

Sense as sampling propensity *

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Abstract Both individuals and predicates can be referred to in different ways which carry different senses or connotations. Despite this being discussed since at least Frege, it poses a deep problem to standard extensional semantics. For example, as discussed by Jennifer Saul, “Clark Kent went into the phone booth and Superman came out” means something different than “Superman went into the phone booth and Clark Kent came out”. I introduce a novel way of modelling these kinds of semantic phenomena using Sampling Propensity (Icard 2016). The idea is that the basic atoms of semantic calculus are generated from a set of potential candidates using a generative cognitive procedure. This sampling procedure is also at play with common nouns in generic sentences like “lions have manes” or “mosquitoes carry malaria”. Crucially, it can distinguish co-extensional nouns like ‘drink’ and ‘beverage’, which occasionally yield different truth values in the same kinds of generic sentences. The account includes a fully formalised compositional system in which individual concepts and category concepts are modeled as an extension linked with a sampling propensity and where some propositions are evaluated by continually sampling exemplars from a concept. The sampling approach also links competence and performance where finite sampling yields performance and sampling repeatedly converges on competence. This approach also has ramifications for quantification, particularly the generic “flavour” of non-partitive ‘all’.

Keywords: concepts, generics, individuals, proper names, sampling propensity, sense, connotation

1 Introduction

It is little news to any of us that the name that you call something can matter a great deal. An author may agonise over a choice between two words which ostensibly refer to the same thing yet carry very different connotations. This extends well beyond writing; if I tell my

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friend that I know a place that serves great *beverages*, they will likely conclude that those things will be very different than if I had referred to the very same beverages as *drinks*. The former brings to mind cold refreshment, a Coca-Cola or an iced tea and the latter, perhaps a glass of Cabernet or a Guinness. Crucially though, there is no drink which is not a beverage nor any beverage which is not a drink.

Despite the words denoting the same things, (1) seems true while (2) seems somewhat inappropriate or false. Furthermore, this is far from an idiosyncrasy of “drink/beverage”, the same phenomenon occurs with “food/comestible” in (3).

- (1) a. Drinks are consumed in bars.
- b. Beverages are consumed in fast-food restaurants.
- (2) a. ? Beverages are consumed in bars.
- b. ? Drinks are consumed in fast-food restaurants.
- (3) a. French people love food.
- b. ? French people love comestibles.

This isn't exclusive to common nouns. Proper names carry sometimes massively different connotations too. As Saul (1997) has pointed out, alter-egos can provide a difficult muddle to standard semantic views. One can know Superman *is* Clark Kent and yet (4a) simply means something different than (4b) and while (5a) seems true, (5b) seems false.

- (4) a. Clark Kent went into the phone-booth and Superman came out.
- b. Superman went into the phone-booth and Clark Kent came out.
- (5) a. Clark Kent is mild-mannered journalist.
- b. # Superman is a mild-mannered journalist.

With proper names, it is not restricted to only alter-egos or fiction either: Augustus was the first emperor of Rome and Octavian was a member of the Second Triumvirate and yet they are one and the same individual. Nevertheless, any historian worth their salt will be exceedingly careful in whether they refer to that individual as Augustus or Octavian as they convey different connotations.

These phenomena pose a problem to standard model-theoretic semantics. If a common noun denotes a set, then under standard assumptions, ‘drink’ and ‘beverage’ have identical interpretations, $\llbracket \text{drink} \rrbracket = \llbracket \text{beverage} \rrbracket$. One might think that intensions which map from worlds to sets might provide us a way out, but they can't solve the ‘drink’/‘beverage’ puzzle since all drinks are beverages and vice versa in every possible world. ‘Superman’ and ‘Clark Kent’ pose a possibly even more troublesome problem for standard semantics; they both rigidly designate the same individual: $\llbracket \text{Superman} \rrbracket = \llbracket \text{Clark Kent} \rrbracket = s$.

It's easy to see why these multiple modes of reference are troubling for traditional semantics: if $\llbracket \text{Superman} \rrbracket = s$ and $\llbracket \text{Clark Kent} \rrbracket = \llbracket \text{Superman} \rrbracket$, then we should be able to substitute

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Clark Kent for Superman and vice-versa *salva veritate*. Problems of this sort have been well-known since Frege (1892) and were later expanded on by Kripke (1979) and various solutions have been proposed to aspects of the problem (e.g. Aloni's Conceptual Covers). However, these solutions generally interpret the problem as a matter of mistaken beliefs, incomplete information or alternative possible worlds: we can handle the fact that Lois Lane **thinks** that Clark Kent isn't Superman because of the opaque context. What makes Saul's version of the problem so important, however, is that examples like (4) and (5) do not involve ignorance or opaque contexts—one can be perfectly aware that Superman *is* Clark Kent and yet distinguish (4a) and (4b). Furthermore, it can't be solely attributed to different times being associated with the different terms: (6) describes a situation where Clark Kent/Superman might be speaking as Clark Kent while dressed as Superman (even these prepositional phrases need explaining).

(6) Clark Kent answered the phone while looking into the mirror at Superman.

This paper proposes a semantic theory which addresses the issues with both nouns like 'drink'/'beverage' and proper names like 'Superman'/'Clark Kent' with a shared mechanism. The view is that there is some extra content which helps determines the connotations of words and additionally, phenomena like those in (1-5). Crucially, this content determines aspects of meaning which don't derive exclusively from external facts and which relate to modes of reference. For example, this extra content provides the "default generalisations" that some argue is the origin of genericity (Leslie 2008). Likewise, it provides the kinds of default assumptions which lead us to think of different scenarios when one says 'Clark Kent' as opposed to 'Superman'. This extra content provides the *sense* of a word, and it does so by using something called a *sampling propensity* (Icard 2016).

2 Sampling propensities and concepts

Sampling propensity boils down to the idea that we *sample* from an underlying generative procedure and then evaluate things on the basis of the outcomes of that sampling process (Icard 2016). For example, causal modelling is handled under the sampling-propensity approach by predicting that people can simulate a causal system and see the outcome, but cannot just read-off probabilities that govern that simulation directly (Icard, Kominsky & Knobe 2017).

Sampling propensities can be formalised using probability distributions over extensions but I want to make it quite clear that the view is not committed in any way to the idea that probability distributions themselves are represented in the mind. The idea is that the mind is a generative machine and is capable of coming up with exemplars of a concept when necessary. Some members may come quickly to mind, and some may take a very long time and some may essentially never be considered. For example, some beverages come to mind quickly and immediately (e.g. Coca-Cola) and others perhaps less quickly (e.g. New England switchel). We can describe which members come to mind using a probability distribution,

but this doesn't mean that the underlying generative procedure is directly represented as probabilities (nor does it say whether the procedure involves randomness at all).

