèng shèng yì-chóu

MOREOVER be.better one-tally
'a bit better'

Fourth, by analyzing gèng along with additive particles like moreover, the current proposal also explains the additive use of gèng like (83) (see (93)).
(93) a. Money cannot buy friendship. Moreover, it cannot buy love. ( $\approx(83)$ )
b. War brings depression. Moreover, it brings chaos. $\quad(=(85))$

We assume that the additive use of gèng/moreover in (93) is based on the accommodation of a contextually relevant scale: e.g., the measurement of price for (93a), how bad the situation is for (93b) (see Greenberg 2018, Zhang 2022 for a similar idea in analyzing English even, another additive particle). Roughly speaking, (93a) (i) presupposes a contextual threshold that is above the price of friendship and (ii) asserts that the price of love is above this threshold. (93b) (i)

[^12]presupposes a contextual threshold that is above the badness of depression and (ii) asserts that the badness of chaos is above this threshold.

As an additive particle similar to even/moreover, gèng can appear at a syntactically higher position in a bř-comparative, leading to an additive use dubbed 'multiple degree comparatives', as illustrated in (94) (see also Kennedy \& McNally 2005b). (94) means that the height difference between Lèlè and Mǐmǐ exceeds a contextual threshold of height difference. Depending on the stress position, the prejacent of gèng has two different sets of alternatives: the one associated with the standard (see (94a)) or the target (see (94b)).
(94) Lèlè gèng bǐ Mǐmǐ gāo.

Lèlè moreover stdd Mǐmǐ tall
'Lèlè is taller to Mǐmǐ by more.'
a. Shared Standard Interpretation (stress on Lèlè):

Someone is taller than Mǐmǐ. Moreover, Lèlè is taller than Mǐmǐ. Height ordering (from low to high): Mǐmǐ, someone, Lèlè
b. Shared Target Interpretation (stress on Mǐmǔ):

Lèlè is taller than someone. Moreover, Lèlè is taller than Mǐmǐ. Height ordering (from low to high): Mǐmǐ, someone, Lèlè

In these examples of additive use (see (93/94)), the prejacent of gèng/more and alternatives are in two distinct sentences, in contrast with comparatives with gèng (see e.g., (79/87)), where the prejacent part and its alternative appear within the same sentence. Actually for the additive use, a single-sentence construction is also possible (see (95/96)). (96) shows a slight difference between two standard markers: bǐ (see (96a)) vs. bǐq̌̌ (see 96b).
(95) Bǐqǐ yǒu-yì, jīnqián gèng mǎi-bú-dào àiqíng compared-to friendship money MOREOVER buy-NEG-get love 'Money cannot buy friendship. Moreover, it cannot buy love.' (see (83))
(96) a. Lèlè bǐ Bōbō (gèng) bǐ Mǐmǐ gāo. Lèlè STdD Bōbō MOREOVER STDD Mǐmǐ tall $\checkmark$ Shared Standard: B is taller than M. Moreover, L is taller than M. \#Shared Target: L is taller than B. Moreover, L is taller than M.
b. Lèlè bǐqǐ Bōbō gèng bǐ Mǐmǐ gāo.
$\checkmark$ Shared Standard: B is taller than M. Moreover, L is taller than M. $\checkmark$ Shared Target: L is taller than B. Moreover, L is taller than M.

Finally, the use of gèng also supports a series of additive computation. (97) means that every year, his height exceeds a threshold of being tall, which exceeds his height in the previous year.
(97) tā yì nián bǐ yì nián gèng gāo.