One concrete consequence of sampling propensities is that while we formalise using probabilities, at no point in the semantics can we directly access probabilities. In other words, we have a big button that says "sample" on it, but we have no way of knowing beforehand which things will be sampled and with what probability.

The specific view proposed in this paper has at its core four parts:

- Concepts are represented as a tuple which is a conceptual extension and a sampling propensity which defines a probability distribution for which examples will be sampled from a concept.
- The conceptual extension is an *internalist* notion which is the set of *potential* atoms (*e*-type objects) which belong to a concept, not the actual, real-world set.
- Individuals are represented with concepts and their conceptual extensions consist of the potential atoms which could be the actual individual.
- Generic sentences and the basic predication of individuals function in similar ways, by sampling from the sampling propensity for a concept.

My approach uses sampling propensity to explain how one applies predicates. For example, when I say "beverages are nice on a hot day", I conjure up in my mind exemplars of cold beverages and use them to evaluate the underlying proposition, i.e. whether those sampled exemplars of beverages happen to be nice on a hot day. This procedure is not restricted to common nouns like "drink", but also applies to individuals. When I evaluate "Superman is a mild-mannered journalist", I don't simply evaluate the proposition for a single unitary Superman representation, rather, I consider a swathe of Superman exemplars and determine whether I think it is true on the basis of the Superman exemplars I happen to sample. So rather than directly accessing objects of type *e* or $\langle e, t \rangle$ when applying a predicate, we sample exemplars or *atoms* (e.g. *e*-type objects) from an extension to evaluate a proposition.

While extension naturally means the actual referents of a concept, this formalism is deeply internalist and when I use extension, I use it to mean the things that *would* be classified as a member of that concept by the mind in question, *not* the actual real-world referents. This notion of extension could be modeled, for example, as a manifold (Gardenfors 2004; Goodale 2022). If the mind encodes members of a concept as a manifold, that means that there are uncountably many atoms (e.g. points on the manifold or *e*-type objects) which are a member of the "extension" of the concept. While the formalism in this paper is agnostic as to the nature of conceptual extensions (beyond that they are sets of atoms), a manifold provides a nice example of the kinds of structures which are appropriate for modelling conceptual extensions.

A sampling propensity, then, is something that takes us from the conceptual extension to *members* of that extension; it samples from the extension. Crucially, the sampling propensity is a distinct part of the concept which is independent of the extension of a concept. So, two

concepts like ‘drink’ and ‘beverage’ may share the same extension *but are likely to sample different things* because they have different sampling propensities.

When I think of a drink, I’ll think of wine and when I think of a beverage, I’ll think of Coca-Cola, because, while the two concepts have the same set of members, different members are likely to be sampled. This means that concepts are (at least) bipartite; they consist of a set of members *and* a sampling propensity over those members.¹ ‘Drink’ and ‘beverage’ have the same extension but happen to have different sampling propensities, giving rise to a different connotations.

Sampling propensities also are *not* beliefs about frequency nor are they directly determined by frequencies in personal experience during learning, they are simply what comes to mind, regardless of whatever facts there are about frequency of a concept or perceived frequency of a concept. An archaeological dig might draw to mind the discoveries of great treasures like King Tut’s tomb, even if one is perfectly aware that the vast majority of archaeological digs find broken potsherds at best. Indeed, if we model a conceptual extension as a manifold, there may be uncountably many members of a concept, but of course, no one believes there are uncountably many lions in the world (they may believe that there are uncountably many *potential* lions however). When one samples from a conceptual extension, they are not sampling *actual* lions, they are sampling lion atoms which might exist. As such, their sampling propensity will be affected by all sorts of different factors beyond their beliefs about actual frequency. For example, there has been much ado about “striking” generics (Leslie 2007), such as “mosquitoes carry malaria”. While very few mosquitoes carry malaria, the generic is true: under the sampling-propensity view, this is because people will more quickly think of mosquitoes which carry malaria than other mosquitoes when sampling. The reason for this is likely to be that it is a useful generalisation to keep oneself safe, but it could just as well be the result of a cultural stereotype about mosquitoes or many other things. What is crucial is that it is *not* because we believe a large number of mosquitoes carry malaria, it is because we *think* of mosquitoes who carry malaria when we think of mosquitoes. This sampling propensity is simply part of the meaning of a concept and are acquired in a way that is just as mysterious as the way that extensions are acquired.

Now, an observant reader may be concerned about how this approach handles quantification if we start discussing “uncountably many lions” but have no fear, no quantified babies are thrown out with the bathwater here. The formalism models individual concepts (e.g. ‘Clark-Kent’ or ‘Superman’) with the same ontological structure as category concepts. The concepts for individuals are also bipartite consisting of a *set* of that individual in different contexts/times/possibilities for that individual *and* a sampling propensity over those potential individuals. So, to evaluate a predicate for a given individual concept, we *also* sample atoms rather than directly applying a predicate to the individual concept.

Thinking of Superman will draw to mind leaping tall buildings in a single bound whereas

¹ Indeed, others have proposed that concepts need multiple independent parts (Putnam 1975; Del Pinal 2015, 2016). I give an account principally of connotation and extension, while leaving other major aspects of conceptual structure open (e.g. similarity).

Clark Kent will lead one to think of mild-mannered journalism. Nevertheless, since Superman *is* Clark Kent, any of these exemplars sampled from either Superman or Clark Kent must necessarily be in both the set of potential Supermen and the set of potential Clark-Kents. Superman and Clark Kent have the same set of members but different sampling propensities over those members, just like drink and beverage do.

Now, to quantify over a category concept, we simply need to quantify over the individual concepts whose extensions are subsets of the category concept's extension. So, when evaluating "mosquitoes carry malaria", we sample atoms directly and evaluate whether they carry malaria, whereas with "few mosquitoes carry malaria", we need to go over individual-concepts for mosquitoes and evaluate whether they carry malaria. As long as the individual-concepts mostly do not have malaria and the atoms mostly do, we can have "mosquitoes carry malaria" and "few mosquitoes carry malaria" both be true.

This formalism has a number of potential applications in semantic puzzles where modes of reference play a role. Beyond Saul's problem, it can provide a straightforward analysis of slurs (i.e. many theories of slurs argue they are co-extensional with the neutral referents for the same thing (Camp 2013; Jeshion 2013)), euphemisms (e.g. "urinate" and "piss" may draw to mind different scenarios) and circumlocutions (e.g. "kill" versus "cause to die" or "people with disabilities" versus "the handicapped"). While I will not expound on these applications, they show the potential power of the formalism at explaining many of the core issues of *sense* that remain outstanding in semantics.

The formalism also has other appealing properties. It is fully compositional and has a tight connection between idealised competence and the noisiness of performance thanks to the law of large numbers in repeated sampling. While this paper focuses exclusively on common nouns and individuals, the approach could be extended to other parts of language and thought. In particular, verbs, if analysed with a neo-Davidsonian event semantics, might be a possible avenue to extend the theory as this provides sampleable events.

2.1 Sampling drinks and beverages

A given concept for a common noun like \llbracket beverage \rrbracket is a tuple with two parts:

- i) A set of *e*-type objects which belong to a concept, including potential (i.e. not necessarily existing) members of a concept.
- ii) A propensity to sample atoms from that set.

I will give the precise formal details later on, but we can formalise the first part with our good old fashioned sets of atoms and the second with that ever-increasingly popular tool, probability distributions. These distinctions between the extension of a concept and its sampling propensity call for some notational clarification.

- i) The extension, written in boldface: **beverage**
- ii) The sampling propensity, written in sans-serif font: beverage

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So a concept like “beverage” is a tuple consisting of a set, **beverage**, and a probability distribution, beverage.

$$\llbracket \text{beverage} \rrbracket = \langle \mathbf{beverage}, \text{beverage} \rangle$$

Compositional rules extract either the extension or sampling propensity in the appropriate contexts. For example, the predicate “is a beverage” simply consists of the following (completely standard) interpretation:

$$\llbracket \text{is a beverage} \rrbracket = \lambda x. \mathbf{beverage}(x)$$

When used as a subject, “beverage” is a bit more complicated. When we say, “beverages are refreshing”, we need to sample the appropriate beverages. The fact this is a generic sentence is not incidental—sampling will turn out to have the strongest effect in generic sentences. To do this, we need to introduce a kind of quantifier that can map from sampling propensities to sets of type e which can then be quantified over. While the precise details of quantification in general will be handled later on, the first and most vital quasi-quantifier is μ .

$$\mu_{x \sim (\mathbf{beverage}, \text{beverage})} \llbracket \text{are refreshing} \rrbracket (x)$$

This operator takes an extension and a sampling propensity and samples from the extension according to the propensity. It then checks whether the predicate is true for those samples and determines the average truth-value. The number of exemplars we sample, N , is variable and increasing N corresponds to increasing mental effort or consideration. While this produces a fuzzy logic, it avoids the criticisms made by [Kamp \(1975\)](#) as shown later. Crucially, the different truth-values track confidence in a proposition; this is not a model of vagueness.

$$\begin{aligned} \mu_{x \sim (\mathbf{beverage}, \text{beverage})} \llbracket \text{are refreshing} \rrbracket (x) = \\ \frac{1}{N} \sum_1^N \llbracket \text{are refreshing} \rrbracket (\text{SAMPLE}(\langle \mathbf{beverage}, \text{beverage} \rangle)) \end{aligned}$$

As we increase N , the truth-value judgement will be more and more consistent as we converge, by the law of large numbers, on the expected value. This stochastic process of repeated sampling corresponds to an account of how to evaluate μ in practice. In other words, *in performance*, people’s evaluations are stochastic. Remember, the conceit of sampling propensities is that while we can sample, we cannot directly access probabilities. However, since the truth-value converges as N increases, we can also discuss what is needed *in competence* for μ . There, we define it in terms of the probability distribution directly (where $P(x \sim y)$ is the probability of sampling x from y):

$$\mu_{x \sim (\mathbf{beverage}, \text{beverage})} \llbracket \text{are refreshing} \rrbracket (x) = \sum_{x \in \mathbf{beverage}} P(x \sim \text{beverage}) \llbracket \text{are refreshing} \rrbracket (x)$$

This gives us a tight connection between performance and competence for μ where competence can be characterised as sampling in the limit.

One thing to recall here is that when we sample, we are not necessarily sampling actual beverages, rather just atoms that could be beverages. For example, under a conceptual-manifold view of concepts, we would be sampling points on the manifold that would be classified as beverages (and might correspondingly have subsymbolic features which make them refreshing). Crucially, since these atoms do not have a necessary connection to specific beverages, frequency plays no direct role in the evaluation of these propositions.

To return to our original problem of drinks and beverages, we can say that these two concepts have identical extensions (in bold) while having different sampling propensities (in sans-serif).

$$\mathbf{drink} = \mathbf{beverage} \quad \text{drink} \neq \text{beverage}$$

As a consequence, we can have the distinction in (1) and (2) by positing that $\llbracket \text{consumed in bars} \rrbracket$ is true for regions of high sampling-propensity for $\langle \mathbf{drink}, \text{drink} \rangle$ whereas it is false for regions of high-sampling propensity for $\langle \mathbf{beverage}, \text{beverage} \rangle$.

$$\mu_{x \sim \langle \mathbf{beverage}, \text{beverage} \rangle} \llbracket \text{consumed in bars} \rrbracket(x) < \mu_{x \sim \langle \mathbf{drink}, \text{drink} \rangle} \llbracket \text{consumed in bars} \rrbracket(x)$$

2.2 Fuzzy logic

Since we are averaging the truth value of the predicate across samples, we have a fuzzy logic, with continuum-many truth values between 0 and 1. Classical connectives are usually defined as follows in fuzzy logic:

$$\llbracket \neg \varphi \rrbracket = 1 - \llbracket \varphi \rrbracket \quad \llbracket \varphi \wedge \psi \rrbracket = \min(\llbracket \varphi \rrbracket, \llbracket \psi \rrbracket) \quad \llbracket \varphi \vee \psi \rrbracket = \max(\llbracket \varphi \rrbracket, \llbracket \psi \rrbracket)$$

It's important to note that these are not the only possible definitions of connectives for infinite-valued logic. There is a broad class of possible fuzzy logics, known as t-norm logics (Hájek 1998). One of these may turn out to be a better match for human cognition than the preceding definitions, but they are sufficient for our purposes here.