3SG one year STDD one year MOREOVER tall
'He is taller every year.'
Comparative
$\approx$ his-height-in-year $N \subseteq \iota I[I-\underbrace{I_{\mathrm{POS}}^{C_{>\text {нT( }}(N-1)}}=(0,+\infty)]$

$$
I_{\mathrm{POS}}^{C_{>\mathrm{Hr}(N-1)} \subseteq \iota I[I-[\text { his-height-in-year }(N-1)]=(0,+\infty)]}
$$

### 5.3 Chinese gèng vs. Chinese hái

In addition to gèng, Chinese comparatives can also contain other additive particles, such as hái. As illustrated in (98), the use of gèng and hái has a similar effect, and both sentences can be translated as 'Lèlè is even taller than Mimǐ.'. ${ }^{19}$
a. Lèlè bǐ Mǐmǐ gèng gāo.

Lèlè STDD Mǐmǐ moreover tall
'Lèlè is even taller than Mimǐ.'
b. Lèlè bǐ Mǐmǐ hái gāo.

Lèlè stdd Mǐmǐ still tall
'Lèlè is even taller than Mimǐ.'

Ma (2019) points out two distinctions between gèng and hái. First, as illustrated in (99), only the use of hái (see (99a)), but not the use of gèng (see (99b)), is compatible with the presence of a numerical differential.
(99) a. Lèlè bǐ Mǐmǐ hái gāo wǔ límǐ.

Lèlè stdd Mǐmǐ still tall five centemeter
'Lèlè is even 5 cm taller than Mimǐ.'

[^13]

Fig．7：【Lèlè bǐ Mǐmǐ hái gāo（ 5 cm ）】：Lèlè is even（ 5 cm ）taller than Mǐmǐ．（see（102））

## b．＊Lèlè bǐ Mǐmǐ gèng gāo wǔ límǐ．

Lèlè STDD Mǐmǐ moreover tall five centemeter
Intended：＇Lèlè is 5 cm taller than Mimǐ．＇

Second，as illustrated in（100），only the use of hái（see（100a）），but not the use of gèng（see（100b）），is felicitous for a comparison with metaphorical or hyperbolic meaning．
（100）a．Lèlè bǐ shīzi hái yǒnggǎn．
Lèlè STDD lion sTiLL brave
＇Lèlè is even braver than lions．＇
b．\＃Lèlè bǐ shīzi gèng yǒnggǎn．
Lèlè STDD lion MOREOVER brave
Intended：＇Lèlè is braver than lions．＇
Given these distinctions，we propose that Chinese hái has a meaning simi－ lar to English even（see Greenberg 2018，Zhang 2022）．As shown in（101）and illustrated in Fig．7，it is the use of hái（rather than gèng）that brings an evalu－ ative presupposition：both the prejacent and alternatives exceed the contextual threshold for the positive use．
（101）【hái】 $(p)$
a．asserts the prejacent $p$
b．presupposes that both the prejacent and alternatives exceeds a con－ textual positive level along a scale，while the prejacent further exceeds alternatives（see Fig．7）
$\rightsquigarrow$ in a comparative，both the target and the standard exceed $I_{\text {POS }}^{c}$
Our analysis of gèng（see（86））and hái（see（101））naturally explains the two observations of Ma （2019）．

In a comparative with the use of hái（see Fig．7），the target（here HEIGHT（Lèlè））is compared with the standard（here HEIGHT（Mǐmǐ）），not with a contextual threshold $I_{\text {POS }}^{c}$ ．In other words，the prejacent of hái is a genuine com－ parative，not a positive use（cf．（87））．Thus it is possible to include a numerical differential to specify the value of height difference．
(102) $\llbracket(99 a) \rrbracket \approx$ Compared with Mǐmǐ, HÁt Lèlè is 5 cm taller. (i.e., compared with Mǐmǐ, Lèlè is even 5 cm taller)

Then for a comparison to convey metaphorical or hyperbolic meaning (see (100)), it is crucial that the comparison standard should already exceeds the threshold for the positive use. Thus naturally, as shown by the contrast between Fig. 6 and Fig. 7, hái, but not gèng, satisfies this requirement.