While in the early 70s, there was some interest in integrating fuzzy logic with natural language semantics (Lakoff 1973), criticisms from Kamp (1975) proved devastating to that endeavour. Despite aspects of his argument having later been criticised by Sauerland (2011), the conclusion against fuzzy logic is still widely accepted. Kamp and Sauerland both criticise fuzzy logic from the perspective of it being a potential analysis of vagueness in natural language. Even though the logic in my approach is fuzzy, it is not meant as an analysis of vagueness and is instead an analysis of something akin to the degree of belief in a proposition. Furthermore, only quantification can introduce fuzziness as atomic predicates remain bivalent.

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Kamp’s argument against fuzzy logic is relatively straightforward. If φ has a truth-value of 0.5, then $\varphi \wedge \neg\varphi$ must have a truth value of 0.5 since $\min(0.5, 0.5) = 0.5$ which Kamp deems “absurd” because “how could a logical contradiction be true to *any* degree?” (Kamp 1975: 131). It does seem troubling for $\varphi \wedge \neg\varphi$ to not be a contradiction, but under the fuzzy logic I have defined, it can still be a contradiction in certain contexts.²

Take a sentence like “Drinks are refreshing” and let us assume it has a truth value of 0.5. Recall, μ here takes a concept, $\langle \mathbf{drink}, \text{drink} \rangle$ and samples atoms from the extension, \mathbf{drink} using the sampling propensity, drink and returns the proportion of sampled atoms which are in the set defined by $\llbracket \text{are refreshing} \rrbracket$.

$$\begin{aligned} \llbracket \text{Drinks are refreshing} \rrbracket &= \mu_{x \sim \langle \mathbf{drink}, \text{drink} \rangle} \llbracket \text{are refreshing} \rrbracket(x) \\ &= \sum_{x \in \mathbf{drink}} P(x \sim \text{drink}) \llbracket \text{are refreshing} \rrbracket(x) \\ &= 0.5 \end{aligned}$$

If we take its negation, this will also have a truth value of 0.5.

$$\begin{aligned} \llbracket \text{Drinks are not refreshing} \rrbracket &= \mu_{x \sim \langle \mathbf{drink}, \text{drink} \rangle} \neg(\llbracket \text{are refreshing} \rrbracket(x)) \\ &= \sum_{x \in \mathbf{drink}} P(x \sim \text{drink}) (1 - \llbracket \text{are refreshing} \rrbracket(x)) \\ &= \sum_{x \in \mathbf{drink}} P(x \sim \text{drink}) - \sum_{x \in \mathbf{drink}} (x \sim \text{drink}) \llbracket \text{are refreshing} \rrbracket(x) \\ &= 1 - \sum_{x \in \mathbf{drink}} (x \sim \text{drink}) \llbracket \text{are refreshing} \rrbracket(x) \\ &= 0.5 \end{aligned}$$

However, the conjunction of the two predicates will lead to a contradiction:

$$\begin{aligned} \llbracket \begin{array}{l} \text{Drinks are refreshing} \\ \text{and not refreshing} \end{array} \rrbracket &= \mu_{x \sim \langle \mathbf{drink}, \text{drink} \rangle} \llbracket \text{are refreshing} \rrbracket(x) \wedge \neg \llbracket \text{are refreshing} \rrbracket(x) \\ &= \sum_{x \in \mathbf{drink}} P(x \sim \text{drink}) \min(\llbracket \text{are refreshing} \rrbracket(x), \\ &\hspace{15em} 1 - \llbracket \text{are refreshing} \rrbracket(x)) \\ &= \sum_{x \in \mathbf{drink}} P(x \sim \text{drink}) 0 \\ &\hspace{10em} (\text{Since } \llbracket \text{are refreshing} \rrbracket(x) \text{ is always 0 or 1}) \\ &= 0 \end{aligned}$$

² Experimentally, people will often judge this kind of “contradiction” as acceptable if the predicate is vague and it is a borderline case (Alxatib & Pelletier 2011; Serchuk, Hargreaves & Zach 2011; Ripley 2011).

This proves that formulae of the structure $\mu_{x \sim \langle \mathbf{P}, \mathbf{P} \rangle} (\varphi \wedge \neg \varphi)$ will necessarily be false. However, $(\mu_{x \sim \langle \mathbf{P}, \mathbf{P} \rangle} \varphi) \wedge \neg (\mu_{x \sim \langle \mathbf{P}, \mathbf{P} \rangle} \varphi)$ and $(\mu_{x \sim \langle \mathbf{P}, \mathbf{P} \rangle} \varphi) \wedge (\mu_{x \sim \langle \mathbf{P}, \mathbf{P} \rangle} \neg \varphi)$ may still be partially true depending on what we sample from $\langle \mathbf{P}, \mathbf{P} \rangle$. If, for the first $\langle \mathbf{P}, \mathbf{P} \rangle$, we happen to sample atoms for which $\varphi(x)$ is true and for the second occurrence of $\langle \mathbf{P}, \mathbf{P} \rangle$, we sample atoms for which $\varphi(x)$ is false, then both $(\mu_{x \sim \langle \mathbf{P}, \mathbf{P} \rangle} \varphi) \wedge \neg (\mu_{x \sim \langle \mathbf{P}, \mathbf{P} \rangle} \varphi)$ and $(\mu_{x \sim \langle \mathbf{P}, \mathbf{P} \rangle} \varphi) \wedge (\mu_{x \sim \langle \mathbf{P}, \mathbf{P} \rangle} \neg \varphi)$ will have truth values of 1.

This can be avoided if we assume that when we sample multiple times from a concept in a discourse, we re-use the atoms that were already sampled beforehand (in a manner vaguely reminiscent of assignment in dynamic semantics).

2.3 Prototypicality, sampling propensity and compositionality

My approach bears some relationship to proposals from psychology about concepts like prototype theory. My theory makes no claims as to how we classify things into concepts, merely that we have a set of atoms for a concept and a method to sample from that set. Sampling propensity corresponds quite closely to prototypicality—beer is a prototypical drink whereas Coke is a prototypical beverage, just as robins are quickly categorised as birds whereas penguins are not (Rosch 1975). In other words, something with high sampling propensity for a concept tends to be prototypical for that concept.

The relationship between generic sentences and prototypicality is not a novel one (Heyer 1985; Geurts 1985), but my approach provides a formal cashing out of this approach. One classic criticism of prototypical theories comes from Osherson & Smith (1981) who show that prototypical theories cannot account for compositional concepts such as ‘pet fish’ as there is no way to derive the prototype of pet fish from the distance to the prototypes of ‘pet’ and ‘fish’ nor is there a way to compose the “features” of both prototypes. Fodor & Lepore (1996); Fodor (2001) and Fodor (2008) claim this and other arguments show that while extensions may compose, prototypes do not compose.

The approach in this article preserves set extensions and so, at the very least, extensions are easy to put together into compositional concepts in a classical manner. Sampling propensities are more complicated. One simple possibility could be that the sampling propensity of a single concept is continually fed upwards as the extension is further restricted. On this view, ‘pet fish’ would consist of the intersection of ‘pet’ and ‘fish’ combined with the sampling propensity for ‘fish’.³ This would mean that we would sample from fish, but restricted to only the ones which are pets.

$$\llbracket \text{Pet fish} \rrbracket = \langle \lambda x. \mathbf{fish}(x) \wedge \mathbf{pet}(x), \text{fish} \rangle$$

This would mean for example, that “pet that is a fish” and “fish that is a pet” would also have different sampling propensities despite their identical extensions because in the former “pet”

³ Noun-noun compounds are another can of worms. For simplicity, here I assume there is just simple intersective modification

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is the base sampling propensity and in the later “fish” is the base sampling propensity.

$$\begin{aligned} \llbracket \text{pet that is a fish} \rrbracket &= \langle \mathbf{fish}(x) \wedge \mathbf{pet}(x), \text{pet} \rangle \\ \llbracket \text{fish that is a pet} \rrbracket &= \langle \mathbf{fish}(x) \wedge \mathbf{pet}(x), \text{fish} \rangle \end{aligned}$$

While this simplifying assumption is sufficient to illustrate how compositional concepts are possible in the system, it is almost certainly incomplete. Under this view, the ordering of the atoms of a concept are preserved through composition (i.e. we can only exclude members, we can’t change which members are more probable than others). So, in order for a goldfish to be a prototypical pet fish, the ordering of ‘pet fish’ (e.g. a pet goldfish is more likely than a pet salmon) would need to be already contained in the prototype of ‘fish’ (e.g. a non-pet salmon is more likely than a pet goldfish which is in turn more likely than a pet salmon).

This might be able to explain some compositional effects of prototypicality but it seems nigh certain that the modifiers of a complex concept ought to influence the sampling propensity of a concept beyond simple restriction. For example, people are likely to assume that Harvard-educated carpenters are idealistic despite neither the Harvard-educated nor carpenters being considered idealistic (Kunda, Miller & Claire 1990). Further work will need to look at how sampling propensities can be influenced by their modifiers. However, it will likely require actually looking inside the generative structure underlying a sampling propensity rather than treating it as a probabilistic black-box.

3 Individual concepts

The most unorthodox aspect to this approach is the treatment of individuals. Rather than treating ‘Superman’, ‘Augustus’ or ‘John’ as simple atoms (e.g. *e*-type objects), I treat them with the same structure as category concepts: a tuple of an extension and a sampling propensity. While it is naturally odd for an individual to have multiple atoms, it is in some sense analogous to a Stalnakerian context but relative to an individual rather than the set of all possible worlds. That is, while the set for an individual can contain multiple atoms with different properties, they are all candidates for the *actual* individual, just as the set of possible worlds should contain the actual world. Under this view, each atom in the set, **Superman**, would consist of another possible Superman who is compatible with our current knowledge and context. In other words, as we learn about an individual, we reduce the space of possible atoms that can be associated with them by making the set of atoms that refers to them smaller and smaller. Of course, the sampling propensity, Superman now samples from this set of potential individuals to find the ones most associated with the individual. As discussed above, sampling propensities do not represent frequencies but rather what comes to mind easily. So, when we’re sampling from an individual, it means that we’re considering the different possibilities associated with that individual. This is clearer in the case of individual concepts where the notion of “frequency” of a potential individual is incoherent.

Since we know that Superman *is* Clark Kent, they must have the same set of possible atoms. So, to sample from ‘Clark Kent’ means to be more likely to think of the Clark-Kent-y possibilities, namely that he’s working as a journalist or wearing glasses. Conversely, Superman is more likely to be saving the day and wearing a red-and-blue leotard. So, just as with ‘drink’/‘beverage’, we have identical extensions but differing sampling propensities.

$$\mathbf{Superman} = \mathbf{ClarkKent} \quad \text{Superman} \neq \text{ClarkKent}$$

Likewise, we can predict the distinction between (5a) and (5b).

- (5) a. Clark Kent is mild-mannered journalist.
 b. # Superman is a mild-mannered journalist.

This is due to a difference in the sampling propensities for Clark Kent and Superman.

$$\mu_{x \sim \langle \mathbf{ClarkKent}, \text{ClarkKent} \rangle} [\text{mild-mannered}] (x) > \mu_{x \sim \langle \mathbf{Superman}, \text{Superman} \rangle} [\text{mild-mannered}] (x)$$

Beyond the immediate proposition, different terms for the same individual can be used by speakers to convey different contexts. When I say ‘Clark Kent’ did something, my interlocutor will likely sample moments that are Clark-Kent-y (e.g. wearing glasses). As a result, I can convey a different context by using different terms since I am aware of the kinds of atoms that those terms draw to mind in the semantics. So, if I were to explain that Clark Kent/Superman was flying in the distance to someone who doesn’t see him, I would be more apt to use ‘Clark Kent’ if he were wearing a tie and glasses and more apt to use ‘Superman’ if he were dressed in a leotard. This is because my interlocutor will sample different atoms depending on which term is used.

Likewise, different definite descriptions can also change connotations: ‘the villain’ will draw to mind very different things than ‘the man’. We can model this using an iota operator which takes the sampling propensity from its definite description and its extension from the individual concept which satisfies it (see 5.3 for full formal details).

$$\iota(\langle \mathbf{villain}, \text{villain} \rangle) = \langle \mathbf{John}, \text{villain} \rangle \quad \iota(\langle \mathbf{man}, \text{man} \rangle) = \langle \mathbf{John}, \text{man} \rangle$$

As a result, the different definite descriptions which pick out the same individual will draw to mind different atoms belonging to that individual, allowing us to convey different modes of presentation for the same individual simply by changing our definite description.

4 Quantification

Our individuals and categories have identical ontological structure: they are sets of atoms paired with a sampling propensity. This requires revamping how we handle quantification. While this is different from standard first-order logic approaches, the compositional story is largely compatible with traditional generalised quantifier approaches.

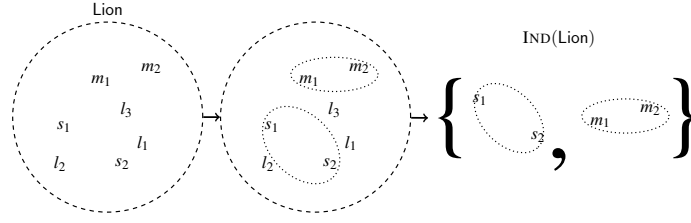


Figure 1 IND extracts the sampling propensities for two lion individual concepts, s and m , while ignoring l_1 , l_2 , and l_3 which are potential lion atoms that aren't a member of any individual concept.