## 6 Discussion and conclusion

In this paper, by zooming into the components of comparison (i.e., the target, the standard, and their difference), we have demonstrated a new perspective on cross-linguistic universals and variation on comparison expressions. We have shown that comparison is universally performed by gradable adjectives. Gradable adjectives like tall and short differ with regard to their direction. Languages with vs. without morphemes like -er/more differ with regard to whether gradable adjectives encode, by default, the meaning of non-strict vs. strict inequality.

Based on this understanding of comparison, we have discussed the semantic contribution of cross-linguistic particles used in comparatives, focusing on English -er/more and Chinese gèng. We analyze them as two kinds of additive particles: (i) English -er/more is similar to another, while (ii) Chinese gèng is similar to moreover. Thus the current work also connects the notion of scalarity (or comparison along a scale with ordering) with the notion of additivity.

Our current work suggests a few new directions for further investigation.
First, to account for cross-linguistic variation, we need to consider parameters both at the language level and at a more fine-grained construction level.

Beck (2009) (see also Beck, Oda \& Sugisaki 2004), a pioneering work on cross-linguistic variation of comparatives, collects data from 14 languages and proposes that with regard to expressing comparison, languages vary along three parameters: (i) whether ontologically, there are degrees; (ii) whether there can be a lambda abstraction over a degree variable; (iii) whether a degree argument can be overtly observed for a gradable adjective.

In this paper, we have shown that even within the same language, there is construction-level variation, and constructions in different languages can share universals. For example, English implicit and explicit comparison (see (20) and (21)) differ with regard to whether an overt degree argument that represents a difference (i.e., a numerical differential) can be observed. On the other hand, English implicit comparison and Chinexe bǐ-comparatives with gèng are parallel in making a comparison with a contextually relevant positive threshold.

Evidently, in the same language, different constructions often co-exist, based on different ontological assumptions and showing parametric variation.

Second, the connection between scalarity and additivity provides a new perspective on many linguistic phenomena. Traditionally, (i) the investigation of comparatives and scalarity in a domain of scalar values and (ii) the investigation of additive particles like also/even in a domain of entities are separate. In analyzing English -er/more as well as Chinese gèng / Japanese motto, we have shown the connection between scalarity and additivity (see also Greenberg 2018, Zhang 2022's analysis of English even).

Scalarity/additivity-related phenomena share similar patterns with regard to anaphoriity and informativeness. Presumably, these phenomena all involve an anaphoricity between some base item and an increase, and increase is essentially towards increased informativeness.

A further issue is that human languages have a vast variety of addtivity effects. As shown in this paper, English -er/more is similar to another, working on a DP level, in a domain of entities or scalar values. Chinese gèng and Japanese motto are similar to English moreover (as well as also/even/still), working at a propositional level. The variation among addtive particles and across languages provides a rich empirical ground for linguistic investigation.

For example, according to Heim's (1991) 'maximize presupposition', which requires an over marking of presuppositional meaning, the presence of additive particles is often obligatory if their existential presuppositional requirement is satisfied. However, as illustrated in (103/104), it seems that English and Chinese differ with regard to which additive particles are obligatory or optional.

## (103) English: (an)other is obligatorily required; also is optional

a. *A girl came. A girl also came.
b. A girl came. Another girl (also) came.
(also: optional)
(104) Chinese: again is obligatory; (an)other is optional lái-le yí-gè rén, yòu lái-le (lìng)-yí-gè rén. come-ASP one-CL person again come-ASP (other)-one-CL person 'A person came. Another person also came'

Finally, along the discussion, we have skipped over many issues which require to be analyzed at the syntax-semantics interface. In particular, the distinction between predicative vs. attributive comparatives in Chinese (see e.g., (79/80)) and their different requirement on the presence of gèng require another paper for a thorough discussion.