In essence, rather than quantifying over atoms (e -type objects), we quantify over *individual concepts*. This requires that we keep track of which concepts are category concepts and which are individual concepts. We can do this by “tagging” concepts as category or individual concepts.

This also means we have to think about how individuals and atoms are counted. Say we have a model with two lions, named Simba and Mufasa. They both could have several atoms consisting of different possibilities for those individuals and all of these different atoms would be lions. Therefore, the set of the concept for ‘lion’ would have many different lion atoms but there would only be two lion individuals. So, when quantifying we would like to quantify over Simba and Mufasa, rather than all the different lion-atoms.

To do this, we need a new operator called IND which, given a category concept, extracts all individual concepts (defined as members of the set of individual concepts, \mathcal{I}) which are a subset of that concept.

$$\llbracket \text{IND}(\langle \varphi, s \rangle) \rrbracket = \{ \langle \mathbf{p}, \mathbf{p} \rangle \in \mathcal{I} \mid \forall x (\mathbf{p}(x) \rightarrow \varphi(x)) \}$$

For example, given the concept, $\langle \mathbf{lion}, \text{lion} \rangle$, $\text{IND}(\langle \mathbf{lion}, \text{lion} \rangle)$ would give us the set $\{ \langle \mathbf{s}, \mathbf{s} \rangle, \langle \mathbf{m}, \mathbf{m} \rangle \}$ consisting of the concepts for Simba and Mufasa (as shown in Figure 1). A generalised quantifier, then, would operate over that set of concepts, using μ on each individual concept to evaluate the predicate.

$$\begin{aligned} \llbracket \text{Five lions have a mane} \rrbracket &= \llbracket \text{Five} \rrbracket (\text{IND}(\langle \mathbf{lion}, \text{lion} \rangle)) (\lambda x. \llbracket \text{has a mane} \rrbracket (x)) \\ \llbracket \text{Every lion has a mane} \rrbracket &= \forall_{\langle \mathbf{x}, x \rangle \in (\text{IND}(\langle \mathbf{lion}, \text{lion} \rangle))} (\mu_{x \sim \langle \mathbf{x}, x \rangle} \llbracket \text{has a mane} \rrbracket (x)) \end{aligned}$$

While it is clearly necessary to quantify over each individual concept in a particular context, sometimes we want to make a quantificational statement about a concept in general. For example, the statement, “all men are created equal” is not merely a claim about whichever particular men (or women) who happen to exist right now; it is a claim about all men (and

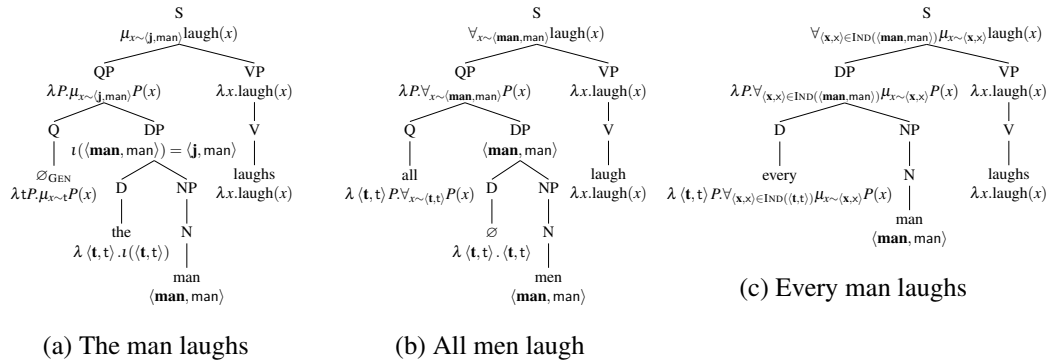


Figure 2 Kinds of quantification with atom-quantified individual and category concepts (a-b) and individually-quantified category concepts (c).

women) who could exist. Indeed, many have remarked on the quasi-generic flavour of non-partitive ‘all’ (Partee 1995; Gil 1995; Brisson 1998) which is missing from ‘every’.

We can address this difference under this theory by positing two basic forms of quantification:

- i. Individual-quantification (where we quantify over individual concepts using IND)
- ii. Atom-quantification (where we quantify over atoms directly via sampling).

Atom quantifiers quantify over the atoms of a concept and crucially, these atoms are *sampled* from the concept. Individually quantifier (like every or five), on the other hand, quantify over the individual concepts, not atoms directly. So, μ and non-partitive ‘all’ are atom quantifiers while ‘every’ is an individual quantifier:

$$\begin{aligned} \llbracket \text{Lions have manes} \rrbracket &= \mu_{x \sim \langle \text{lion}, \text{lion} \rangle} \llbracket \text{has a mane} \rrbracket(x) \\ \llbracket \text{All lions have a mane} \rrbracket &= \forall_{x \sim \langle \text{lion}, \text{lion} \rangle} \llbracket \text{has a mane} \rrbracket(x) \\ \llbracket \text{Every lion has a mane} \rrbracket &= \forall_{\langle x, x \rangle \in \text{IND}(\langle \text{lion}, \text{lion} \rangle)} (\mu_{x \sim \langle x, x \rangle} \llbracket \text{has a mane} \rrbracket(x)) \end{aligned}$$

This means that when we say ‘all’, we merely sample a number of atoms and check whether all of *the sampled atoms* belong to the predicate. Conversely, ‘every’ requires that we check each individual concept, rather than just a number of sampled atoms. Matthewson (2001) argues that non-partitive uses of English ‘all’ have underlyingly a bare plural, unlike partitive uses or quantification with ‘every’. My analysis is similar but claims that the generic flavour arises from the difference between atom and individual quantification (see Figure 2).

People sometimes think that universally quantified sentences are true if the corresponding generic sentence is true. For example, despite being aware that most lions are not adult male lions, people will often accept with the statement that “all lions have manes” (Leslie, Khemlani & Glucksberg 2011). Leslie et al. (2011) account for this by arguing that participants

Set	Typographic convention	Examples	Use
\mathcal{F}	Normal serif font	f, g, h	Relational functions
\mathcal{P}	Boldface	P, Q	Predicates (e.g. lion (x) or Superman (x))
\mathcal{S}	Sans-serif	P, Q	Sampling propensities

Table 1 Typographic conventions for different kinds of terms.

are switching the ‘all’ for the “default” quantifier, GEN. My view is that this phenomenon occurs due to the stochastic nature of sampling from a sampling propensity; occasionally people will simply not sample any atom that falsifies the claim (e.g. they will just happen to only sample lion atoms who have manes).

Crucially, the theory predicts that while people will do this with ‘all’ (an atom-quantified quantifier), they shouldn’t with ‘every’ (an individually-quantified quantifier) because ‘every’ operates over all (relevant) individual concepts rather than sampling atoms directly. As [Leslie et al.](#)’s experimental materials looked only at statements with ‘all’, future work could see if this prediction is borne out by evaluating differences in people’s acceptance of ‘every’ v.s. ‘all’ in these kinds of statements. Indeed, to my ears, while both (7) and (8) are false, (7) is more appealing than (8).

(7) All lions have manes.

(8) Every lion has a mane.

5 Formalism

5.1 Syntax

Signature The signature of this system is a tuple consisting of four parts:

- i) \mathcal{F} : The set of function symbols
- ii) \mathcal{P} : The set of predicate symbols
- iii) \mathcal{S} : The set of sampling propensities.
- iv) ar: An arity function such that $\mathcal{F} \cup \mathcal{P} \rightarrow \mathbb{N}$.

To help with clarity, each set has its own typographic conventions (see Table 1).

Alphabet The alphabet, \mathcal{A}^* consists of all members of $\mathcal{P} \cup \mathcal{F} \cup \mathcal{S}$ and standard first-order logic (FOL) symbols as well as $\mu, \rangle, \langle, \sim, \text{IND}$, and \in . There are also three kinds of variables, regular variables (x, y, \dots) , predicate variables $(\mathbf{x}, \mathbf{y}, \dots)$, and sampling variables (x, y, \dots) . The latter two are used when quantifying over individual concepts (e.g. with IND) as in $\llbracket \text{Every lion has a mane} \rrbracket = \forall_{\langle \mathbf{x}, \mathbf{x} \rangle \in (\text{IND}(\langle \mathbf{lion}, \mathbf{lion} \rangle))} (\mu_{x \sim \langle \mathbf{x}, \mathbf{x} \rangle} \llbracket \text{has a mane} \rrbracket(x))$.

Well-formed terms The set, $\mathcal{T} \subset \mathcal{A}^*$ of well-formed terms is the same as FOL.

Well-formed sampling terms The set of well-formed sampling-terms, $\mathcal{B} \subset \mathcal{A}^*$ is defined as follows:

- i. If $s \in \mathcal{S}$ (e.g. s is a sampling propensity) and φ is a well-formed formula with a free variable, then the concept for that pair, $\langle \varphi, s \rangle \in \mathcal{B}$ and $\iota(\langle \varphi, s \rangle) \in \mathcal{B}$.
- ii. If x is a sampling variable and \mathbf{x} is a predicate variable, then $\langle \mathbf{x}, x \rangle \in \mathcal{B}$.

Sampling terms include primitive concepts (e.g. $\langle \mathbf{drink}, \text{drink} \rangle$ or $\langle \mathbf{John}, \text{John} \rangle$), complex concepts (e.g. $\langle \lambda x. \llbracket \text{cold} \rrbracket(x) \wedge \mathbf{drink}(x), \text{drink} \rangle$), definite descriptions (e.g. $\iota(\langle \mathbf{man}, \text{man} \rangle)$) and combinations of sampling and predicate variables (e.g. $\langle \mathbf{x}, x \rangle$).

Well-formed formulae The set of well-formed formulae, $\mathcal{W} \subset \mathcal{A}^*$ can be defined inductively as follows:

- i. If φ is a WFF without quantifiers in FOL, then $\varphi \in \mathcal{W}$.
- ii. If $\varphi \in \mathcal{W}$, x is a variable and $\langle s, s \rangle \in \mathcal{B}$, then $(\forall_{x \sim \langle s, s \rangle} \varphi) \in \mathcal{W}$.
- iii. If $\varphi \in \mathcal{W}$, x is a variable and $\langle s, s \rangle \in \mathcal{B}$, then $(\exists_{x \sim \langle s, s \rangle} \varphi) \in \mathcal{W}$.
- iv. If $\varphi \in \mathcal{W}$, x is a variable and $\langle s, s \rangle \in \mathcal{B}$, then $(\mu_{x \sim \langle s, s \rangle} \varphi) \in \mathcal{W}$.
- v. If $\varphi, \psi \in \mathcal{W}$, \mathbf{x} is a predicate variable, and x is a sampling variable, then $(\forall_{\langle \mathbf{x}, \mathbf{x} \rangle \in \text{IND}(\psi)} \varphi) \in \mathcal{W}$.
- vi. If $\varphi, \psi \in \mathcal{W}$, \mathbf{x} is a predicate variable, and x is a sampling variable, then $(\exists_{\langle \mathbf{x}, \mathbf{x} \rangle \in \text{IND}(\psi)} \varphi) \in \mathcal{W}$.

5.2 Semantics

A structure in the language is a quintuple, $(\mathbb{D}, \sigma, I, \mathcal{C}, \mathcal{I})$, consisting of the domain, \mathbb{D} , the signature, σ , and the interpretation function, I, \mathcal{C} , and \mathcal{I} . \mathcal{C} is the set of concepts and must meet the following condition.

$$\mathcal{C} = \{\langle \mathbf{p}, \mathbf{p} \rangle\} \text{ where for all } \langle \mathbf{p}, \mathbf{p} \rangle \in \mathcal{C}, \mathbf{p} \in \mathcal{S} \wedge \mathbf{p} \in \mathcal{P} \wedge \text{ar}(\mathbf{p}) = 1$$

$\mathcal{I} \subseteq \mathcal{C}$ is the set of individual concepts in the model. These are concepts which refer to a single individual, e.g. Clark Kent.