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[^0]:    1. Special abbreviations used in the gloss: COP=copula, LNK=linker, POSS=possession marker, $\mathrm{Q}=$ interrogative marker, $\mathrm{RELZ}=$ relativizer, $\mathrm{STDD}=$ standard marker.
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[^2]:    2. In (7), we use a minimal pair of yes/no questions to illustrate the positive and comparative use of gradable adjective $g \bar{a} o(' t a l l(e r)$ '), because in Chinese, a declarative positive use (e.g., Lucy is tall) involves additional complication, which is orthogonal to this paper (see e.g., Zhang 2023a (Sections 2.1 and 2.2) and Grano 2012 for discussion).
[^3]:    3．We can use a type shifter to bridge（12a）and（12b）：$\lambda G_{\langle e d\rangle} \cdot \lambda d \cdot \lambda x \cdot G(x) \geq d$ ．
    4．The use of capital letters is to indicate lack of phonology，following Kayne（2005b）．

[^4]:    5．Here（17）is a clausal comparatives，which is arguably distinct from phrasal compar－ atives（see e．g．，Larson 1988，Schwarzchild \＆Wilkinson 2002 for more discussion）．
    6．Adjustments are needed for comparatives with a numerical differential，e．g．，
    （i）$\llbracket$－er $\xlongequal{=} \stackrel{\text { def }}{=} \lambda d \cdot \lambda D_{1} \cdot \lambda D_{2} \cdot \operatorname{MAX}\left(D_{2}\right) \geq \operatorname{mAx}\left(D_{1}\right)+d$ ．
    （including a differential argument $d$ for（18a））

[^5]:    9. The $w h$-word for degree in Chinese is $d u o ́ / d u \bar{o}$, which is segmentally identical to the adjective $d u \bar{o}$ 'many/much'. Arguably $d u o ́ / d u \bar{o}$ modifies the adjective indirectly with a silent NUMBER/AMOUNT mediating in between (see Kayne 2005a).
[^6]:    10．According to the canonical analysis，e．g．，Kennedy and McNally（2005a），Section 6．2： ＇Roughly speaking，the difference between，for example，expensive and very expensive is

[^7]:    11. According to their formal properties and what mathematical operations they support, scales can be divided into four levels: nominal scales, ordinal scales (equipped with an ordering), interval scales (equipped with an ordering and a unit that supports the measurement of differences), and ratio scales (equipped with an ordering, a unit, and an absolute zero point) (see Stevens 1946). Obviously, measurement constructions require the existence of a zero point, i.e., a ratio scale. See Sassoon (2010) and Zhang \& Ling (2021) for discussion on how this 4-level distinction of scales is relevant to natural language.
[^8]:    a partial answer to the CQ

[^9]:    14. Chinese has several constructions to express equatives, which involve extra complications orthogonal to the current paper (see Zhang 2020, 2023a (Section 2.4) for discussion).
[^10]:    15. In addition to $b \check{\text {-comparatives, Chinese has other types of comparative constructions }}$ (see Zhang 2023a (Sections 2.3 and 4)). There has been a debate on whehter Chinese bǐ-comparatives are phrasal or clausal comparatives. We tend to agree with Lin 2022's view that bǐ-comparatives are phrasal comparatives (also see Zhang 2023a (Section 4)).
[^11]:    16. This additive use in (83) is distinct from the additive use of more in (57c) in $\S 4.1$. In $(57 \mathrm{c})$, in more (chocolate), more is actually much+-er, i.e., the gradable adjective here is much. In more intelligent / beautiful, more is an allomorph of -er.
[^12]:    18. Although in Chinese, the presence of gèng is required in an attributive comparative like (80), the case of Japanese motto is different. For a Japanese attributive comparative like (78), the presence of motto is optional. We do not know how to explain this difference between Chinese and Japanese data at this moment, so this issue is left for future work.
[^13]:    19. In the existing literature on Chinese gèng, Liu (2010) claims that gèng has an evaluative presuppositon (e.g., (98a) presupposes that the comparison standard, Mǐmǐ, is already tall), while Chen (2023) analyzes gèng along with English even. It seems to us that due to the meaning similarity between (98a) and (98b), their analysis actually works for hái, rather than gèng. A detailed comparison among theories is for another occasion.