Sense as sampling propensity

Interpretation function We use the standard interpretation from FOL for basic terms, \top , \perp and so on. Well-formed formulae without free variables have interpretations in the range $[0, 1]$

Connectives The following definitions are here for completeness, however any t -norm based set of connectives would be appropriate. If φ and ψ are well-formed formulae, then:

$$\llbracket \neg\varphi \rrbracket = 1 - \llbracket \varphi \rrbracket \quad \llbracket \varphi \wedge \psi \rrbracket = \min(\llbracket \varphi \rrbracket, \llbracket \psi \rrbracket) \quad \llbracket \varphi \vee \psi \rrbracket = \max(\llbracket \varphi \rrbracket, \llbracket \psi \rrbracket)$$

5.2.1 Sampling propensities and atom-quantifiers

- i. If $s \in \mathcal{S}$, (e.g. if s is a sampling propensity) then $\llbracket s \rrbracket$ is a function from \mathbb{D} to \mathbb{R} such that for all $x \in \mathbb{D}$, $s(x) > 0$.⁴
- ii. If φ is a well-formed formula and $s \in \mathcal{S}$ then their associated sampling term, $\llbracket \langle \varphi, s \rangle \rrbracket : \mathbb{D} \rightarrow [0, 1]$ is the following function:

$$\llbracket \langle \varphi, s \rangle \rrbracket(x) = \begin{cases} \frac{\llbracket s \rrbracket(x)}{\sum_{x \in \mathbb{D} | \llbracket \varphi(x) \rrbracket = 1} \llbracket s \rrbracket(x)} & \text{if } x \in \{x \in \mathbb{D} | \llbracket \varphi(x) \rrbracket = 1\} \\ 0 & \text{otherwise} \end{cases}$$

Otherwise put, it is a probability distribution over the set of the domain where φ is true normalised according to s (other normalisation functions could be alternatives, e.g. soft-max).

- iii. If φ is a well-formed formula, and $\langle \mathbf{t}, \mathbf{t} \rangle \in \mathcal{B}$ is a well-formed sampling term, then:

$$(9) \quad \llbracket \forall_{x \sim \langle \mathbf{t}, \mathbf{t} \rangle} \varphi \rrbracket(\langle \mathbf{t}, \mathbf{t} \rangle) = \begin{cases} 1 & \text{if } 1 = \sum_{x \in \mathbb{D}} \llbracket \varphi \rrbracket(x) \cdot \llbracket \mathbf{t} \rrbracket(x) \\ 0 & \text{otherwise} \end{cases}$$

$$(10) \quad \llbracket \exists_{x \sim \langle \mathbf{t}, \mathbf{t} \rangle} \varphi \rrbracket(\langle \mathbf{t}, \mathbf{t} \rangle) = \begin{cases} 1 & \text{if } 0 < \sum_{x \in \mathbb{D}} \llbracket \varphi \rrbracket(x) \cdot \llbracket \mathbf{t} \rrbracket(x) \\ 0 & \text{otherwise} \end{cases}$$

$$(11) \quad \llbracket \mu_{x \sim \langle \mathbf{t}, \mathbf{t} \rangle} \varphi \rrbracket(\langle \mathbf{t}, \mathbf{t} \rangle) = \sum_{x \in \mathbb{D}} \llbracket \varphi \rrbracket(x) \cdot \llbracket \mathbf{t} \rrbracket(x)$$

Note that here, I give a characterisation of *competence* without stochasticity rather than *performance* where we expect actual sampling from $\langle \mathbf{t}, \mathbf{t} \rangle$. These are atom quantifiers which go directly over the potential atoms in the conceptual extension of a concept (e.g. generics and normal predication or non-partitive all) using the concept's sampling propensity, rather than individual quantifiers which go over a set of individual concepts.

⁴ This means that all sampling propensities have a (small) probability of generating any atom in the domain. In a concept, $\langle \mathbf{p}, \mathbf{p} \rangle$, the extension, \mathbf{p} , restricts the sampling propensity, \mathbf{p} , to only sample from the extension. Since all sampling propensities are non-zero for the entire domain, no combination of a sampling propensity and a distribution can lead to an improper probability distribution.

5.3 Individual-quantifiers and models

If φ and ψ are well-formed formulae and s is a sampling process, then:

$$\begin{aligned} \llbracket \text{IND}(\langle \varphi, s \rangle) \rrbracket &= \{ \langle \mathbf{p}, \mathbf{p} \rangle \in \mathcal{S} \mid \forall x (\mathbf{p}(x) \rightarrow \varphi(x)) \} \\ \llbracket \forall_{\langle \mathbf{x}, \mathbf{x} \rangle \in \text{IND}(\langle \psi, s \rangle)} \varphi \rrbracket &= \bigwedge_{\langle \mathbf{x}, \mathbf{x} \rangle \in \llbracket \text{IND}(\psi) \rrbracket} \varphi \\ \llbracket \exists_{\langle \mathbf{x}, \mathbf{x} \rangle \in \text{IND}(\langle \psi, s \rangle)} \varphi \rrbracket &= \bigvee_{\langle \mathbf{x}, \mathbf{x} \rangle \in \llbracket \text{IND}(\psi) \rrbracket} \varphi \end{aligned}$$

The latter two define universal and existential quantification over individual concepts as big conjunctions or disjunctions of φ for each individual in $\text{IND}(\psi)$ (where φ possibly includes a free concept variable, $\langle \mathbf{x}, \mathbf{x} \rangle$, which is bound by the individuals). This definition only works in the case where $\text{IND}(\psi)$ is finite, but it could be adapted for the infinite case.

We can also define the iota operator similarly:

$$\llbracket \iota(\langle \varphi, s \rangle) \rrbracket = \begin{cases} \langle \mathbf{p}, s \rangle & \text{if } \exists! \mathbf{p} \text{ such that } \exists \mathbf{p} \text{ such that } \langle \mathbf{p}, \mathbf{p} \rangle \in \mathcal{S} \text{ and } \forall x \mathbf{p}(x) \rightarrow \varphi(x) \\ \text{otherwise undefined} & \end{cases}$$

Note that this iota operator is defined in such a way so that we extract an individual concept and use its extension while using the sampling propensity of the input. As defined, if there is no individual which is a subset of set defined by $\varphi(x)$, the iota operation is undefined. With this definition, ‘the man’ or ‘the villain’ would have different sampling propensities even when referring to the same individual.

The iota operator only works if there is a unique *extension* of an individual concept which is a subset of φ . To handle ‘Superman’/‘Clark Kent’ cases, there can be multiple individual concepts in \mathcal{S} which are subsets of φ provided they have identical extensions (but possibly differing sampling propensities). This is because, ultimately, we only need the extension from the individual since the sampling-propensity is provided by the definite description.

To access the predicate or sampling propensity of something retrieved by the iota operator, we add the following syntactic sugar. If $\iota(\langle \varphi, s \rangle) = \langle \mathbf{p}, s \rangle$, then:

$$\iota(\langle \varphi, s \rangle)_{\text{pred}} = \mathbf{p} \quad \iota(\langle \varphi, s \rangle)_{\text{samp}} = s$$

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